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# STRENGTHENING METHODOLOGY FOR LIGHTLY REINFORCED CONCRETE FRAMES-I

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**NIST**

United States Department of Commerce  
Technology Administration  
National Institute of Standards and Technology

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U.S. Department of Commerce  
Ronald H. Brown, *Secretary*  
National Institute of Standards and Technology  
Raymond G. Kammer, *Acting Director*



## ABSTRACT

An analytical method for evaluating the inelastic dynamic structural response of lightly reinforced concrete (RC) frames strengthened by infilled shear walls was developed. This method consists of the development of hysteresis failure models for existing and strengthened RC frames and the incorporation of the models into computer program IDARC for use in analytical study. The hysteresis models were developed by, first, using the system identification techniques to characterize the load-deformation histories of fifty-five RC frame tests in terms of the stiffness degradation parameter  $\alpha$ , the strength degradation parameter  $\beta$ , and the pinching parameter  $\gamma$ . Next, multi-variable regressions were performed to relate  $\alpha$ ,  $\beta$ ,  $\gamma$  as functions of the specimen's material and geometric properties and reinforcement parameters. The empirical expressions resulted from these regressions are the hysteresis failure models. The models were validated by analyzing a one-story, one-bay infilled frame, tested by Aoyama et al., and a three-story, one-bay infilled frame tested by Higashi et al. The results of the analyses showed that (1) hysteresis models developed using one-story, one-bay frames can be incorporated into IDARC for the analysis of frames with more than one-story height, and (2) reasonable predictions of structural behavior, both in terms of ultimate load capacity and in absorbed energy on the per cycle basis, can be achieved using the hysteresis models. Thus, in the present form, the hysteresis models can be used in parameter study to assist in the design of strengthening of RC frame structures.

**Keywords:** Analytical; reinforced concrete; dynamic analysis; experimental; frames; hysteresis models; infilled walls; system identification; multi-variable regression.

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# STRENGTHENING METHODOLOGY FOR LIGHTLY REINFORCED CONCRETE FRAMES

## 1. INTRODUCTION

### 1.1 Background

Forty-six of the fifty United States are vulnerable to the effects of strong earthquakes. A primary focus of earthquake engineering research in past decades has been on developing standards for seismic-resistant design and construction of new buildings. Much progress has been made in this area; by late 1991 all three major model building codes had adopted up-to-date seismic design requirements.

Efforts are now underway to develop similar standards for the seismic rehabilitation of existing buildings. The population of buildings that were designed and built without adequate consideration of seismic safety far exceeds that of buildings constructed with the benefit of a modern understanding of earthquake resistance. In areas where earthquakes occur infrequently, the building stock is especially vulnerable because technological advances that were adopted in high seismic regions often were not recognized as being necessary in seismically less active areas.

Unless properly designed and detailed, reinforced concrete (RC) buildings are vulnerable to earthquake ground shaking. The relatively large mass of concrete buildings creates high inertial forces. Catastrophic failures that occurred in the 1971 San Fernando, 1985 Mexico City, and 1988 Armenia earthquakes, among others, illustrate the vulnerability and potential for large loss of life in older or poorly designed and built RC buildings.

NIST has initiated a multiyear effort to develop rehabilitation guidelines for RC buildings. In previous years, in cooperation with researchers at Cornell University, a nonlinear dynamic analysis program for reinforced concrete frames (IDARC) was improved, and experimental tests of beam-column joint strengthening techniques were performed.

### 1.2 Goals and Objectives

In order to reduce the risk associated with RC structures that were designed and built without adequate consideration of seismic safety, an accurate understanding of the behavior of such structures under seismic loads must be developed. Similarly, the effectiveness of proposed strengthening schemes must be assessed. Information collected after actual earthquakes can provide preliminary insights. Experimental studies provide additional valuable information. However, analytical and computational methods are the

most time and cost effective methods for assessing large numbers of structures and strengthening schemes. The goals of the NIST existing buildings research project is to develop reliable tools that can be used to:

- accurately evaluate the performance of existing RC buildings under credible earthquake excitation,
- identify the critical weaknesses in the existing structures,
- reliably model strengthening schemes, and assess the effectiveness of different strengthening schemes.
- develop guidelines for strengthening RC buildings.

Increasingly sophisticated nonlinear dynamic analysis programs capable of analyzing the performance of RC structures under seismic loads are being developed. To obtain sufficiently accurate analyses of actual behavior, the hysteresis rules which characterize the behavior of RC structures under cyclic loads must be identified and incorporated into the analysis programs. The hysteretic behavior of strengthened elements must be similarly determined and incorporated.

Once reliable analytical techniques have been developed, the functional relationships between experimental load-displacement relationships and the physical characteristics of structural elements (such as geometric dimensions, material properties, and reinforcement patterns) can be determined through sensitivity analysis of critical parameters. Establishing sufficient functional relationships will make it possible to analyze the cyclic behavior of any RC structure, strengthened or unstrengthened.

Ultimately, these analysis techniques can be used to develop a reliable body of information about the efficacy of various retrofit techniques for common building types and structural systems. This information can be consolidated into guidelines for use by design engineers nationwide.

The objectives of this phase of the research were:

- to develop accurate hysteretic models using existing experimental data to describe the actual behavior under cyclic loads of existing RC frames with and without strengthening elements.
- to validate the accuracy of the hysteretic models by comparing predicted responses to existing experimental data.
- to develop tentative recommendations for effective applications of strengthening techniques.

### 1.3 Scope

The scope of this report is limited to the development of analytical methods for evaluating the structural performance of lightly reinforced concrete frames strengthened with infilled shear walls. The report is organized as follows:

- Chapter 2 describes commonly used and experimentally documented retrofit techniques.
- Chapter 3 presents information on the analysis program IDARC.
- Chapter 4 describes the selection of the experimental data sets for use in this study from among those amassed in a literature search of sources worldwide, the techniques used to identify hysteresis parameters for use with IDARC that accurately describe the experimental data, and the development of generally applicable hysteresis models using statistically based regression analysis techniques.
- Chapter 5 describes the validation of the models and their incorporation into IDARC.
- Chapter 6 summarizes the study and presents conclusions and recommendations.
- Chapter 7 lists the references used in this study.

Types of infilled shear walls considered include cast-in-place concrete and Multiple Precast concrete panels.

## 2. DISCUSSION OF REHABILITATION SCHEMES

Existing literature on seismic strengthening of RC frame structures was reviewed to identify common retrofit techniques and to locate available experimental data. This chapter presents general information about retrofit issues and techniques, and describes the assessment of available data which led to the selection of specific strengthening schemes for investigation in this project.

Seismic retrofit of existing buildings is particularly challenging because of the interrelated effects of any change to a structural system. For example, increasing strength generally results in a corresponding increase in stiffness, reducing the fundamental period of the building, which in turn results in an increase in the seismically-induced lateral forces. If new elements have significant mass, earthquake induced forces will be increased proportionally. Existing foundations may be insufficient to support massive new elements or resist overturning forces induced by new structural systems. For example, attempts to enhance the shear capacity of columns must be carefully designed to avoid increasing their flexural stiffness, which would increase the shear forces on the column. Therefore, "cookbook" solutions to rehabilitation problems would not be realistic. However, general recommendations and rehabilitation guidance can be developed based on research and experience, with the caveat that the appropriateness of the guidelines must always be assessed in the context of the specific building being retrofit.

The seismic capacity of existing RC frame buildings can be improved by

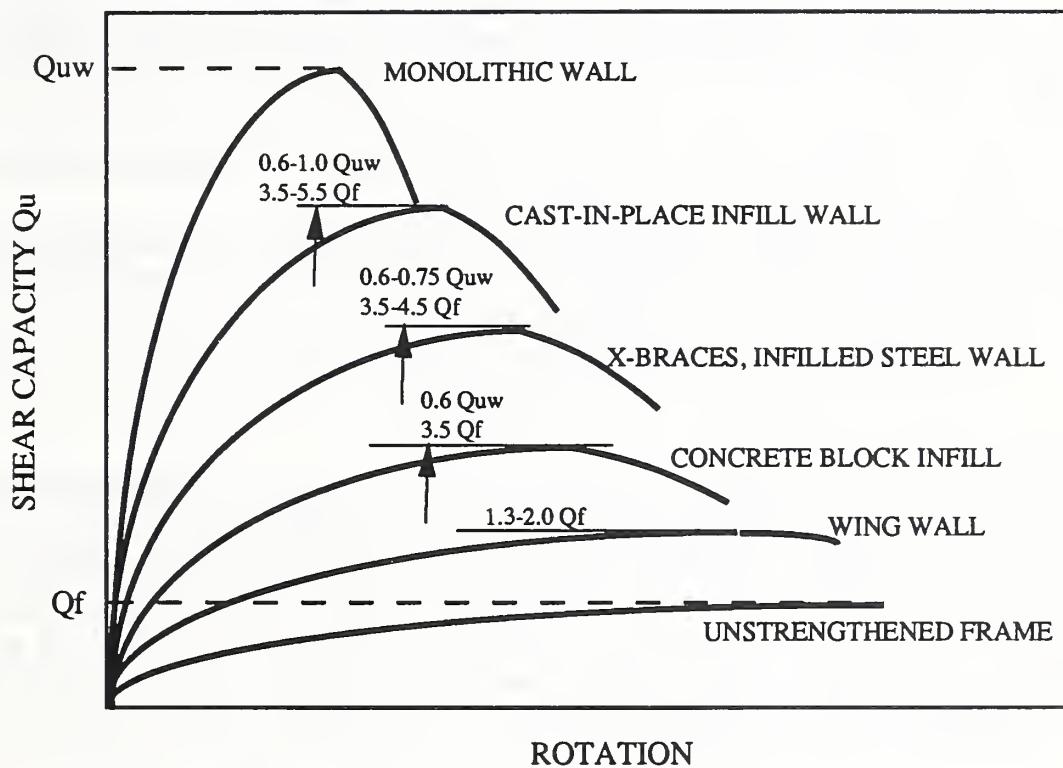
- increasing the lateral strength,
- improving the ductility, or
- using a combination of strength and ductility enhancements.

Figure 2.1, after Sugano and Fujimura<sup>2</sup>, generically illustrates how these approaches affect a structure's force-displacement curve. The trends illustrated in Figure 2.1 are supported by experimental results obtained by Sugano and by other researchers. In general, strength is increased by adding new elements; ductility is enhanced by reinforcing existing elements.<sup>28</sup> Rehabilitation schemes for concrete frame buildings include:

- adding infilled walls or steel cross-bracing in frame openings
- adding new continuous shear walls or braces through existing floor slabs between existing column lines
- adding buttresses or frames at the building exterior
- increasing the thickness of existing walls or infilled walls
- adding wing walls to columns
- jacketing existing columns and/or beams

- strengthening existing joints

The success of any rehabilitation project depends, of course, on adequate detailing of connections between the new and existing elements.



Quw: Ultimate Shear Capacity of Monolithic Wall-Frame Construction  
 $Q_f$  : Ultimate Shear Capacity of Unstrengthened Frame.

Figure 2.1 Relative Shear Capacities of RC Frame Strengthened By Different Techniques (After Sugano et al.<sup>2</sup>)

Four experimentally-proven techniques for seismic strengthening of RC structures are described below. Most experimental test programs evaluate the behavior of single frame units or single bays to assess the potential effectiveness of various proposed retrofit schemes. Very little data are available on the effectiveness of these schemes in complete structures, and almost no specific design guidance has been proposed. The intent of the NIST research effort is to make use of the available experimental data, or if necessary to conduct experimental study, to develop valid analytical models which can assess the effectiveness of retrofit schemes in prototypical and actual buildings. Ultimately, design guidelines can be developed using the results of sufficient analytical studies.

## 2.1 Infilled Walls

Adding wall elements to RC frames by infilling the frame cells can add strength and stiffness to a building. Infilled walls that have been experimentally tested have been constructed using:

- cast-in-place concrete, connected to the original construction with dowels, epoxy, or wedge anchors; or shear keys,
- precast concrete, using either single or multiple panels, connected by welding to new steel anchors in the original construction,
- masonry, either brick or concrete block,
- steel panels, connected by welding to new anchors, or
- pneumatically applied concrete (shotcrete).

Rigid infilled walls act primarily as shear walls. Because of the relative rigidity of the infilled bays, the demand on the existing frame is substantially reduced. This is especially true for buildings with rigid diaphragms.<sup>33</sup> Frames with less rigid infill, such as unreinforced masonry often used to form exterior walls in original construction, will behave like braced frames with the infill acting as a compression strut.<sup>33</sup> A test of unreinforced brick masonry infill by Krause and Wight suggests that this method of infill can lead to unstable hysteretic behavior.<sup>14</sup>

Tests of solid CIP concrete infilled walls demonstrate that the strength and stiffness of the retrofit structure approaches that of a monolithically cast wall (see Figure 2.1). For CIP infilled walls, once maximum strength is reached, strength degradation is moderate, but not abrupt. The method of anchoring the infilled wall to the existing frame has some effect on behavior, but in general, all tests reviewed in the present literature search showed substantial increases in strength and stiffness, regardless of anchoring technique used. Tests of frames infilled with precast concrete panels show that with this technique the retrofit frame attains slightly less than half the strength of the monolithic wall. As strength levels decrease, the rate of strength degradation after the maximum load is reached also decreases, i.e. the ductility increases. In tests by Sugano and Fujimura<sup>2</sup>, a frame retrofit with reinforced concrete block masonry infill (using a Japanese butterfly

shape not commonly available in this country) acquired over half the strength of a monolithically cast wall. A study of the effects of concrete masonry infill by Zarnic and Tomazevic,<sup>44,45</sup> as part of a US-Yugoslav joint research effort, reported significant increases in lateral resistance and stiffness over the bare frame response. Studies in this country by Klingner and Bertero<sup>20</sup>, and Brokken and Bertero<sup>27</sup>, have produced similar results. A very limited amount of information on pneumatically applied infill exists. Tests by Gaynor<sup>18</sup> showed that shotcrete infill did increase strength, but no comparisons to monolithically cast walls were made.

Openings for doors, windows, mechanical/electrical conduits, or other needs can reduce the effectiveness of infilled walls. A small number of experiments have examined the effect of openings in infilled walls.<sup>4,16,18</sup>

Partial walls added adjacent to the column lines are known as wing walls. This rehabilitation method is intermediate between full infill and column strengthening. The relative levels of ductility and strength increases are dependent on the proportions and detailing of the original and strengthened elements.

Among the practical problems associated with designing effective infilled walls is providing sufficient anchorage to ensure good vertical continuity in multi-story buildings. Some engineers have proposed schemes which add continuous multi-story CIP walls through holes cut in the floor slabs on lines adjacent to, rather than directly on, the column lines in an attempt to avoid this problem.<sup>41</sup>

Designers using infilled walls must consider uplift that may be created in the infilled bays. Foundations may require re-examination and strengthening due to the newly created overturning forces and the added weight of the infill. Drag struts or collectors may be needed to transfer diaphragm forces to the new shear wall elements.

Adding infilled walls can create significant functional changes which must be considered when evaluating potential rehabilitation schemes. Loss of windows, interrupted travel paths, and aesthetic changes to the building interior and exterior are common problems with most rehabilitation schemes.

## 2.2 Steel Bracing, Frames, and Trusses

Steel bracing, frames, or trusses can be added to existing RC frame buildings to supplement the existing lateral force resisting system. Steel members can be inserted in frame openings to enhance the ductility and strength of the existing concrete frame. Complete steel structural systems which are continuous through the floor slabs or attached to the building exterior can be designed to essentially replace the existing lateral force resisting system. These schemes typically require the addition of collectors to transfer the load from floor slabs to the new frame.

Sugano and Fujimura<sup>2</sup> strengthened and tested identical frames using a variety of infilling and bracing techniques. They found that steel bracing provided a moderate increase in strength compared to the increases provided by CIP solid infill. However, the steel system did provide substantial ductility and energy absorption capacity. For simple cross bracing, Sugano found that connections to the concrete were the vulnerable link in the system. Goel and Lee<sup>15</sup> tested a rehabilitation technique utilizing a complete steel truss inserted into the frame opening. They found that the horizontal and vertical steel members acted as both truss members and as supplements to the moment resistance of the concrete frame, this despite the fact that no shear connectors were used on the vertical members. Apparently by using truss inserts the connection problems associated with cross bracing are minimized. Higashi et al.<sup>4</sup> tested steel bracing, trusses, and moment frames inserted in the frame opening and had similar results.

Jones and Jirsa<sup>22</sup> tested a two-thirds scale model of a concrete frame building retrofit with a concentrically braced steel frame attached to the exterior of the building and designed to carry the entire seismic load. They found that the system greatly improved the performance of the building and protected the concrete columns from shear failure, even after buckling of the steel frame. However, weld failures and construction problems pointed out the need for high quality workmanship and careful consideration of constructability as details are developed.

Functional changes created by steel braces and frames (loss of windows, alteration of traffic patterns, etc.) are similar to those caused by infilling. Diagonal elements can be challenging to incorporate into an existing building in a visually pleasing manner. If elements are added to the building exterior, disruption to building occupants during construction can be minimal.

## 2.3 Column Strengthening

Inadequate ductility of the columns is frequently found to be the weak link in the seismic resistance of a RC frame building. Column deterioration, due to insufficient shear strength and lack of core confinement, can cause abrupt, catastrophic failures of entire stories or entire buildings. Building configurations that can exacerbate the problem include soft and weak story designs; short and "captured" columns; and weak column-strong beam configuration.

Detailing requirements for new structures call for closely spaced transverse reinforcement in the regions of plastic hinging in order to provide ductile rather than brittle behavior under lateral loads. Most column strengthening techniques add transverse reinforcement in an attempt to improve ductility. Column strengthening techniques that have been experimentally studied include:

- encasing the column in steel plates or pipes and filling the gap with grout,

- attaching tightly fitted steel bands or straps around the column,
- enlarging the column with additional reinforced concrete, using either welded wire fabric or closely spaced ties for transverse reinforcement, and either pneumatically applied or CIP concrete.

These techniques are often generically termed "jacketing". Where the flexural capacity of the column is adequate, gaps are left at top and bottom of the jacketing to avoid increasing the flexural capacity and related induced shear forces. Testing programs by Hayashi et al.,<sup>3</sup> Nene,<sup>47</sup> and Bett et al.<sup>24</sup> have verified the ability of these techniques to strengthen and stiffen columns.

Jacketing columns creates many of the same construction and occupant dislocation problems as does infilling frames. However, permanent disruption of traffic flow, loss of window space, and other major changes in building function will not occur.

Anticipating public demand for immediate strengthening of structures following earthquake forecasts, Kahn<sup>46</sup> investigated three quick and simple jacketing techniques: strapping the column with steel packaging bands, bolting on steel U-clamps, and hammering a plain steel rod spirally around the column. Testing showed that all three techniques greatly increased the ductility of the columns. Because the steel is not enclosed in concrete, these easy to install schemes are aesthetically unpleasing. Architectural coverings could solve this problem.

A rehabilitation scheme investigated by Roach and Jirsa<sup>23</sup> consisted of casting new reinforced concrete piers around three sides of the columns at the exterior of a building. The prototype tested was typical of an architectural style widely used in the 1950's and 1960's: a reinforced concrete frame with deep spandrel beams and windows filling the remaining openings. With this retrofit scheme, the new piers partially filled the window openings. Dowels were anchored into the existing concrete using epoxy to achieve monolithic behavior of the old and new concrete. This technique is intended to increase both flexural and shear strength of the columns, and provide continuity in the new elements over the entire height of the building. Testing showed that the scheme was successful in shifting the mode of failure in the frame from shear in the columns to flexure in the beams. The new piers are aesthetically acceptable even though they change the visual impact of the building. Because the new elements are on the exterior of the building, disruption during construction may be minimal, depending on whether the existing windows can be left in place.

Adding wing walls adjacent to columns, discussed in the section on infilled walls, can provide benefits similar to the piers described above.

## 2.4 Beam-Column Joint Upgrading

In theory, improving the strength and/or toughness of the beam-column joints in a concrete frame will improve the overall ductility of the building. Although many experimental studies of the behavior of typical interior and exterior joints under cyclic loads have been done, there has been very little experimental testing of joint strengthening techniques. In an attempt to partially fill this gap, NIST, in an earlier phase of this multi-year existing concrete buildings research program, carried out a joint study at Cornell University to design, construct, and test several joint strengthening techniques.

Following the 1985 Mexico earthquake, Alcocer and Jirsa<sup>42</sup> tested joint strengthening. The scheme they used required perforating the slab in order to construct a steel and concrete jacket around the joint, columns, and in some cases, beams. In addition to longitudinal bars and transverse steel around the jacketed columns and beams, the retrofit scheme included a welded steel frame of angles and straps intended to confine the concrete in the joint. They found that the technique enabled them to change the behavior of the specimens from weak column-strong beam to strong column-weak beam. They state that the placement of forms and concrete was not difficult, but it did require "intensive labor and artful detailing that might be uneconomical for U.S. practice."

The NIST-Cornell study, reported by Beres et al.,<sup>43</sup> investigated the behavior of two simple, inexpensive, easy to implement rehabilitation schemes. For interior joints, the retrofit was designed to prevent the pullout of discontinuous bottom beam reinforcement. Steel channel sections were bolted into the bottom surfaces of beams on each side of the joint, and connected by steel bars welded to the channels. Testing under cyclic loads showed the scheme to be successful in preventing pullout, increasing shear strength, and reducing the rate of strength deterioration. The stiffness and energy dissipation characteristics were essentially unchanged. For exterior joints, the retrofit was designed to reduce vertical cracks propagating in the column lap splice zone above the joint by eliminating loss of cover due to prying at the outside (non-beam side) of the joint. Steel plates above and below the beam were through-bolted to a continuous steel plate on the outside of the joint. Testing showed significant improvements in the behavior of the specimen: cover was protected, and peak strength, initial stiffness, and energy dissipation capacity were increased. However, strength deterioration after peak strength was achieved was more rapid than for the unstrengthened specimen.

The retrofit schemes investigated at Cornell show great promise, particularly in light of the fact that they are relatively inexpensive and non-disruptive both aesthetically and during construction. It may be possible to implement schemes of this type building-wide without requiring long term relocations of people and contents. However, these schemes are specifically designed to rectify problems common to concrete construction of the 1950's and 1960's (which typically have 1) little or no transverse reinforcement within the beam-column joint region, 2) widely spaced column ties, and 3) discontinuous

negative and positive beam reinforcement with approximately 150 mm (6 inches) embedment length into the column), subject to moderate (0.2g) earthquake loads, and they may not be useful for buildings which were constructed with different details or that are sited in areas of greater expected accelerations.

## 2.5 Collection of Data

Existing experimental data were obtained for use in developing and validating analytical models. Data sets for existing and strengthened conditions were collected for frames, beam-column joints, and columns. Seventy sets of data were collected on frames and infilled walls. More than half of the data were on behavior of various retrofit schemes. In contrast, over one hundred sets of data were collected on the behavior of beam-column joints, but only five of the tests were on strengthened joints. Twenty-three data sets were obtained on columns that had been experimentally tested; only nine had been strengthened, and those nine included a wide variety of dissimilar strengthening schemes.

The amount of data available led to the decision to investigate variations on infilled walls in this phase of the research program. The seventy available data sets on existing and strengthened frames were culled to identify specific cases for further use. The selected specimens shared common physical and geometric characteristics, were tested using similar quasi-static cyclic loads, and produced results that were published as readable hysteresis loops. The specimens selected for study are described in greater detail in Section 4.1.

### **3. INELASTIC ANALYSIS OF REINFORCED CONCRETE FRAMES USING IDARC**

#### **3.1 Introduction to Program IDARC**

The program IDARC (Inelastic Damage Analysis of Reinforced Concrete Frame-Shear Wall Structures) was developed from 1985 to 1987 at the State University of New York at Buffalo by Park, Reinhorn, and Kunnath<sup>35</sup>. The program, developed for use as a research tool, was designed to overcome several limitations typical of previous analytical programs. Park et al. describe three major drawbacks in extant inelastic analysis programs that were overcome by IDARC:

- the analysis was carried out using equivalent properties of damaged or cracked sections of elastic models,
- the general hysteresis models used for inelastic analysis did not always fit actual behavior (shear and flexure) of reinforced concrete elements, and
- strength limits, which had to be precomputed off-line, remained unchanged throughout the analysis.

IDARC performs in the first phase a static analysis which determines component properties, inelastic behavior and failure mode under monotonic loading, and natural period. In the second phase, a step-by-step inelastic dynamic response analysis using the Newmark- $\beta$  method, is performed. A hysteresis model that accounts for shear and flexure was developed for use in this part of the program. The program also computes and updates strength levels of components. In the third phase, the program performs a damage analysis, calculating damage indices for individual members, specified subsections, and the entire building. A detailed description of the program as originally released can be found in Park et al.<sup>35</sup>

NIST sponsored additional development of the program at Cornell University in the early 1990's. A description of the improvement of the hysteresis model and development of a System Identification Method can be found in El-Borgi et al.<sup>36</sup> Researchers at NIST have developed further refinements and modifications for use in specific projects.

IDARC uses two-dimensional analysis to evaluate the behavior of three-dimensional structures; transverse beam elements are used to model the effects of slabs and beams connecting parallel frames. Identical frames can be lumped together. Other elements available for modeling structures include beams, columns, shear walls, and edge columns.

In beam and column elements, rigid panel zones and flexibility distribution are accounted for using non-linear springs. Edge columns are modeled using inelastic axial springs. Transverse beams are modeled with elastic linear and rotational springs. Shear wall

elements are modeled using flexure and shear springs connected in series, each with independent inelasticity. This allows shear hysteresis to be modeled independently of the flexural hysteresis in these elements.

For this IDARC-based study of frames strengthened with infilled walls, each frame unit (one-story one-bay), whether strengthened or bare frame, is modeled using a single shear wall element rather than a combination of beam, column, and wall elements. Chapter 4 describes the development of hysteresis models for use with IDARC shear wall elements that describe the behavior of unstrengthened and strengthened single-story single-bay frames. Chapter 5 describes the validation of these models, including an assessment of the effectiveness of modeling multi-story multi-bay frames using stacks of these single-story single-bay units.

### 3.2 Three-Parameter Hysteresis Model

The accuracy of any dynamic inelastic response analysis is heavily dependent on the validity of the model used to describe the hysteretic behavior of the components. For analysis of reinforced concrete, the model must be sophisticated enough to describe stiffness degradation, strength deterioration, pinching behavior, and unsymmetric hysteresis. However, simplicity of the model is also at a premium, since a large number of inelastic springs are needed to model any given structure, and every additional parameter used to refine complex hysteresis loop shape adds to computational time and complexity.

The programmers of IDARC assessed many available hysteretic models and found that most of them were specifically aimed at a particular type of component such as beams, columns, or shear walls. Thus, most lacked the versatility needed to accurately describe the behavior of actual buildings. The IDARC designers developed a three-parameter model that can be used to describe the behavior of all types of structural elements. The parameters  $\alpha$ ,  $\beta$ , and  $\gamma$  determine the stiffness degradation, strength deterioration, and pinching behavior, respectively. Figure 3.1 and the descriptions below, taken from Park et al.,<sup>35</sup> describe the effects of the three parameters on a trilinear skeleton curve.

- $\alpha$  - "The stiffness degradation is introduced by setting a common point on the extrapolated initial skeleton curve line, and assumes that the unloading lines aim at this point until they reach the x-axis. The parameter  $\alpha$  specifies the degree of stiffness degradation, and, more importantly, the area enclosed by the hysteresis loops."
- $\beta$  - "The parameter  $\beta$  specifies the rate of strength degradation."

$\gamma$  - "The pinching behavior is introduced by lowering the target maximum point (A in Figure 3.1) to a straight level of  $\gamma P_y$  (B in Figure 3.1) along the previous unloading line. Reloading points aim this new target point 'B' until they reach the crack closing deformation. The stiffness of reloading paths is changed at this point to aim the previous target maximum point 'A'. The introduction of such a pinching behavior also leads to a reduction of hysteresis loop areas and indirectly, the amount of dissipated energy."

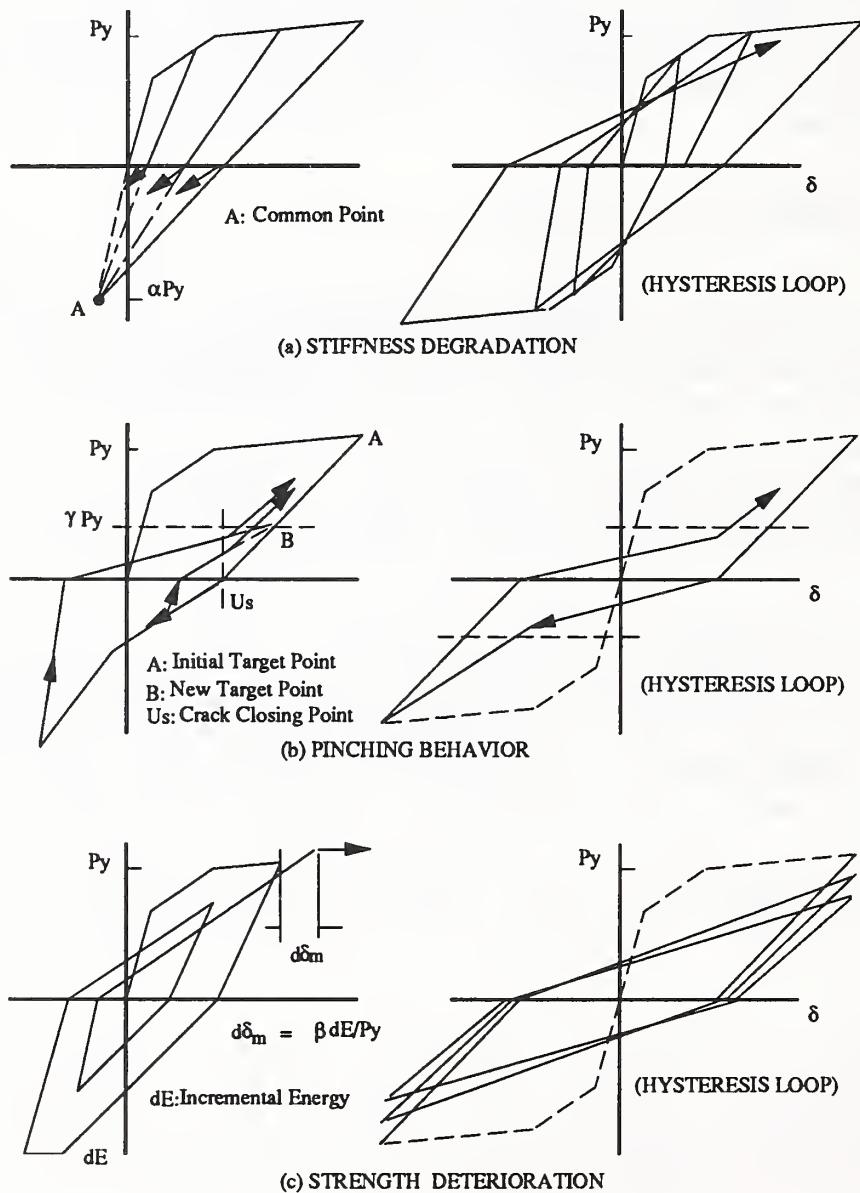


Figure 3.1 Three-Parameter Hysteresis Models  
(After Park, Reinhorn and Kunzath<sup>35</sup>)

NIST, in an earlier phase of this multi-year research project, supported a Cornell University effort to improve IDARC's basic hysteresis model. The results of that study are reported by El-Borgi et al.<sup>36</sup> The three-parameter model was refined to use smooth continuous curves to model hysteresis loops. Several problems associated with the hysteresis model of the original program were eliminated, including error accumulation due to overshooting during unloading.

The refined model requires that the  $\alpha$ ,  $\beta$ , and  $\gamma$  parameters be calibrated against experimental test records prior to use. El-Borgi et al.<sup>36</sup> refer to this task as the System Identification Method, and describe the procedure in their report. NIST researchers Stone and Taylor have incorporated the System Identification Method into an Interactive-Graphics based system identification software called NIDENT.<sup>40</sup> The calibration of the three-parameter model for this investigation is discussed in Chapter 4.

## 4. DEVELOPMENT OF HYSTERESIS MODELS FOR R/C FRAMES

As discussed in Chapter 3, the current program IDARC<sup>35</sup> requires pre-characterization of the hysteresis behavior of the structural components by means of the three parameters: stiffness degradation parameter  $\alpha$ , strength degradation parameter  $\beta$ , and pinching parameter  $\gamma$ . Even though IDARC offers default values for  $\alpha$ ,  $\beta$ , and  $\gamma$  based on a frame identification study by Yeh<sup>38</sup> (1988), these default values are judged to be too simplistic to correctly characterize the hysteretic response of reinforced concrete frame structures given the complexity and the innumerable factors which influence this behavior. This is especially true for structures which are strengthened by adding new structural elements, since the current default values of the three parameters were not calibrated by experimental results of strengthened structures. Thus, in order to accurately analyze existing or strengthened reinforced concrete frame structures using the program IDARC, it is crucial to obtain parameters ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) which have been calibrated by the results of experiments on both existing and strengthened frames.

The hysteresis models developed in this study, which are empirical expressions relating the three parameters  $\alpha$ ,  $\beta$ ,  $\gamma$  to the geometric and material properties of the structural frames, were calibrated using actual test results of the selected experiments described in section 4.1. The procedure used in developing the models, and the hysteresis models for various constructions indicated above, are described in section 4.2. Models have been developed which may be used to predict the hysteresis parameters of the following types of construction:

- bare frames
- monolithic wall-frame constructions
- frames strengthened by CIP infilled walls, with and without wall openings
- frames strengthened by multiple precast concrete panels, with and without wall openings

### 4.1 Relevant Experimental Programs

Experimental programs on seismic strengthening of RC frames conducted by Aoyama et al.<sup>8,9,10,11,12</sup>, Kahn<sup>1</sup>, Hayashi et al.<sup>3</sup>, Sugano et al.<sup>2</sup>, Higashi et al.<sup>4</sup>, Corley et al.<sup>5,6,7</sup>, Ogata et al.<sup>13</sup>, Gaynor<sup>18</sup>, and Shah<sup>16</sup> were selected for use in developing the hysteresis models in this study. These programs were selected based on the following criteria:

- The test specimens are one-bay one-story frames.
- The loading program is quasi-static reversed cyclic.
- Strengthening is accomplished by reinforced concrete infilled wall.

- Reinforcement details in the existing frame are typical of construction in the 1950's or 1960's.

The use of one-bay one-story frame tests limits the number of variables that need to be considered and permits direct comparison of test results between the various test programs. It also allows the most efficient utilization of existing test data relevant to seismic strengthening since the majority of seismic strengthening tests on RC frames are one-bay one-story. Further, the hysteresis models developed for RC frames based on one-bay one-story tests are versatile and may easily be incorporated into such programs as IDARC for use in the analysis of RC structures being strengthened by different schemes.

A total of fifty-five specimens were selected from these experimental programs. These consisted of five bare frames, twenty-one monolithic wall-frame constructions, twenty-one frames strengthened by CIP infilled wall (with and without wall opening), and eight frames strengthened by multiple precast concrete panels used as infilled wall. In most cases, the specimens were deliberately designed to have reinforcement details that are typical of lightly reinforced construction<sup>1,2,3,4,8,9,10,11,12,13</sup> - i.e., low longitudinal reinforcement ratio for columns, little or no transverse reinforcement within the beam-column joint regions, and large spacing between column transverse reinforcement which results in little confinement of the concrete core. The ranges of some typical parameters of the specimens included in this study are as follow:

- Flexural Reinforcement ratio of column (%)	:	0.71 to 5.35
- Shear Reinforcement ratio of column (%)	:	0.068 to 1.92
- Ratio of beam clear span/column height	:	0.40 to 1.90
- Frame concrete compressive strength (kgf/cm <sup>2</sup> )	:	183.0 to 548.2
- Column axial stress (kgf/cm <sup>2</sup> )	:	0.0 to 38.3

As indicated in Chapter 2, many other experimental programs dealing with seismic strengthening of existing RC buildings beside those mentioned above have been performed. Those tests were not utilized in the hysteresis model development in this study because they do not meet the criteria indicated above. However, the results of these tests will provide useful data for validating this and future analytical developments. Brief summaries of the selected experimental programs are given below.

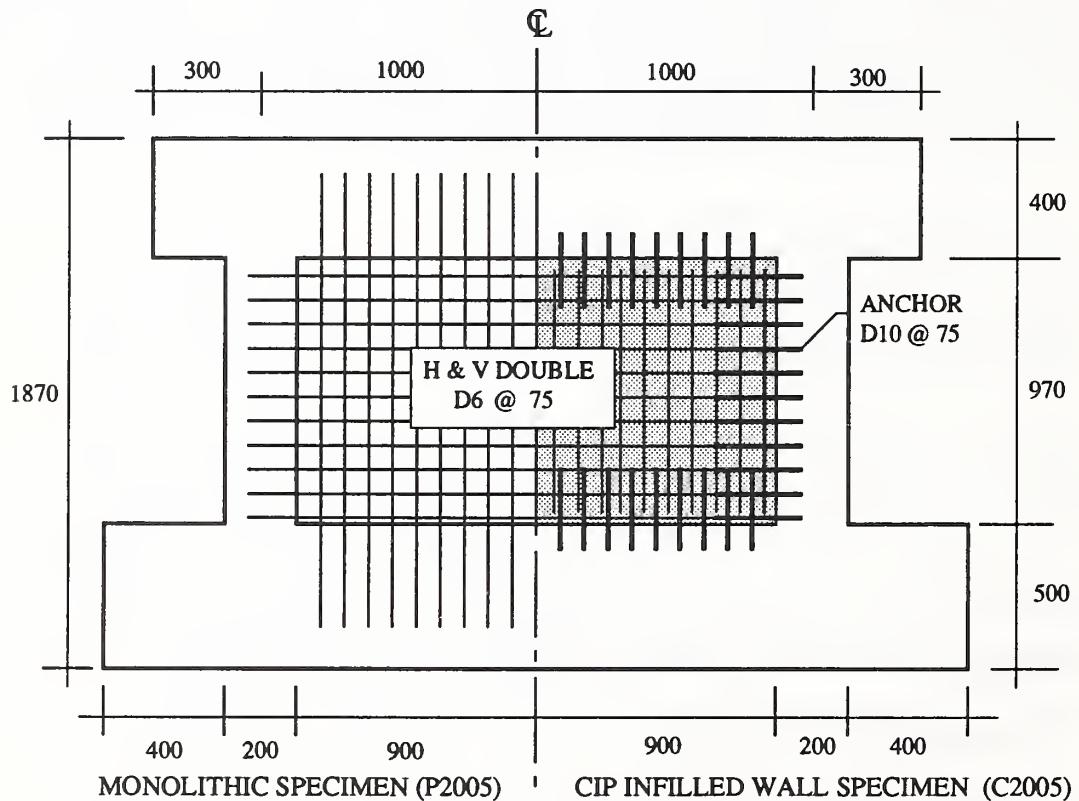
#### 4.1.1 Aoyama et al.<sup>8,9,10,11,12</sup>

A total of fourteen one-third scale specimens were selected from Aoyama's test program for use in this study. These included three monolithic wall-frame constructions and eleven frames strengthened by CIP infilled wall. The specimens had non-ductile columns and were intended to represent buildings designed in accordance with the Japanese building code of the 1960's. The variables studied included column sizes, column

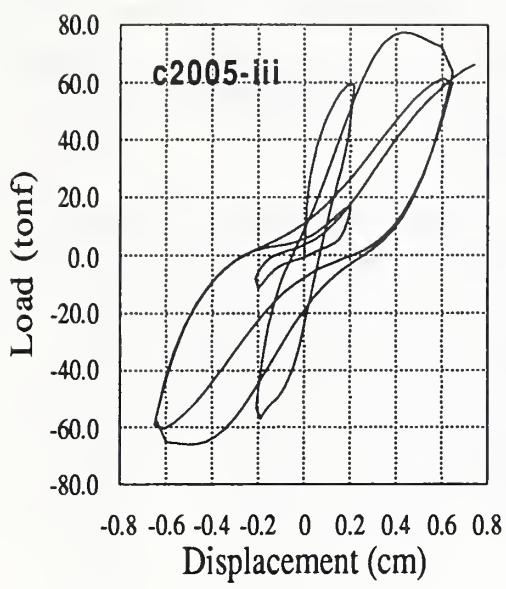
reinforcement ratio, method of anchoring infilled wall to frame (monolithic vs. mechanical wedge anchors vs. epoxy anchors), test variability, and wall opening. Typical parameters and material properties of the selected specimens are listed in Table 4.1. Figure 4.1 shows the geometry, dimensions, and reinforcement pattern of a typical specimen. Figure 4.2 shows the hysteresis behavior, as digitized from published reports<sup>8,9,10,11,12</sup>, of four specimens tested in this test program. Two of the specimens are frames strengthened by CIP infilled walls with epoxy anchors (specimens C2005-III and C2015-A), one is a monolithic wall-frame construction (specimen P2005-A), and one is a frame strengthened by CIP infilled wall with wedge anchors (specimen M2005).

Among the findings of this experimental program are:

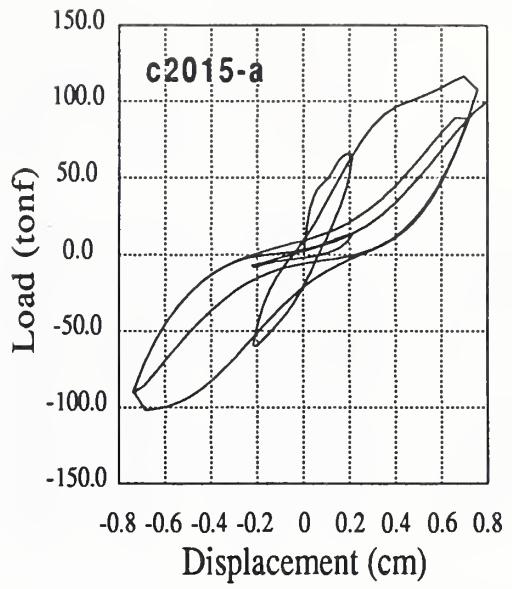
- Ultimate shear strengths of frames strengthened by CIP infilled wall are about 70 - 80 percent of the corresponding monolithic frame-wall constructions.
- Ultimate shear strengths of frames strengthened by infilled walls increase with increasing column stiffness and column flexural reinforcement.



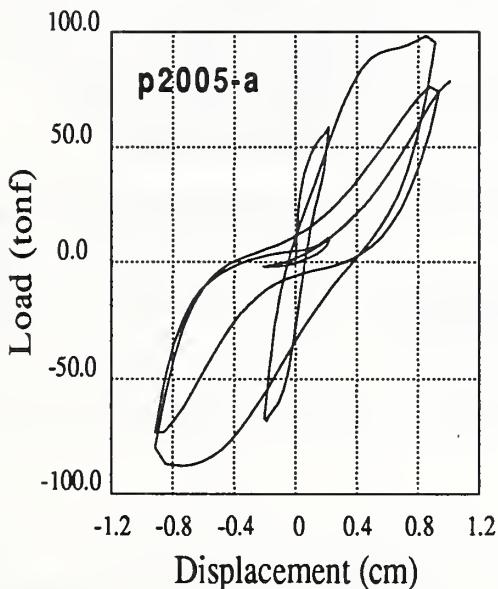
**Figure 4.1 Geometry, Dimensions, and Reinforcement Pattern of Aoyama's Test Specimens**



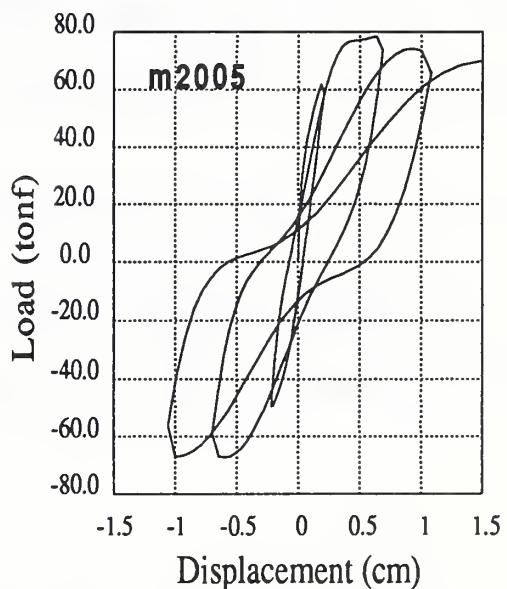
(a)



(b)



(c)



(d)

**Figure 4.2 Hysteresis Behavior of Aoyama's Test Specimens**

- (a) CIP Infilled Frame C2005-III
- (b) CIP Infilled Frame C2015-A
- (c) Monolithic Wall-Frame P2005-A
- (d) CIP Infilled Frame M2005

Table 4.1 SUMMARY OF AOYAMA'S TEST SPECIMENS

	Column bxD (cm)	Concrete $f'_c$ $A_g$ (kgf/cm <sup>2</sup> ) (cm <sup>2</sup> )	Frame	$P_x/A_{cg}$ L <sub>b</sub> /H <sub>c</sub> Wall (kgf/cm <sup>2</sup> )	Construction and Anchor Type	Max. Load (ton)		
C2005-I	20x20	5.08	236.0	205.0	30.0	1.86	CIP Infill/Epoxy	84.2
C2005-II	20x20	5.08	236.0	205.0	30.0	1.86	CIP Infill/Epoxy	81.2
C2005-III	20x20	5.08	226.0	220.0	30.0	1.86	CIP Infill/Epoxy	75.8
C2015-A	20x20	15.2	223.0	150.0	30.0	1.86	CIP Infill/Epoxy	116.2
C2015-B	20x20	15.2	198.0	150.0	30.0	1.86	CIP Infill/Epoxy	112.2
C2015-C	20x20	15.2	403.0	394.0	30.0	1.86	CIP Infill/Epoxy	159.7
P2005	20x20	5.08	220.0	220.0	30.0	1.86	Monolithic	97.8
P2015	20x20	15.2	394.0	394.0	30.0	1.86	Monolithic	171.1
C4015	20x40	15.2	234.0	297.0	15.0	1.65	CIP Infill/Epoxy	126.0
P4015	20x40	15.2	297.0	297.0	15.0	1.65	Monolithic	165.0
M2005	20x20	5.08	301.0	287.0	30.0	1.86	CIP Infill/Wedge	77.0
CH2015	20x20	15.2	289.0	222.0	30.0	1.86	Expansive CIP Infill/Epoxy	122.0
CH2018	20x20	18.1	261.0	222.0	30.0	1.86	Expansive CIP Infill/Epoxy	119.0
OLU2015	20x20	15.2	223.0	181.0	30.0	1.86	Expansive CIP w/opening/Epoxy	78.0

bxD: Column Width x Depth

$A_g$  : Gross Area of Column Flexural Reinforcement

$P_x/A_{cg}$  : Column Axial Stress

$L_b/H_c$  : Ratio of Beam Length vs. Column Height

#### 4.1.2 Kahn<sup>1</sup>

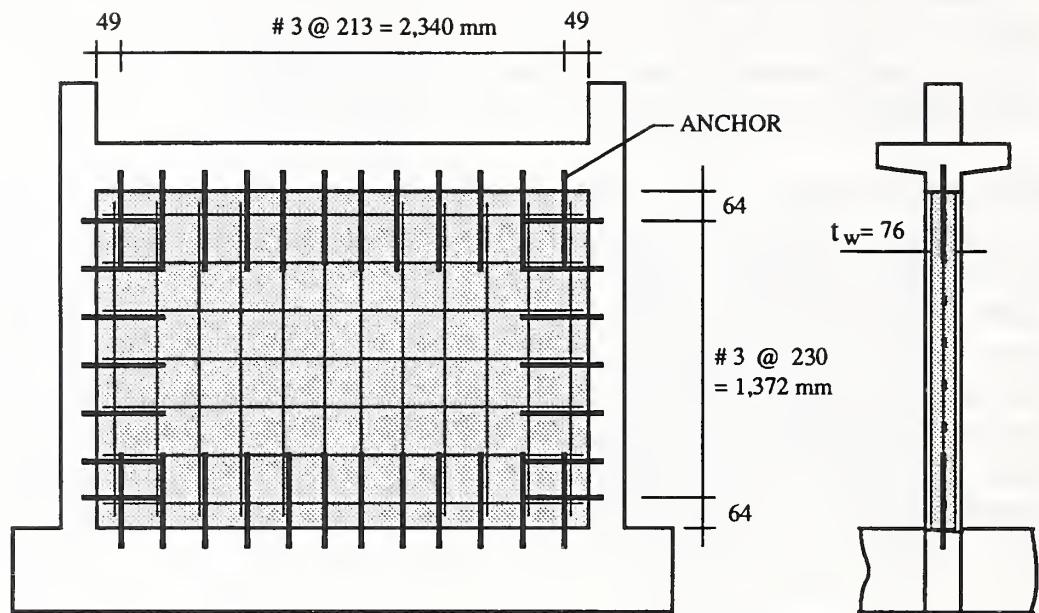
Four half-scale specimens were selected from this test program. The selected specimens consisted of a monolithic frame-wall system (specimen 1), a bare frame (specimen 2), a frame strengthened by CIP infilled wall (specimen 3), and a frame strengthened by multiple precast panel walls (specimen 5). Like those of Aoyama, Kahn's specimens were also designed to represent construction of the 50's and 60's. Three typical characteristics of Kahn's specimens which are representative of past building codes are:

- There is no transverse reinforcement within the beam-column joint region.
- Column ties are widely spaced which provide little confinement to the concrete core.
- Negative and positive beam reinforcement are discontinuous with approximately 150 mm (6 inches) embedment length into the column.

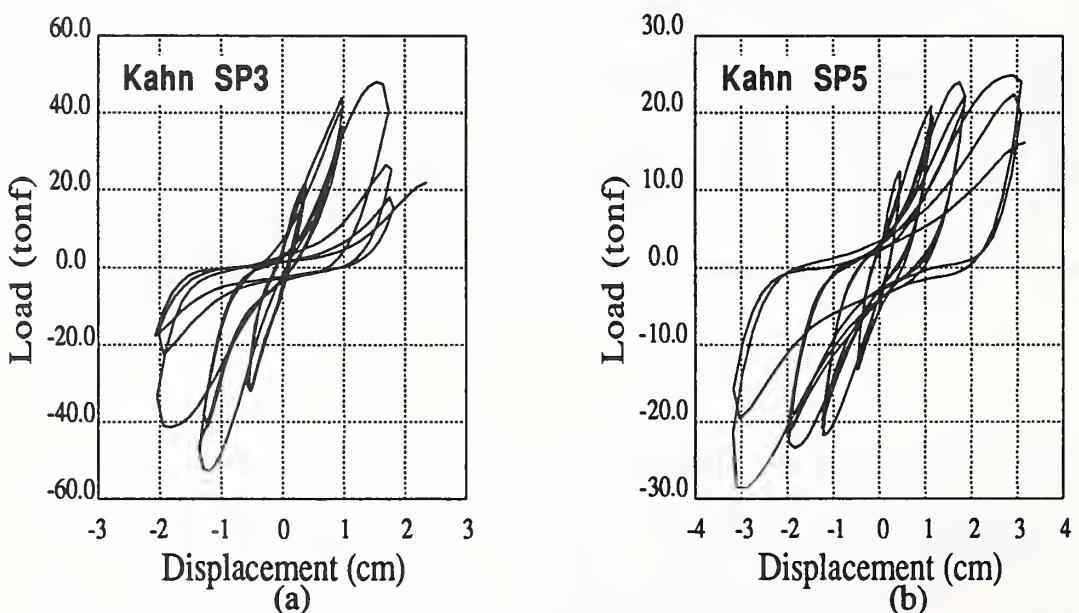
No axial load was applied to the column. The principal variables of this study were the type of construction of the infilled wall (CIP wall vs. precast panel wall) and the frame-to-wall connection. Table 4.2 lists the typical parameters and properties of the selected specimens. Figure 4.3 shows the geometry, dimensions, and reinforcement pattern of a specimen. Figure 4.4 shows the hysteresis behavior of specimens SP3 and SP5, as digitized from the published report<sup>1</sup>, for quasi-static cyclic loading. It was concluded from this study that frames strengthened by CIP infilled wall can achieve almost the same maximum strength as an equivalent monolithic wall-frame system but with less ductility, and that multiple precast infilled walls provide reasonable increase in shear strength and ductility.

Table 4.2 SUMMARY OF KAHN'S TEST SPECIMENS

Specimen	Column bxD (cm)	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	$P_x/A_{cg}$ Frame (kgf/cm <sup>2</sup> )	$L_b/H_c$ Wall (kgf/cm <sup>2</sup> )	Construction and Anchor Type		Max. Load (ton)	
SP1	15x15	8.0	351.0	351.0	0.0	1.63	Monolithic	74.9
SP2	15x15	8.0	317.0	----	0.0	1.63	Bare Frame	4.7
SP3	15x15	8.0	251.6	198.2	0.0	1.63	CIP Infill/Epoxy	56.5
SP5	15x15	8.0	247.4	204.5	0.0	1.63	Multiple Precast Panel/Welded Connectors	30.5



**Figure 4.3 Geometry, Dimensions and Reinforcement Pattern of Kahn's Test Specimen**



**Figure 4.4 Hysteresis Behavior of Kahn's Test Specimens**

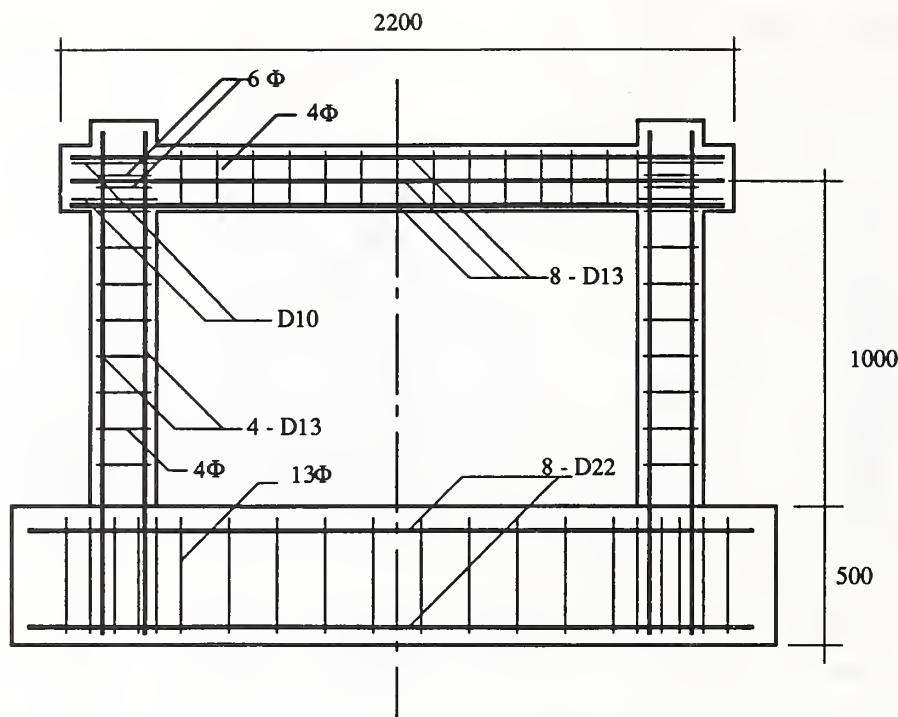
- (a) CIP Infilled Frame SP3
- (b) Frame Infilled by Precast Panels SP5

#### 4.1.3 Hayashi<sup>3</sup>

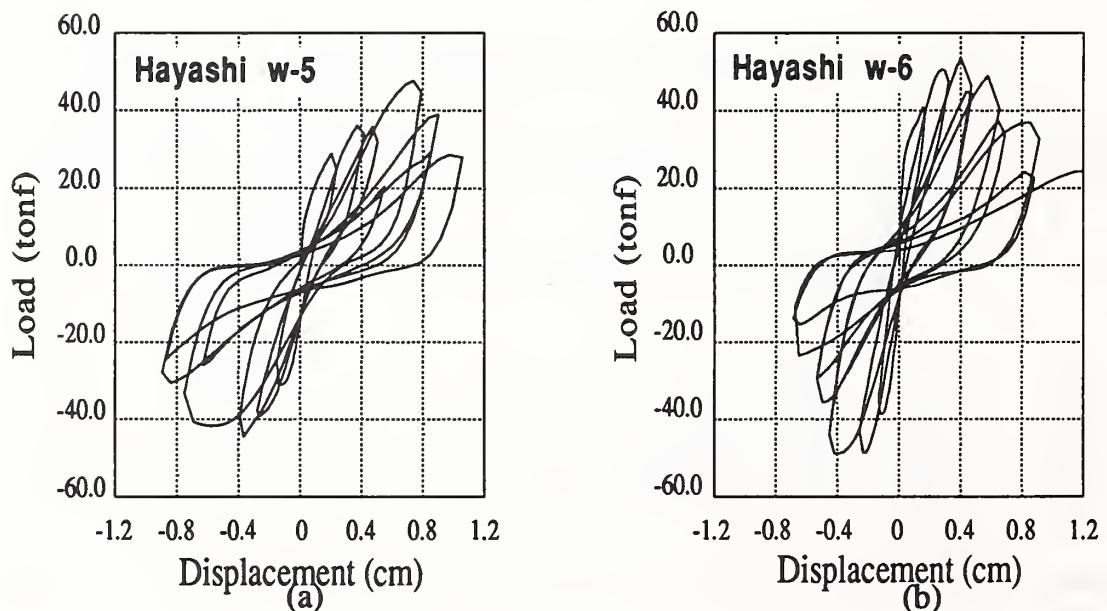
Five specimens, labeled W-1, W-2, W-4, W-5, W-6, were selected from this experimental program. The specimens were one-bay, one-story frames which were designed in accordance with the 1950 and 60's Japanese building code provisions. Specimen W-1 was a bare frame. Specimen W-2 was a monolithic wall-frame. Specimens W-4 to 6 were frames infilled with a reinforced concrete wall. The differences between specimens W-4, 5, and 6 were in the methods of connecting CIP infilled walls to the frames. In specimen W-4, mechanical wedge anchors were used only at the bottom of the upper beam of the frame, and the remaining inner sides of the frame were roughened. In specimen W-5, wedge anchors were used on all four sides of the frame. In specimen W-6, wedge anchors were used on all inner sides of the frame, and roughening was done for all inner sides except for the top beam. There was a specimen W-3 which was also an infilled wall. However, this specimen was not used here since the method of connecting the infilled wall to the frame was by means of concrete shear keys, which is considered nonconventional and not compatible with other tests. Table 4.3 shows typical parameters and properties of these specimens. Figure 4.5 shows specimen's geometry, dimensions, and reinforcement pattern. Figure 4.6 shows the hysteresis curves of specimens W-5 and W-6 under quasi-static cyclic loading. This study concluded that an increase in lateral load capacity, by a factor of 3.5 to 5.0 times, can be achieved by strengthening a bare frame with infilled wall, and a frame strengthened by infilled wall may achieve a lateral strength of 55 to 75 percent of that for a corresponding monolithic wall-frame.

Table 4.3 SUMMARY OF HAYASHI'S TEST SPECIMENS

Specimen	Column bxD (cm)	Concrete $f_c$ (kgf/cm <sup>2</sup> )	$P_x/A_{cg}$ Frame (kgf/cm <sup>2</sup> )	$L_b/H_c$ Wall (kgf/cm <sup>2</sup> )	Construction and Anchor Type	Max. Load (ton)
W-1	20x20	5.07	183.0	----	Bare Frame	11.2
W-2	20x20	5.07	183.0	183.0	Monolithic	77.5
W-4	20x20	5.07	183.0	272.0	CIP Infill/Wedge	55.0
W-5	20x20	5.07	185.0	306.0	CIP Infill/Wedge	48.0
W-6	20x20	5.07	185.0	306.0	CIP Infill/Wedge	55.0



**Figure 4.5 Geometry, Dimensions, and Reinforcement Patterns of Hayashi's Test Specimen**



**Figure 4.6 Hysteresis Behavior of Hayashi's Test Specimens**  
 (a) CIP Infilled Frame W-5  
 (b) CIP Infilled Frame W-6

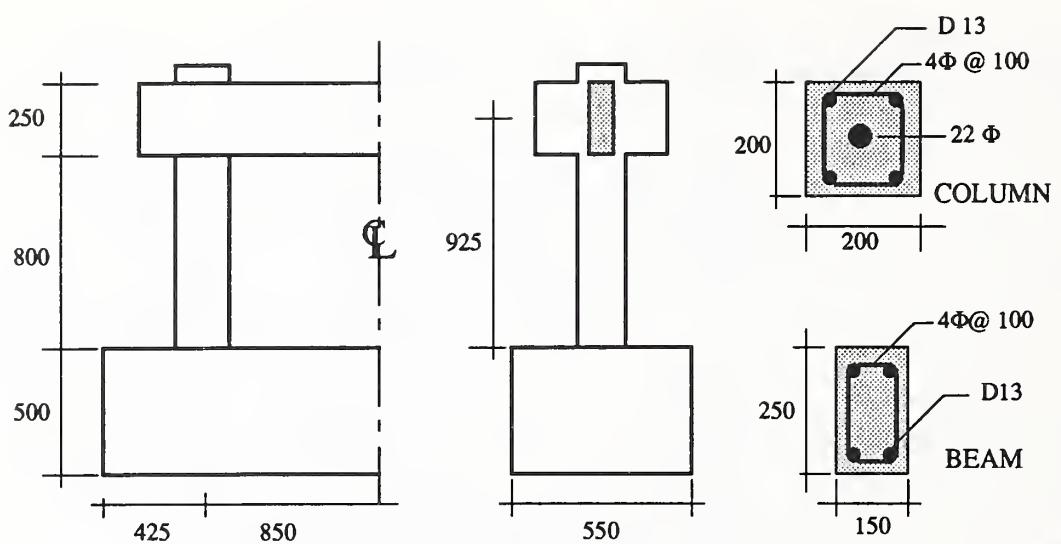
#### 4.1.4 Sugano et al<sup>2</sup>

Seven one-bay one-story specimens were selected from this study. Specimen F was a bare frame. Specimens W-80S and W-40S were monolithic wall-frames with wall thicknesses of 8.0 cm and 4.0 cm, respectively. Specimen W-40W was also a monolithic wall-frame similar to specimen W-40S except that the wall was thickened by new layers of concrete to 8 cm thick. Specimen W-HA was a frame strengthened by 8-cm thick CIP infilled wall. The infilled wall was connected to the frame using wedge anchors. Specimen W-BL was a frame strengthened by precast concrete block wall. Specimen W-CO was a frame strengthened by 8-cm thick CIP infilled wall, but with mortar shear keys as connectors. Other specimens, W-S, B-C, and B-T, which were frames strengthened by a steel panel, a compression steel brace, and a tension steel brace, were not selected for use in this study. The variables studied included thicknesses of infilled wall, methods of wall-frame connection, and wall types. The study concluded that infilled wall may produce a lateral strength increase of at least 3.5 times that of a bare frame, and an infilled frame may achieve at least 60 percent of the lateral strength of a corresponding monolithic wall-frame system. Table 4.4 lists typical parameters and material properties of the selected specimens in Sugano's test program. Figure 4.7 shows geometry, dimension, and reinforcement pattern of a typical specimen. Figure 4.8 show the hysteresis behavior observed when the CIP infilled frame specimen W-HA and the monolithic wall-frame specimen W-40W were subjected to quasi-static cyclic loading.

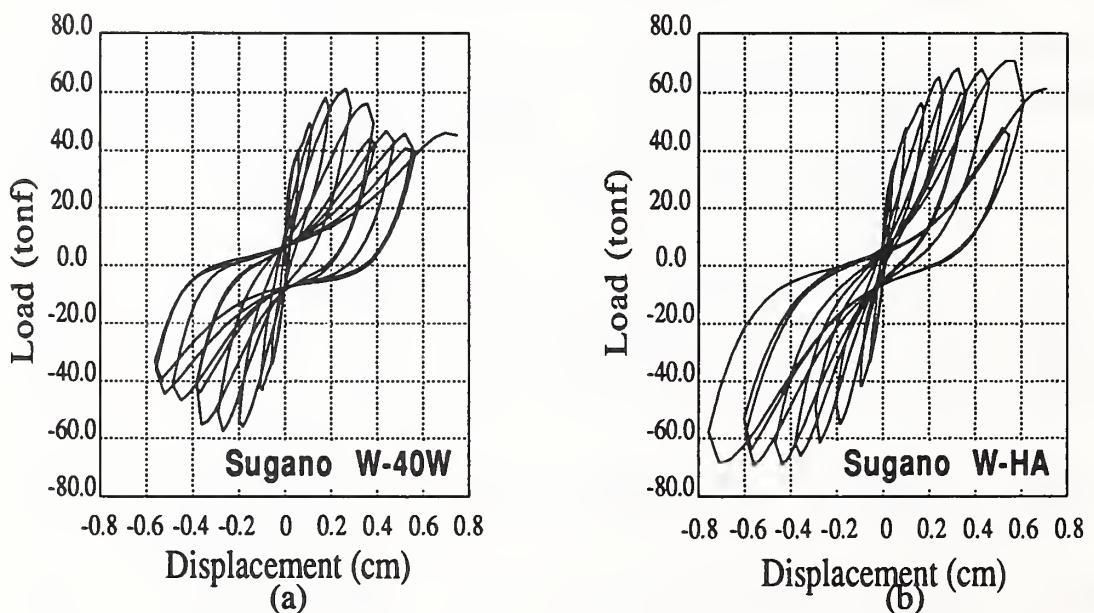
Table 4.4 SUMMARY OF SUGANO'S TEST SPECIMENS

Specimen	Column bxD (cm)	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	P <sub>x</sub> /A <sub>cg</sub> (kgf/cm <sup>2</sup> )	L <sub>b</sub> /H <sub>c</sub> Ratio	Construction and Anchor Type	Max. Load (ton)
	A <sub>g</sub> (cm <sup>2</sup> )	Frame	Wall			
F	20x20	5.16	240.0*	----	31.2	1.88 Bare Frame
W-80S	20x20	5.16	240.0*	380.0*	31.2	1.88 Monolithic
W-40S	20x20	5.16	240.0*	380.0*	31.2	1.88 Monolithic
W-40W	20x20	5.16	240.0*	380.0*	31.2	1.88 Monolithic w/thickened wall
W-HA	20x20	5.16	240.0*	380.0*	31.2	1.88 CIP Infill/Wedge
W-BL	20x20	5.16	240.0*	300.0*	31.2	1.88 Precast block Infill
W-CO	20x20	5.16	240.0*	380.0*	31.2	1.88 CIP Infill/ Mortar shear keys

\* Design Compressive Strength



**Figure 4.7 Geometry, Dimensions, and Reinforcement Patterns of Sugano's Test Specimen**



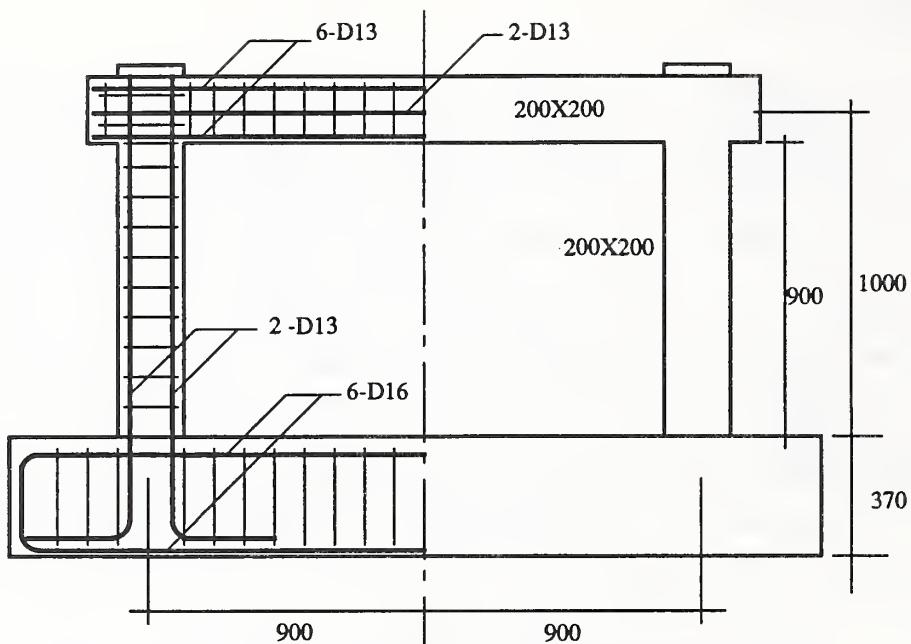
**Figure 4.8 Hysteresis Behavior of Sugano's Test Specimens**  
 (a) Monolithic Wall-Frame Construction W-40W  
 (b) CIP Infilled Frame W-HA

#### 4.1.5 Higashi et al<sup>4</sup>

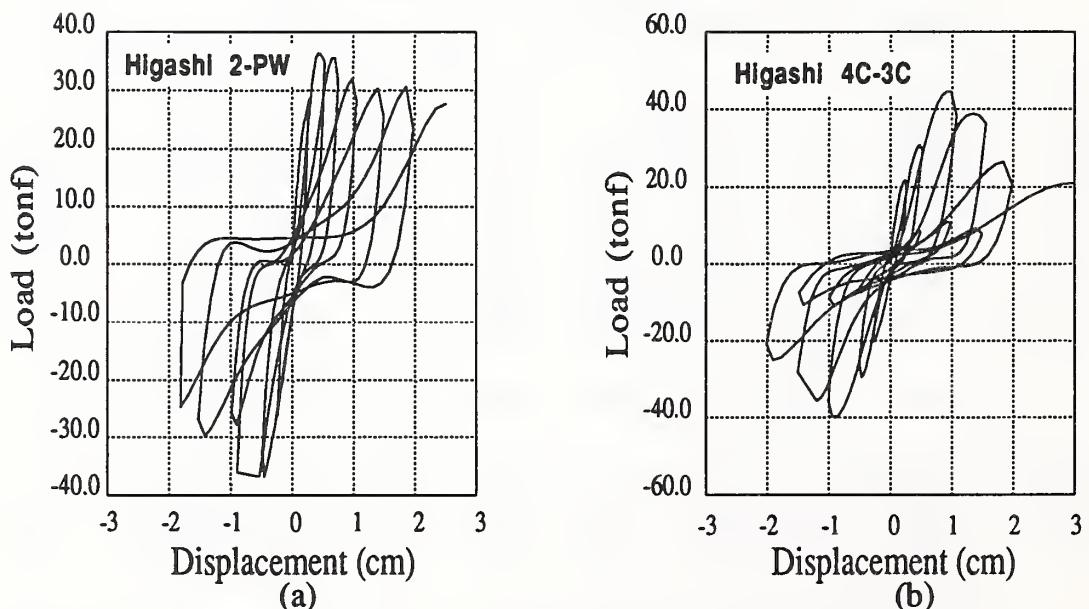
Ten one-third scale, one-bay, one-story frames with low column shear reinforcement ratio were selected from Higashi's test program. The selected specimens included two bare frames (specimens 1-F1 and 5-F2), one monolithic wall-frame system (13-FW), one frame strengthened by CIP infilled wall (2-PW), and six frames strengthened by multiple precast concrete wall panels. The differences in these multiple precast panel infilled walls were in the methods of connecting the walls to the frames and the existence of wall openings. A uniform axial stress of 30 kgf/cm<sup>2</sup> was applied to each column, and the frames were tested under quasi-static cyclic lateral load. This experimental program's main objective was to study the effectiveness of using multiple precast panels for strengthening lightly reinforced concrete frames. Table 4.5 lists the typical parameters and properties of the selected specimens. Figure 4.9 shows the geometry, dimensions, and reinforcement pattern of a typical specimen. Figure 4.10 shows the hysteresis behavior of the CIP infilled specimen 2-PW and the multiple precast panels infilled specimen 4-C3C due to quasi-static cyclic loading.

Table 4.5 SUMMARY OF HIGASHI'S TEST SPECIMENS

Specimen	Column bxD (cm)	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	Frame $A_g$ (cm <sup>2</sup> )	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	$P_x/A_{cg}$ (kgf/cm <sup>2</sup> )	$L_b/H_c$	Construction and Anchor Type	Max. Load (ton)
1-F1	20x20	5.16	176.0	----	30.0	1.78	Bare Frame	10.7
2-PW	20x20	5.16	176.0	219.0	30.0	1.78	CIP Infill/Wedge	40.0
5-F2	20x20	5.16	210.0	----	30.0	1.78	Bare Frame	11.1
13-FW	20x20	5.16	210.0	210.0	30.0	1.78	Monolithic	58.0
4-C3C	20x20	5.16	176.0	242.0	30.0	1.78	Precast Panels	46.0
6-C2A	20x20	5.16	210.0	228.0	30.0	1.78	Precast Panels w/Center Opening	15.7
7-C2B	20x20	5.16	210.0	228.0	30.0	1.78	Precast Panels w/Side Opening	14.5
9-C40	20x20	5.16	210.0	228.0	30.0	1.78	Precast Panels	16.0
3-C3	20x20	5.16	176.0	242.0	30.0	1.78	Precast Panels	33.0
8-C4	20x20	5.16	210.0	228.0	30.0	1.78	Precast Panels	40.0



**Figure 4.9 Geometry, Dimensions, and Reinforcement Patterns of Higashi's Test Specimen**



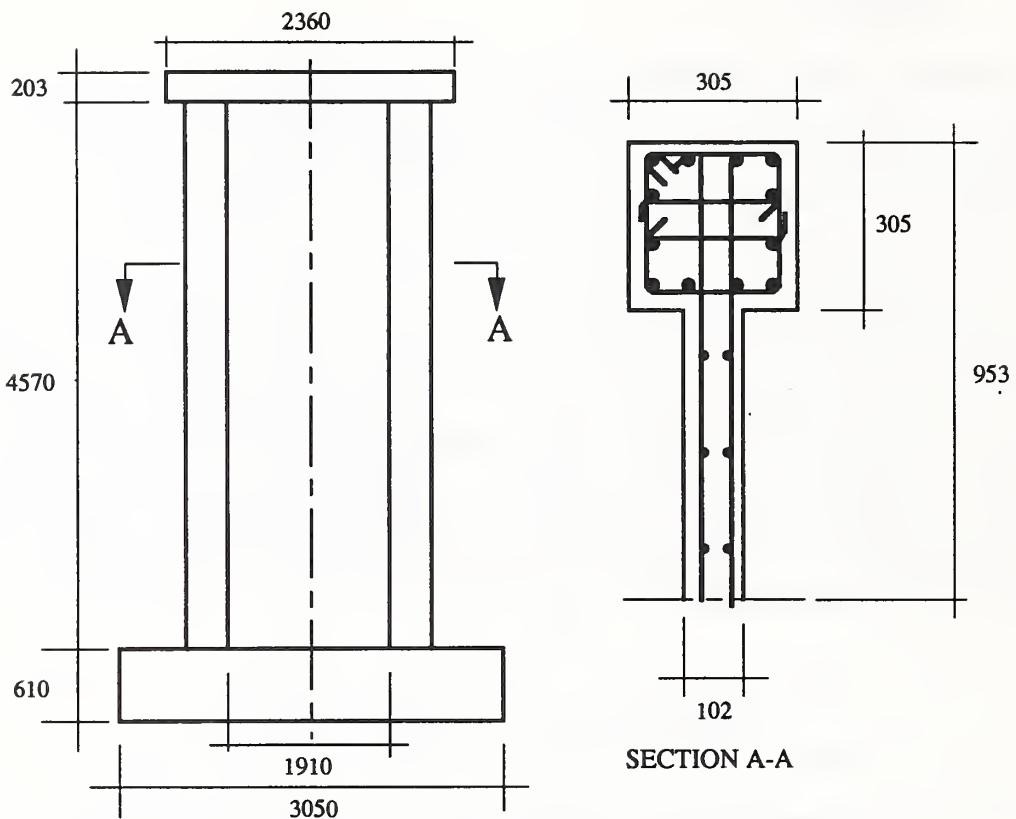
**Figure 4.10 Hysteresis Behavior of Higashi's Test Specimens**  
 (a) CIP Infilled Frame 2-PW  
 (b) Multiple Precast Panel Infilled Frame 4-C3C

#### 4.1.6 Corley<sup>5,6,7</sup>

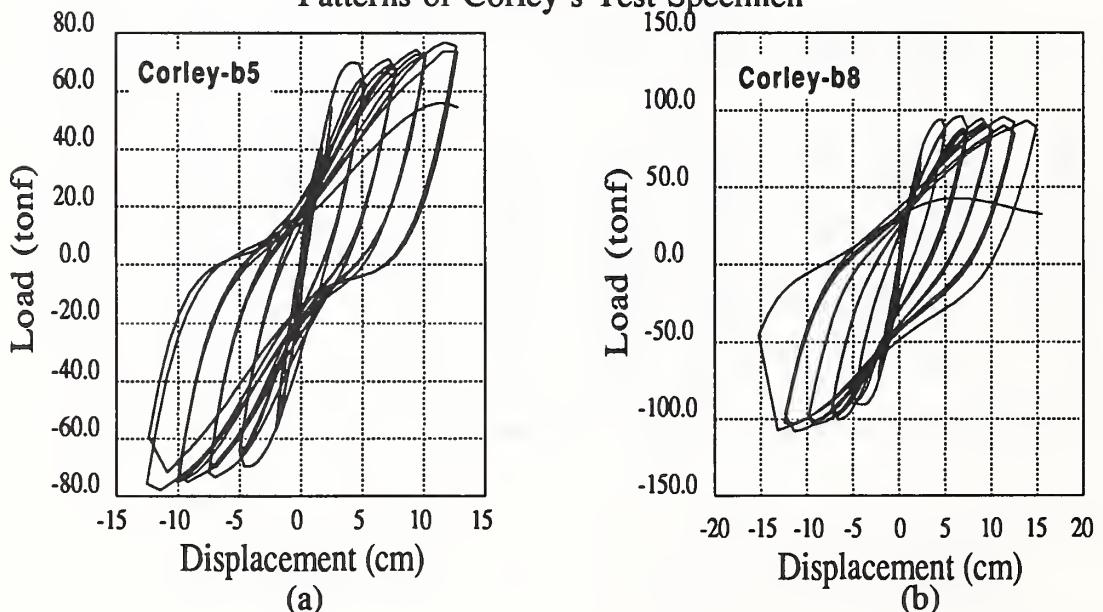
Six monolithic Wall-Frame constructions, which represented high-rise structural walls ( $L_b/H_c < 1$ ), were selected from the test program conducted by Corley et al. The specimens, named B5 to B9 and B11, were subjected to constant axial load in the column in combination with laterally-applied, quasi-static cyclic loading. Most of the specimens listed above were tested to complete failure and then repaired and retested. However, the results of the repaired specimens were not selected for this study since the focus here is on strengthening of existing, undamaged structures. The variables studied included the influence of axial load on the behavior of the walls, amount of column's flexural and shear reinforcement, and the effectiveness of the repair techniques employed in the test program. Table 4.6 lists some typical parameters and properties of the selected specimens. Figure 4.11 shows the geometry, dimensions, and reinforcement pattern of a typical specimen. Figure 4.12 shows the hysteresis behavior, as digitized from the published reports<sup>5,6,7</sup>, of a specimen without axial load (B5) and a specimen with axial load (B8) due to quasi-static cyclic lateral load.

Table 4.6 SUMMARY OF CORLEY'S SPECIMENS

Specimen	Column bxD (cm)	Concrete $f'_c$ $A_g$ ( $\text{kgf}/\text{cm}^2$ ) ( $\text{cm}^2$ )	Frame	Concrete $f'_c$ $P_x/A_{cg}$ ( $\text{kgf}/\text{cm}^2$ )	Wall	$L_b/H_c$	Construction Ratio	Construction and Anchor Type	Max. Load (ton)
B5	31x31	34.1	461.8	461.8	0.0	0.43	Monolithic	77.7	
B6	31x31	34.1	222.4	222.4	29.9	0.43	Monolithic	86.7	
B7	31x31	34.1	502.9	502.9	38.3	0.43	Monolithic	103.8	
B8	31x31	34.1	427.7	427.7	38.3	0.43	Monolithic	108.0	
B9	31x31	34.1	449.5	449.5	38.3	0.43	Monolithic	99.6	
B11	31x31	34.1	548.2	548.2	0.0	0.43	Monolithic	74.1	



**Figure 4.11 Geometry, Dimensions, and Reinforcement Patterns of Corley's Test Specimen**



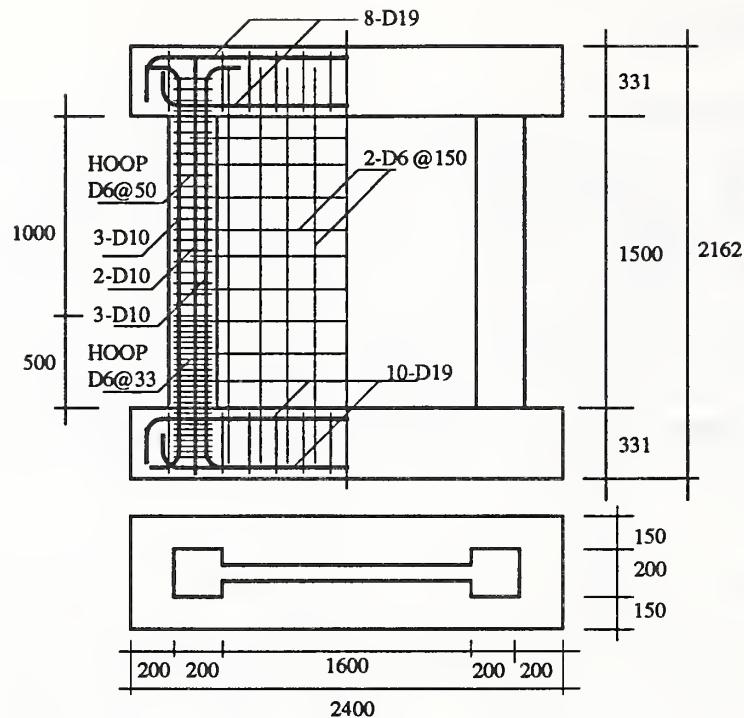
**Figure 4.12 Hysteresis Behaviors of Corley's Test Specimens**  
**(a) Monolithic Wall-Frame Specimen B5**  
**(b) Monolithic Wall-Frame Specimen B8**

#### 4.1.7 Ogata et al<sup>13</sup>

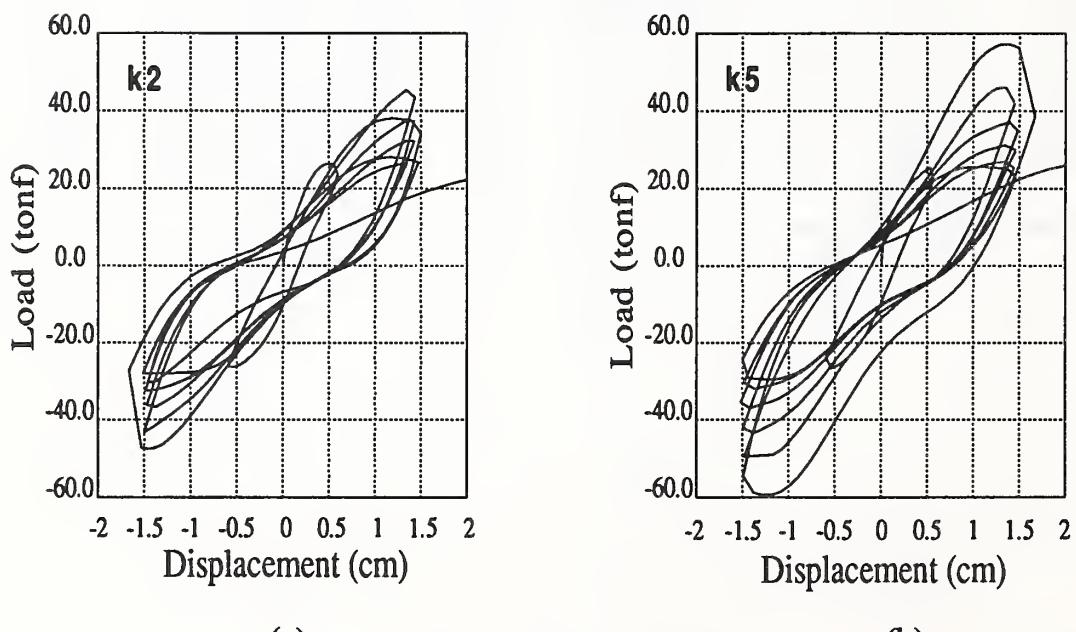
All six monolithic wall-frame systems representing first-story, low-rise shear walls ( $L_b/H_c \geq 1$ ) tested by Ogata et al. were included in this study. The specimens were designated K1 to K6. All six specimens have identical geometric dimensions. The variables investigated by Ogata et al. included the applied moment-to-shear ratios in the walls, the amount of flexural reinforcement in the columns and the walls, and the shear reinforcement in the columns. An axial load of 7.7 tons was applied to each column in combination with the quasi-static cyclic lateral load. Table 4.7 lists typical parameters of Ogata's specimens. Figure 4.13 shows the geometry, dimensions , and reinforcement pattern of the specimens. Figure 4.14 shows the hysteresis behavior of two typical specimens, K2 and K5, as digitized from the published report<sup>13</sup>.

Table 4.7 SUMMARY OF OGATA'S TEST SPECIMENS

Specimen	Column bxD (cm)	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	Frame $A_g$ (cm <sup>2</sup> )	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	$P_x/A_{cg}$ (kgf/cm <sup>2</sup> )	$L_b/H_c$	Construction and Anchor Type	Max. Load (ton)
K1	20x20	2.8	196.0	196.0	19.2	1.07	Monolithic	45.0
K2	20x20	5.7	196.0	196.0	19.2	1.07	Monolithic	49.0
K3	20x20	8.6	196.0	196.0	19.2	1.07	Monolithic	55.2
K4	20x20	5.7	212.0	212.0	19.2	1.07	Monolithic	52.0
K5	20x20	5.7	212.0	212.0	19.2	1.07	Monolithic	59.9
K6	20x20	8.6	212.0	212.0	19.2	1.07	Monolithic	74.3



**Figure 4.13** Geometry, Dimensions, and Reinforcement Patterns of Ogata's Test Specimen



**Figure 4.14** Hysteresis Behavior of Ogata's Test Specimens  
 (a) Monolithic Wall-Frame Specimen K2  
 (b) Monolithic Wall-Frame Specimen K5

#### 4.1.8 Gaynor<sup>18</sup>

Three two-third scale, one-bay, one-story frames infilled by solid shotcrete wall, shotcrete wall with a window opening, and shotcrete wall with a door opening, were tested by Gaynor<sup>18</sup>. The specimens were designed to be representative of non-ductile reinforced concrete frames of the 1950's (widely spaced column ties inadequate for the confinement of concrete core, compression splice at column base inadequate for developing tensile yield in the bars). The specimens were subjected to quasi-static cyclic loading. Typical parameters of the specimens in this test program are listed in Table 4.8. Figure 4.15 shows the geometry of the specimens tested in this program. The hysteresis behavior of two specimens, specimen W with window opening and specimen D with door opening, are shown in Figure 4.16.

Table 4.8 SUMMARY OF GAYNOR'S TEST SPECIMENS

Specimen	Column bxD (cm)	Concrete $f'_c$ (kgf/cm <sup>2</sup> )	$P_x/A_{cg}$ Frame Wall (kgf/cm <sup>2</sup> )	$L_b/H_c$	Construction and Anchor Type	Max. Load (ton)		
F	31x31	20.6	292.0	238.0	0.0	1.76	Shotcrete Infill	118.3
W	31x31	20.6	392.0	218.0	0.0	1.76	Shotcrete Infill w/Window Opening	85.9
D	31x31	20.6	337.0	230.0	0.0	1.76	Shotcrete Infill w/Door Opening	98.5

#### 4.1.9 Shah<sup>16</sup>

One of the specimens tested by Gaynor did not suffer major damage to the bounding frame. The specimen's shotcrete infilled wall was removed and the frame was restrengthened by a CIP infilled wall with a door opening and tested by Shah<sup>16</sup>. Typical parameters of this specimen, which was included in this study, are listed in Table 4.9. The hysteresis behavior of the tested specimen is shown in Figure 4.17.

Table 4.9 SUMMARY OF SHAH'S TEST SPECIMEN

Specimen	Column bxD (cm)	Concrete $f_c$ (kgf/cm <sup>2</sup> )	$P_x/A_{cg}$ Frame (kgf/cm <sup>2</sup> )	$L_b/H_c$ Wall (kgf/cm <sup>2</sup> )	Construction and Anchor Type	Max. Load (ton)		
SP1	31x31	20.6	329.3	275.6	0.0	1.76	Cast-In-Place Infill w/door	132.6

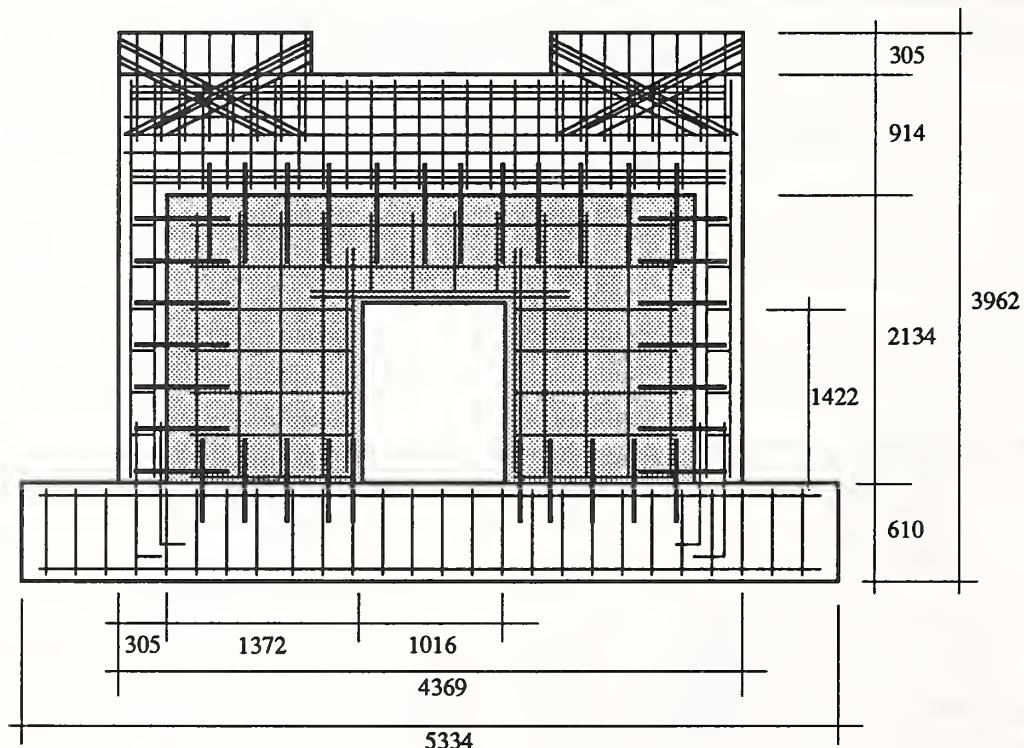
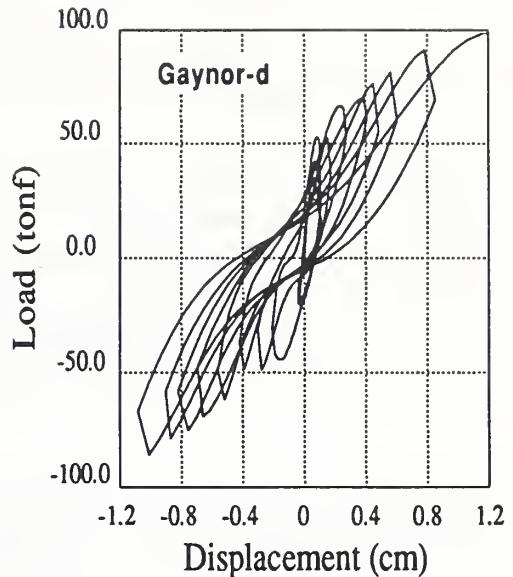
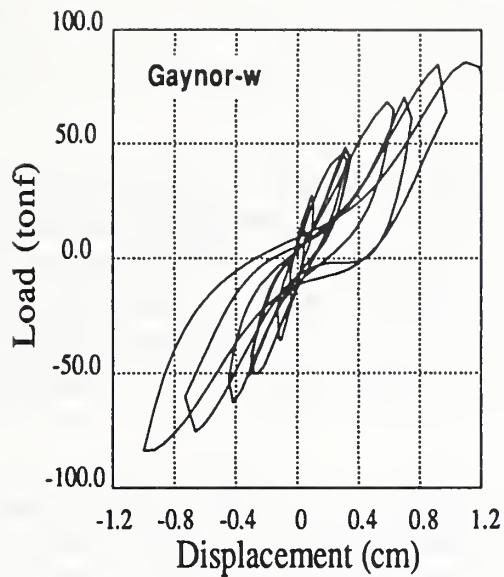


Figure 4.15 Geometry, Dimensions, and Reinforcement Patterns of Gaynor and Shah's Test Specimen

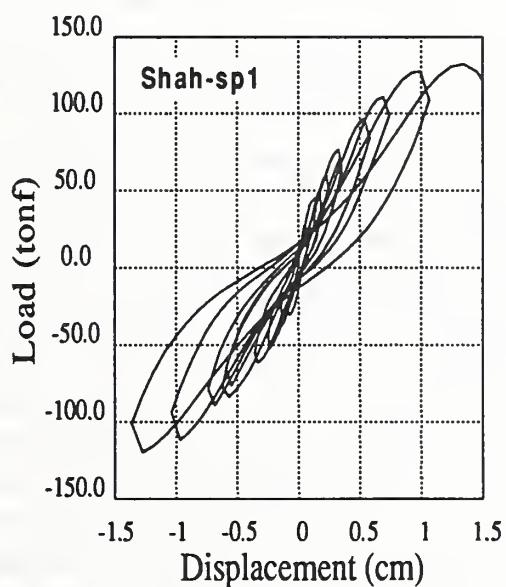


(a)

(b)

**Figure 4.16 Hystereses Behavior of Gaynor's Test Specimens**

- (a) Shotcrete Infilled Frame with Window Opening W
- (b) Shotcrete Infilled Frame with Door Opening D



**Figure 4.17 Hysteresis Behavior of Shah's Specimen SP1**

## 4.2 Development of Three-Parameter Hysteresis Models

The procedure used for the development of the empirical three-parameter hysteresis models in this study involved the following two main tasks:

1. Determine the values for three parameters  $\alpha$ ,  $\beta$ , and  $\gamma$  which best fit the experimental hysteresis loop of each of the fifty five tests selected in section 4.1. The method used for this process is referred to as the System Identification method (see Yeh<sup>38</sup>, 1988 and Kunnath and Reinhorn<sup>37</sup>, 1989). The corresponding fifty five sets of  $\alpha$ ,  $\beta$ ,  $\gamma$ , so determined are from here on referred to as the estimated parameters  $\alpha$ ,  $\beta$ ,  $\gamma$ . This task is further described in section 4.2.1 of this report.
2. Based on the fifty five sets of estimated parameters  $\alpha$ ,  $\beta$ , and  $\gamma$ , perform multiple-variable regression to obtain empirical expressions for  $\alpha$ ,  $\beta$ , and  $\gamma$  in terms of the physical properties of the selected test specimens. These empirical expressions, referred to in this study as the hysteresis models, are then used to predict the three parameters for the analysis of bare frames, infilled frames, and monolithic wall-frame constructions. This task is explained in detail in section 4.2.2.

### 4.2.1 System Identification of Hysteresis Parameters

The concept of identifying or estimating hysteresis parameters of concrete structures subjected to cyclic loading using actual test results has been tried by many researchers. The purpose is to derive a set of parameters which may be used to simulate as closely as possible the hysteresis behavior observed from experiment. Earlier research included the work by Yeh<sup>38</sup> (1988) at SUNY/Buffalo which utilized nonlinear search algorithms and optimization techniques to obtain the best possible set of hysteresis parameters based on the actual test results. Later modification of the optimization techniques used by Yeh<sup>38</sup> (1988) were performed at NIST by Stone and Taylor<sup>40</sup> (1992). The result is a graphics-based system identification package, called NIDENT 3.0. Principally, the system identification procedure employed in NIDENT 3.0 performs a three dimensional trial and error search for a set of initial values of  $\alpha$ ,  $\beta$ ,  $\gamma$  such that the cumulative error between the predicted and experimentally observed hysteretic energy is minimized. NIDENT 3.0 displays the hysteresis response corresponding to the initial parameters together with the experimentally-observed response. The users are then allowed to interactively adjust the values of  $\alpha$ ,  $\beta$ , and  $\gamma$  while continuously monitoring the fit between the predicted and the experimentally-observed responses in real time until a satisfactory match between the responses is observed. At any time during the fitting process, a check of cumulative error, in terms of the absorbed hysteretic energy, between the latest prediction and the experimentally-observed response can be performed. Generally, a reasonable visual match of the hysteretic responses and an absorbed energy cumulative error of within a few percent is considered satisfactory. The values of  $\alpha$ ,  $\beta$ , and  $\gamma$  so determined

constitute the identified hysteresis parameters of the corresponding experiment. A more detailed discussion concerning NIDENT 3.0 is given in reference <sup>40</sup>.

The above system identification procedure was used to identify hysteresis parameters of the fifty-five test results selected for this study and described in section 4.1. In most cases, the cumulative errors between the predicted and measured total absorbed hysteretic energy were less than 3 percent. Table 4.10 lists the estimated hysteresis parameters and cumulative absorbed hysteresis energy error for each of the selected specimens. A negative difference in cumulative absorbed energy, as listed for a few cases in Table 4.10, simply means that the total cumulative absorbed energy predicted by system identification exceeds that obtained from experiment. Examples of the match between the predicted and measured hysteresis responses of four specimens, Aoyama's specimen C2005-III, Ogata's specimen K3, Higashi's specimen 5-F2, and Gaynor's specimen W, are shown in Figures 4.18 a to h. In these Figures (4.18 a, c, e, g), the dashed lines represent the experimental results and the solid lines are the predicted hysteresis responses corresponding to the estimated hysteresis parameters  $\alpha$ ,  $\beta$ ,  $\gamma$  obtained from system identification. Also plotted in Figures 4.18 (b, d, f, h) are histograms of the measured and predicted absorbed energy for the four specimens. As can be seen from Figures 4.18, the three parameters  $\alpha$ ,  $\beta$ ,  $\gamma$ , identified for each test specimen were able to predict reasonably well the load-deformation hysteresis behavior of the test specimens. They also predict the absorbed energy of the specimen on a per cycle basis. A complete set of comparative plots for each of the fifty-five specimens, superposing the best-fit curve generated with NIDENT on the experimental load-displacement curve, are reproduced in Appendix B.

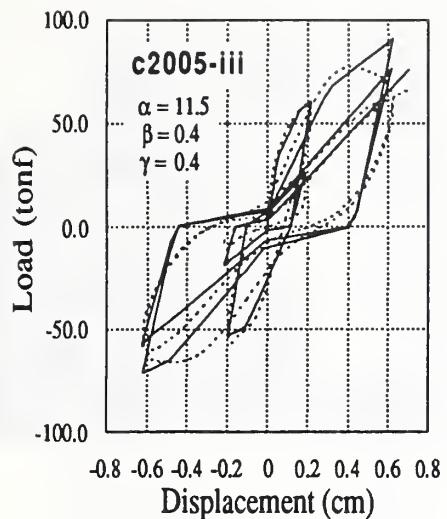
#### 4.2.2 Empirical Expressions for Hysteresis Parameters

Empirical expressions for the hysteresis parameters were formulated by correlating the estimated hysteresis parameters,  $\alpha_{exp}$ ,  $\beta_{exp}$ , and  $\gamma_{exp}$ , identified from the fifty five tests, with a set of variables relating to the geometric and material properties, dimensions, and reinforcement patterns of the specimens. These variables were selected to include all possible factors which were judged to have an influence on the hysteresis behavior of the lightly reinforced concrete frames. The variables are defined and listed in Appendix A. The numerical values corresponding to each of these variables for each of the fifty five test specimens are given in Appendix B. The correlation was performed using the linear regression procedure of a commercially available statistical analysis software package. There are several model-selection methods which can be selected for the regression analysis. The method which maximizes the  $R^2$  values, was chosen for this study.  $R^2$  is an indicator of how much variation in the data is explained by the empirical expressions obtained by the regression analysis and is defined as:

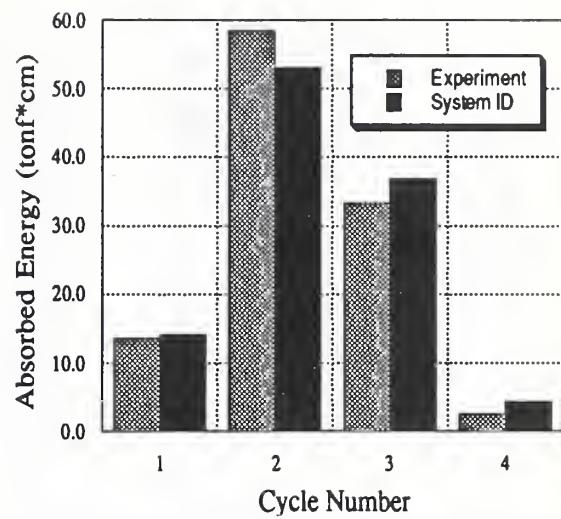
$$R^2 = 1 - (SSE/TSS)$$

where SSE is the Sum of Square for Errors, and TSS is the Corrected Total Sum of Squares. As the Sum of Square for Errors approaches zero,  $R^2$  values approach one, indicating increasingly accurate models.

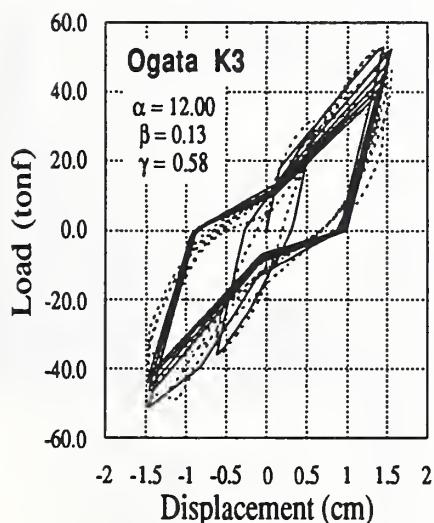
Four sets of empirical expressions for  $\alpha$ ,  $\beta$ , and  $\gamma$ , constituting the hysteresis models for existing frames, frames strengthened by CIP infilled walls, frames strengthened by precast concrete wall panels, and monolithic wall-frame constructions, were derived from the regression analysis. It should be noted that, even though  $\alpha$ ,  $\beta$ ,  $\gamma$  are non-dimensional parameters, the variables which are included in the hysteresis models are listed following specific units (see Appendix B). Therefore, to correctly compute  $\alpha$ ,  $\beta$ ,  $\gamma$ , units which are consistent with those listed in Appendix B must be used. The empirical expressions for each of those cases are given in the following sections.



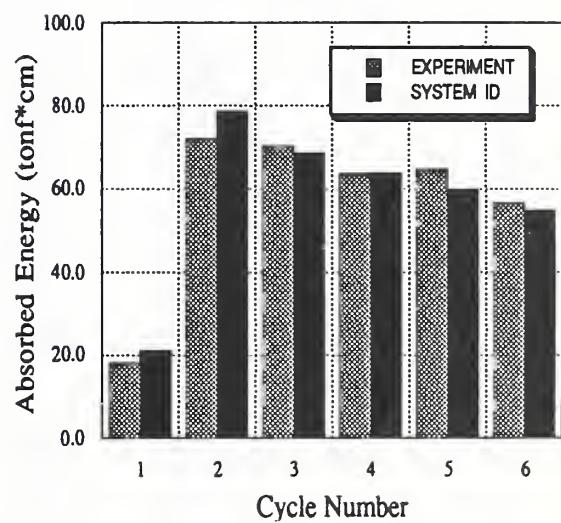
(a)



(b)



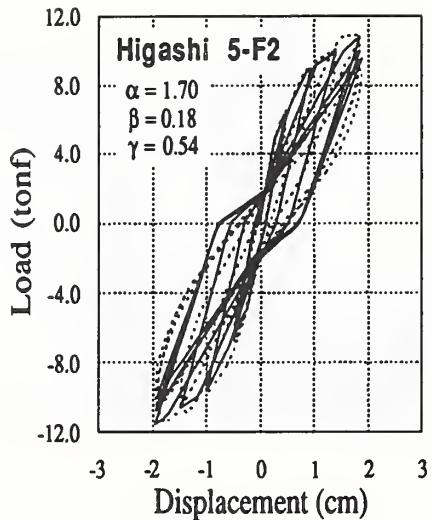
(c)



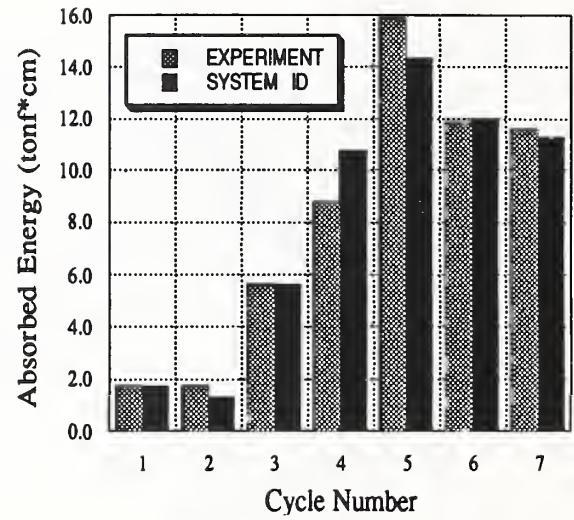
(d)

Figure 4.18 System Identification of Experimental Results

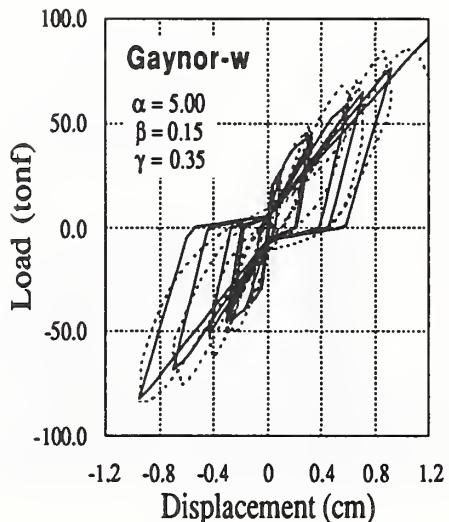
- (a) Load-Deformation Characteristics of Specimen C2005-III
- (b) Absorbed Energy Histograms of Specimen C2005-III
- (c) Load-Deformation Characteristics of Specimen K3
- (d) Absorbed Energy Histograms of Specimen K3



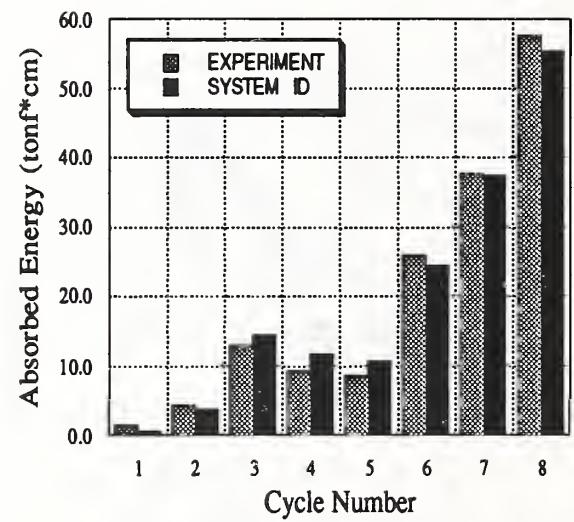
(e)



(f)



(g)



(h)

**Figure 4.18 System Identification of Experimental Results (continued)**

(e) Load-Deformation Characteristics of Specimen 5-F2

(f) Absorbed Energy Histograms of Specimen 5-F2

(g) Load-Deformation Characteristics of Specimen W

(h) Absorbed Energy Histograms of Specimen W

Table 4.10 ESTIMATED HYSTERESIS PARAMETERS  
FROM SYSTEM IDENTIFICATION

TEST NAME	$\alpha$	$\beta$	$\gamma$	ENERGY DIFFERENCE (%)
AOYAMA C2005-I	11.00	0.35	0.25	-0.50
AOYAMA C2005-II	9.00	0.25	0.31	0.40
AOYAMA C2005-III	11.50	0.40	0.4	0.40
AOYAMA C2015-A	9.00	0.88	0.5	0.10
AOYAMA C2015-B	7.25	0.70	0.3	0.10
AOYAMA C2015-C	2.50	0.02	0.2	0.20
AOYAMA P2005-A	12.50	0.10	0.3	-0.30
AOYAMA P2015-A	2.00	0.10	0.3	-0.30
AOYAMA C4015	4.00	0.01	0.32	0.00
AOYAMA P4015	3.50	0.01	0.4	0.70
AOYAMA M2005	12.50	0.45	0.94	0.10
AOYAMA CH2015	7.50	0.34	0.32	0.20
AOYAMA CH2018	12.50	0.96	0.63	-0.30
AOYAMA OLU2015	12.50	0.65	0.5	-0.50
KAHN SP1	13.00	0.20	0.95	-11.80
KAHN SP2	4.00	0.20	0.6	0.60
KAHN SP3	7.50	0.98	0.15	1.10
KAHN SP5	12.50	0.20	0.49	0.10
HAYASHI W1	5.00	0.39	0.8	-0.40
HAYASHI W2	2.50	0.11	0.49	0.20
HAYASHI W4	11.50	0.44	0.75	0.00
HAYASHI W5	12.50	0.49	0.35	-0.30
HAYASHI W6	12.50	0.75	0.5	0.40
SUGANO-WHA	4.50	0.15	0.16	0.00
SUGANO-W40S	9.00	0.62	0.65	-0.30
SUGANO-W40W	12.50	0.64	0.5	0.20
SUGANO-W80S	5.50	0.40	0.25	0.30
SUGANO-F	3.50	0.45	0.7	0.20
SUGANO-WBL	4.00	0.40	0.8	-1.20
SUGANO-WCO	12.50	0.39	0.5	0.30
HIGASHI 1-F1	10.50	0.75	0.94	3.00
HIGASHI 2-PW	17.50	0.63	0.47	1.40
HIGASHI 5-F2	1.70	0.18	0.536	-0.20
HIGASHI 13-FW	10.00	0.45	0.9	0.30
HIGASHI 4-C3C	12.50	1.00	0.2	9.60
HIGASHI 6-C2A	12.50	0.48	0.6	0.40
HIGASHI 7-C2B	6.00	0.49	0.5	7.00
HIGASHI 9-C40	10.50	0.31	0.98	3.10
HIGASHI 3-C3	12.50	0.85	0.25	0.20
HIGASHI 8-C4	12.50	1.35	0.45	0.50
CORLEY B5	3.00	0.02	0.7	-3.00
CORLEY B6	2.00	0.10	0.5	-0.50
CORLET B7	3.00	0.01	0.985	-3.00
CORLEY B8	5.50	0.55	0.95	-0.10
CORLEY B9	8.50	0.04	0.9	-0.10
CORLEY B11	6.00	0.05	0.7	0.30
OGATA K1	7.50	0.49	0.77	0.30
OGATA K2	12.50	0.02	0.99	0.20
OGATA K3	12.00	0.13	0.58	0.40
OGATA K4	12.50	0.08	0.98	0.20
OGATA K5	12.50	0.36	0.9	0.10
OGATA K6	10.50	0.42	1	-0.50
GAYNOR F	2.00	0.11	0.44	0.30
GAYNOR W	5.00	0.15	0.35	0.50
GAYNOR D	3.50	0.20	0.94	0.50

#### 4.2.2.1 Hysteresis Model for Existing Frames

Empirical expressions for  $\alpha$ ,  $\beta$ , and  $\gamma$  for existing reinforced concrete frames are given as follows:

$$\alpha = a_0 + a_1 d_{tb} + a_2 \rho_{vb} + a_3 b_c + a_4 P_{xc} + a_5 \left( \frac{P_{xc}}{A_c f_{cf}} \right) + a_6 \left( \frac{h_c}{L_b} \right) + a_7 \rho_{vc} + a_8 f_{cf} + a_9 f_y + a_{10} E_{cf} + a_{11} I_c$$

$$\beta = b_0 + b_1 b_{tb} + b_2 \rho_{fb} + b_3 \rho_{vb} + b_4 A_c + b_5 \left( \frac{h_c}{L_b} \right) + b_6 \rho_{fc} + b_7 f_y + b_8 E_{cf} + b_9 E_s$$

$$\gamma = g_0 + g_1 b_{tb} + g_2 \rho_{fb} + g_3 d_{bb} + g_4 b_{bb} + g_5 \rho_{vbb} + g_6 P_{xc} + g_7 \rho_{fc} + g_8 f_{cf} + g_9 f_y$$

The  $R^2$  values for the above hysteresis models are 0.90, 0.79, and 0.74 for  $\alpha$ ,  $\beta$ , and  $\gamma$ , respectively. The regression coefficients,  $a_i$ ,  $b_i$ , and  $g_i$ , are listed in Table 4.11. Note that these coefficients and all others that follow are calibrated for use with SI units. The variable definitions are given in Appendix A. The ratio of the predicted hysteresis parameters (calculated using the above empirical expressions) and the estimated hysteresis parameters (obtained from the system identification procedure) are plotted in Figures 4.19 a,b and c to facilitate an assessment of the adequacy of the empirical expressions in predicting the hysteresis parameters of the test specimens. A ratio of 1.0 means there is no deviation between the predicted and the estimated values.

TABLE 4.11 REGRESSION COEFFICIENTS FOR HYSTERESIS  
MODEL FOR EXISTING FRAME

i	a <sub>i</sub>	b <sub>i</sub>	g <sub>i</sub>
0	-160.952	3.749	-0.174
1	1.525	-5.47x10 <sup>-3</sup>	-7.6x10 <sup>-3</sup>
2	-49.955	-0.124	8.91x10 <sup>-2</sup>
3	-9.132	1.932	4.31x10 <sup>-3</sup>
4	-1.182	-8.61x10 <sup>-4</sup>	-0.011
5	539.596	-1.720	0.597
6	46.925	0.086	5.29x10 <sup>-3</sup>
7	13.186	0.125	-0.051
8	-463.459	-7.26x10 <sup>-3</sup>	1.685
9	3.269	-5.69x10 <sup>-4</sup>	0.204
10	1.381	-----	-----
11	4.99x10 <sup>-6</sup>	-----	-----

#### 4.2.2.2 Hysteresis Model for Frames with CIP Infilled Walls

Similarly, empirical expressions for  $\alpha$ ,  $\beta$ , and  $\gamma$  for reinforced concrete frames strengthened by CIP infilled walls are given as follows:

$$\begin{aligned}\alpha = & a_0 + a_1 d_{tb} + a_2 \rho_{vb} + a_3 b_c + a_4 P_{xc} + a_5 \left( \frac{P_{xc}}{A_c f_{cf}} \right) + a_6 \left( \frac{h_c}{L_b} \right) + a_7 \rho_{vc} \\ & + a_8 f_{cf} + a_9 f_y + a_{10} E_{cf} + a_{11} I_c + a_{12} t_w + a_{13} I_w + a_{14} I_0 \\ & + a_{15} \rho_{ww} + a_{16} f_{cw} + a_{17} f_{yw} + a_{18} f_{ya} + a_{19} A_{ac} + a_{20} d_{ac}\end{aligned}$$

$$\begin{aligned}\beta = & b_0 + b_1 b_{tb} + b_2 \rho_{fb} + b_3 \rho_{vb} + b_4 A_c + b_5 \left( \frac{h_c}{L_b} \right) + b_6 \rho_{fc} + b_7 f_y \\ & + b_8 E_{cf} + b_9 E_s + b_{10} t_w + b_{11} I_0 + b_{12} A_w + b_{13} \rho_{wh} + b_{14} \rho_{ww} \\ & + b_{15} f_{yw} + b_{16} A_{ab} + b_{17} d_{ab} + b_{18} s_{ac} + b_{19} A_{ac} f_{ya}\end{aligned}$$

$$\begin{aligned}\gamma = & g_0 + g_1 d_{tb} + g_2 d_c + g_3 P_{xc} + g_4 \left( \frac{P_{xc}}{A_c f_{cf}} \right) + g_5 \left( \frac{h_c}{L_{tb}} \right) + g_6 \rho_{cf} + g_7 f_{cf} \\ & + g_8 f_y + g_9 E_{cf} + g_{10} E_s + g_{11} \left( 12 E_{cf} \frac{I_c}{h_c^3} \right) + g_{12} t_w + g_{13} I_o + g_{14} h_3 \\ & + g_{15} f_{cw} + g_{16} \left( \frac{A_o}{L_w h_c} \right) + g_{17} f_{ya} + g_{18} (A_{ab} f_{ya}) + g_{19} s_{ac} + g_{20} (A_{ac} f_{ya})\end{aligned}$$

The corresponding regression coefficients,  $a_i$ ,  $b_i$ , and  $g_i$ , are listed in Table 4.12 as follows:

TABLE 4.12 REGRESSION COEFFICIENTS FOR HYSTERESIS MODEL  
FOR CAST-IN-PLACE INFILLED FRAMES

i	a <sub>i</sub>	b <sub>i</sub>	g <sub>i</sub>
0	-160.952	3.749	-14.224
1	1.525	-5.47x10 <sup>-3</sup>	0.017
2	-49.955	-0.124	0.130
3	-9.132	1.932	-0.022
4	-1.182	-8.61x10 <sup>-4</sup>	12.049
5	539.596	-1.720	-3.035
6	46.925	0.086	-0.044
7	13.186	0.125	-23.471
8	-463.459	-7.26x10 <sup>-3</sup>	0.285
9	3.269	-5.69x10 <sup>-4</sup>	0.071
10	1.381	-0.09	1.441x10 <sup>-1</sup>
11	4.99x10 <sup>-6</sup>	7x10 <sup>-8</sup>	-6.84x10 <sup>-5</sup>
12	-1.448	2.36x10 <sup>-4</sup>	-0.055
13	-2.29x10 <sup>-6</sup>	0.657	----
14	-2.29x10 <sup>-6</sup>	-0.550	-0.7x10 <sup>-7</sup>
15	-23.508	0.256	-0.014
16	26.881	-0.027	-0.735
17	13.636	-0.039	5.221
18	-2.285	0.015	0.109
19	-2.924	-6.81x10 <sup>-3</sup>	2.53x10 <sup>-3</sup>
20	1.555	-----	-0.02

#### 4.2.2.3 Hysteresis Model for Frame Infilled by Precast Panels

The empirical expressions for hysteresis parameters  $\alpha$ ,  $\beta$ ,  $\gamma$  for lightly reinforced concrete frames strengthened by adding precast concrete panels are given as follows:

$$\begin{aligned}\alpha = & a_0 + a_1 d_{bb} + a_2 \rho_{vb} + a_3 A_c + a_4 h_c + a_5 \rho_{vc} + a_6 E_s + a_7 I_c \\ & + a_8 (12E_{cf} \frac{I_c}{h_c^3}) + a_9 \rho_{hpc} + a_{10} A_{ab} + a_{11} f_{ya} + a_{12} (A_{ac} f_{ya})\end{aligned}$$

$$\begin{aligned}\beta = & b_0 + b_1 b_{ib} + b_2 d_{bb} + b_3 b_{bb} + b_4 b_c + b_5 A_c + b_6 \rho_{cf} + b_7 f_y + b_8 (12E_{cf} \frac{I_c}{h_c^3}) \\ & + \frac{b_9}{n} (\frac{L_b}{L_{pc}}) + b_{10} \rho_{hpc} + b_{11} (A_{ab} f_{ya}) + b_{12} s_{ac} + b_{13} d_{ac} + b_{14} (\sqrt{f_{cw}})\end{aligned}$$

$$\begin{aligned}\gamma = & g_0 + g_1 b_{ib} + g_2 \rho_{fb} + g_3 d_{bb} + g_4 b_{bb} + g_5 \rho_{vbb} + g_6 P_{xc} + g_7 \rho_{fc} + g_8 f_{cf} \\ & + g_9 f_y + g_{10} t_p + g_{11} L_{pc} + g_{12} f_{ya} + g_{13} (\sqrt{f_{cw}})\end{aligned}$$

The corresponding regression coefficients are listed in Table 4.13.

TABLE 4.13 REGRESSION COEFFICIENTS FOR HYSTERESIS MODEL  
FOR PRECAST PANEL INFILLED FRAME

i	a <sub>i</sub>	b <sub>i</sub>	g <sub>i</sub>
0	148.92	0.641	-0.174
1	1.302	-0.018	-7.6x10 <sup>-3</sup>
2	-38.426	0.034	0.089
3	0.037	0.02	4.31x10 <sup>-3</sup>
4	-0.154	-0.17	-0.011
5	2.577	2.24x10 <sup>-3</sup>	0.597
6	-0.093	0.072	5.29x10 <sup>-3</sup>
7	1.02x10 <sup>-6</sup>	0.368	-0.051
8	6.22x10 <sup>-4</sup>	-4.57x10 <sup>-5</sup>	1.685
9	-6.819	-0.429	0.204
10	0.243	0.981	0.198
11	2.694	-3.14x10 <sup>-3</sup>	-0.034
12	-0.503	0.043	0.019
13	----	-0.06	-0.034
14	----	-0.019	-----

#### 4.2.2.4 Hysteresis Model for Monolithic Wall-Frame Construction

Finally, the empirical expressions for  $\alpha$ ,  $\beta$ ,  $\gamma$  for monolithic wall-frame constructions are given as follows:

$$\begin{aligned}\alpha = & a_0 + a_1 d_{tb} + a_2 \rho_{vb} + a_3 b_c + a_4 P_{xc} + a_5 \left( \frac{P_{xc}}{A_c f_{cf}} \right) + a_6 \left( \frac{h_c}{L_b} \right) + a_7 \rho_{vc} + a_8 f_{cf} \\ & + a_9 f_y + a_{10} E_{cf} + a_{11} I_c + a_{12} t_w + a_{13} I_w + a_{14} I_o + a_{15} \rho_{vw} + a_{16} f_{cw} \\ & + a_{17} f_y + a_{18} f_{ytb} + a_{19} (A_{stb} f_{ytb}) + a_{20} A_{sbb} + a_{21} A_{sc} + a_{22} (A_{sc} f_{yc})\end{aligned}$$

$$\begin{aligned}\beta = & b_0 + b_1 b_{tb} + b_2 \rho_{fb} + b_3 \rho_{vb} + b_4 A_c + b_5 \left( \frac{h_c}{L_b} \right) + b_6 \rho_{fc} + b_7 f_y + b_8 E_{cf} \\ & + b_9 E_s + b_{10} t_w + b_{11} I_o + b_{12} A_w + b_{13} \rho_{wh} + b_{14} \rho_{vv} + b_{15} f_{yw} \\ & + b_{16} (t_w L_b \sqrt{f_{cw}}) + b_{17} (A_{stb} f_{ytb}) + b_{18} A_{sbb} + b_{19} A_{sc} + b_{20} S_{sc}\end{aligned}$$

$$\begin{aligned}\gamma = & g_0 + g_1 d_{tb} + g_2 d_c + g_3 P_{xc} + g_4 \left( \frac{P_{xc}}{A_c f_{cf}} \right) + g_5 \left( \frac{h_c}{L_b} \right) + g_6 \rho_{cf} + g_7 f_{cf} + g_8 f_y \\ & + g_9 E_{cf} + g_{10} E_s + g_{11} \left( 12 E_{cf} \frac{I_c}{h_c^3} \right) + g_{12} t_w + g_{13} I_w + g_{14} I_o \\ & + g_{15} h_3 + g_{16} f_{cw} + g_{17} \left( \frac{A_o}{L_w h_c} \right) + g_{18} A_{stb} + g_{19} S_{sbb} + g_{20} A_{sc}\end{aligned}$$

The regression coefficients are listed in Table 4.14 as follows:

TABLE 4.14 REGRESSION COEFFICIENTS FOR HYSTERESIS MODEL  
FOR MONOLITHIC WALL-FRAME CONSTRUCTION

i	a <sub>i</sub>	b <sub>i</sub>	g <sub>i</sub>
0	-160.952	3.749	-14.224
1	1.525	-5.47x10 <sup>-3</sup>	0.017
2	-49.955	-0.124	0.130
3	-9.132	1.932	-0.022
4	-1.182	-8.61x10 <sup>-4</sup>	12.049
5	539.596	-1.720	-3.035
6	46.925	0.086	-0.044
7	13.186	0.125	-23.471
8	-463.459	-7.26x10 <sup>-3</sup>	0.285
9	3.269	-5.69x10 <sup>-4</sup>	0.071
10	1.381	-0.09	1.441x10 <sup>-1</sup>
11	4.99x10 <sup>-6</sup>	7.46x10 <sup>-8</sup>	-6.84x10 <sup>-5</sup>
12	-1.448	2.36x10 <sup>-4</sup>	-0.055
13	-2.29x10 <sup>-6</sup>	0.657	-4.06x10 <sup>-9</sup>
14	-2.29x10 <sup>-6</sup>	-0.550	-6.64x10 <sup>-8</sup>
15	-23.508	0.256	-0.014
16	26.881	4.576x10 <sup>-5</sup>	-0.735
17	13.636	-0.026	5.221
18	-7.576	-0.0956	-0.068
19	1.629	0.107	0.049
20	-5.141	-0.054	0.097
21	3.872	----	----
22	-1.133	-----	-----

#### 4.2.3 Comparison between the Predicted and Experimental Hysteresis Parameters

From the four sets of empirical expressions for  $\alpha$ ,  $\beta$ ,  $\gamma$  given above, the hysteresis parameters of the fifty-five specimens selected in this program were predicted using the material and geometric properties of the specimens. The ratios of the predicted vs. experimental hysteresis parameters (obtained by system identification) were then plotted against the predicted parameters (see Figures 4.19a,b,c) to facilitate an assessment of the accuracy of the hysteresis models. A ratio of 1 means that the predicted parameter ( $\alpha_{\text{pre}}$ ,  $\beta_{\text{pre}}$ , or  $\gamma_{\text{pre}}$  from the hysteresis models) is identical to the experimental  $\alpha_{\text{exp}}$ ,  $\beta_{\text{exp}}$ , or  $\gamma_{\text{exp}}$  (from system identification of test results). As can be seen from Figures 4.19a,b, and c, the hysteresis models produce parameters that compare well with the hysteresis parameters determined from system identification of the given test specimens. It should be noted that, since the hysteresis models derived in the above sections are statistically based, the applicability of the models is limited to specimens with characteristics within the ranges of geometric and material properties of the selected fifty-five test specimens. Caution should be used when applying the derived hysteresis models to cases where material and geometric properties, reinforcement patterns, or reinforcement ratios fall outside the ranges of the selected specimens.

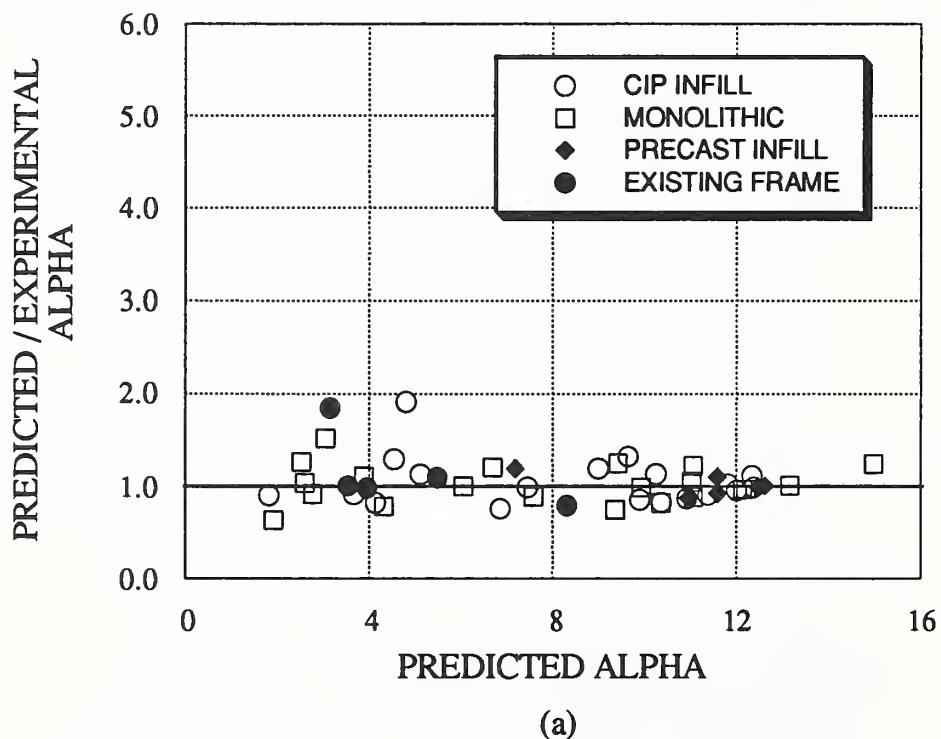
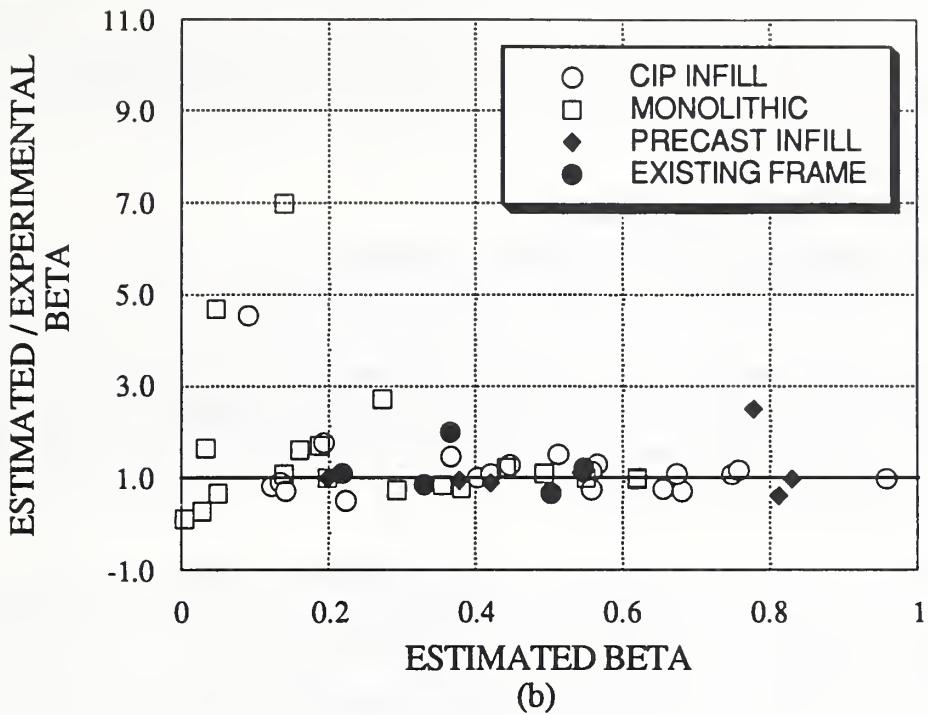
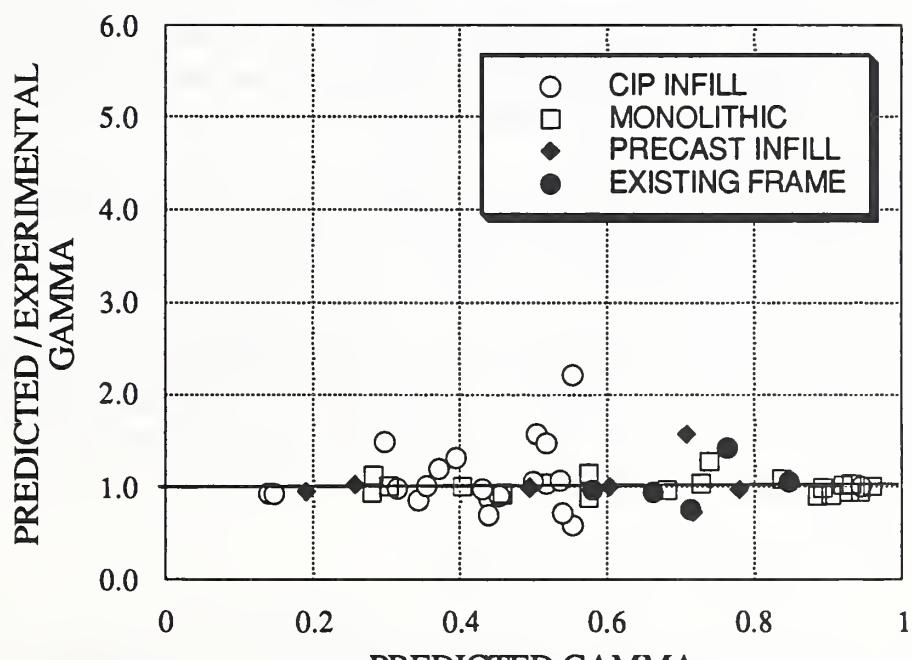


Figure 4.19 Comparisons of Predicted versus Experimental Hysteresis Parameters  
 (a) for Parameter  $\alpha$   
 (b) for Parameter  $\beta$   
 (c) for Parameter  $\gamma$



(b)



(c)

Figure 4.19 (Continued)

## 5. VALIDATION OF HYSTERETIC MODELS FOR USE WITH IDARC

The hysteresis models developed above allow hysteresis parameters  $\alpha$ ,  $\beta$ ,  $\gamma$  to be estimated for

- bare frames,
- monolithic wall-frame systems,
- frames strengthened by CIP infilled wall, and
- frames strengthened by multiple precast concrete panels.

The validity of the models for estimating hysteresis parameters for the ranges of geometric and material properties specified has been demonstrated in Section 4.2.2.5. The validity of using these models to predict the behavior of actual structures using IDARC is discussed in this chapter.

These parameters may be input into the program IDARC as rules for hysteresis behavior of RC frames for inelastic analysis. The validity of the hysteresis models may be examined by estimating, using the hysteresis models, the  $\alpha$ ,  $\beta$ ,  $\gamma$  values for a variety of RC frames that have been experimentally tested, using IDARC to analyze the frames, and comparing the analytical to the experimental results.

The validation process answers two main questions. 1) Do the improved hysteresis models result in more accurate analysis by IDARC? 2) Can entire structures be analyzed using the limited array of improved hysteresis models now available, or is more work needed before actual buildings and proposed retrofit schemes can be evaluated?

Two frames were analyzed, a one-story one-bay frame tested by Aoyama et al.<sup>8,9,10,11</sup> (specimen C2005-I), and a three-story one-bay frame specimen tested by Higashi et al<sup>48</sup> (specimen 78-3PW). For each frame, two IDARC analyses are performed, one using the IDARC recommended default values for hysteresis parameters  $\alpha$ ,  $\beta$ , and  $\gamma$ , and the other using hysteresis parameters obtained from the hysteresis models developed in this study. Analytically-obtained load-deformation characteristics, per-cycle absorbed energy, and ultimate load capacity were compared to those obtained from test results.

### 5.1 Analysis of One-Story One-Bay Frame

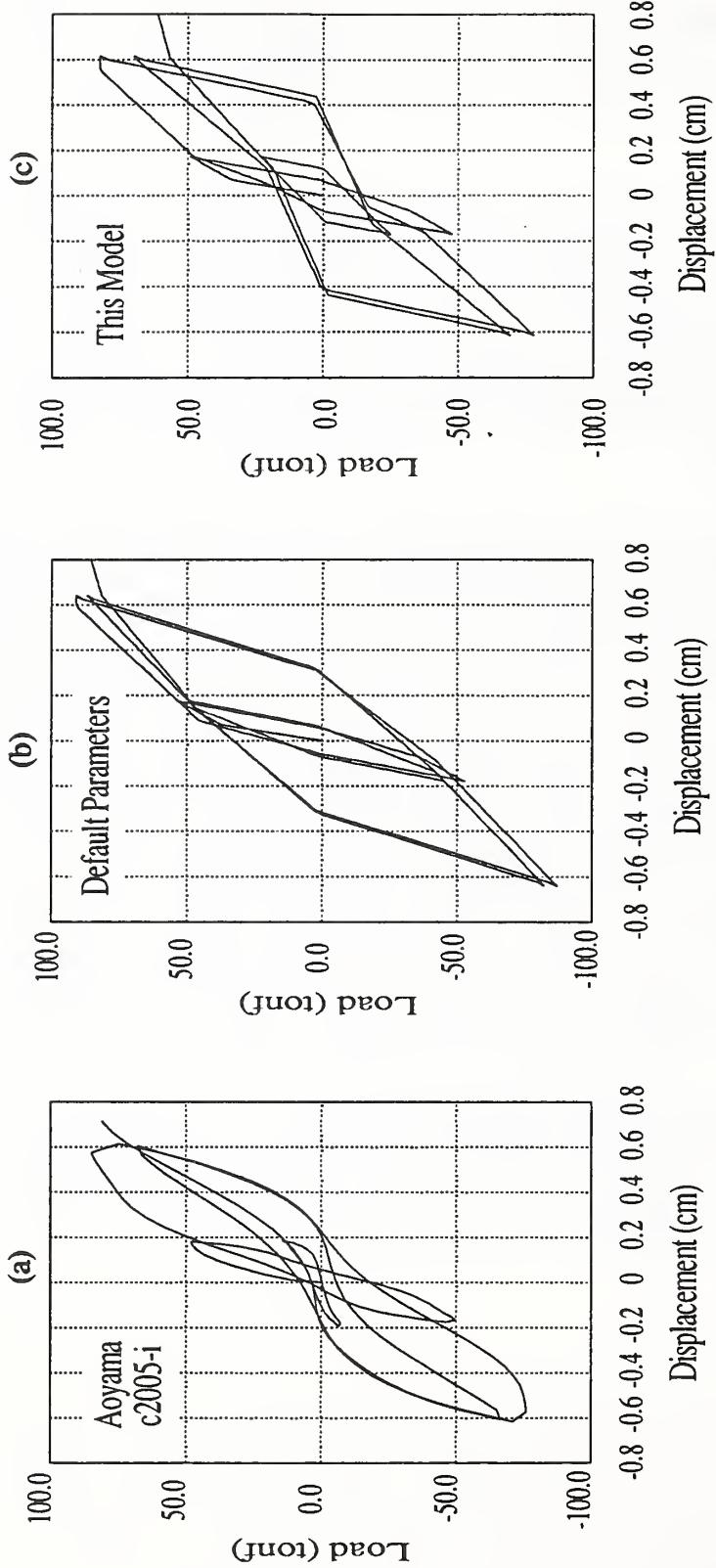
A one-story one-bay frame strengthened with a CIP infilled wall tested by Aoyama et al.<sup>8,9,10,11</sup> (specimen C2005-I) was analyzed using IDARC. The one-third scale model test specimen was constructed using modern deformed bars and adequate transverse reinforcement rather than the smooth bars and minimal transverse reinforcement typical of Japanese construction prior to the 1960's. The cast in place infilled wall was connected to the frame using epoxied anchors. After placement of concrete, the gap left

between the underside of the top beam and the top of the infilled wall was filled with expansive mortar. The specimen was subjected to five cycles of statically reversing lateral load. The measured ultimate strength of 84.2 tonf was attained in the second cycle. In the fifth cycle the specimen was loaded to failure. The experimental hysteresis behavior, measured at the center of the top beam and digitized in this study, is shown in Figure 5.1 a.

Two IDARC runs were performed, one using the default hysteresis parameters recommended by IDARC ( $\alpha=2.0$ ,  $\beta=0.02$ ,  $\gamma=0.5$ ), and one using the hysteresis parameters obtained from the hysteresis model developed in this study ( $\alpha=11.0$ ,  $\beta=0.35$ , and  $\gamma=0.25$ ). The analytical hysteresis behavior of the frame corresponding to these two analyses is shown in Figure 5.1 b and c. Further, the absorbed energy per cycle, calculated based on the experimental result and the two analytical results, are shown in Figure 5.2 for comparison.

As can be seen in Figure 5.1 a, b, and c, the experimental load-deformation characteristics of the frame was more closely matched by the analytical result which used the hysteresis parameters generated by the hysteresis models developed in this study. The default hysteresis parameters appear unable to correctly characterize the strength degradation characteristic (the decreasing load capacity with increasing number of cycle) and the pinching action of the frame. The ultimate load capacities, being 84.1 tonf for the experimental result, 84.3 tonf for the analytical result using hysteresis model developed in this study, and 95.5 tonf for the analytical result using the default hysteresis parameters, also show better comparison between the model developed in this study and the result of experiment. In terms of absorbed energy per cycle, the comparison between the result of this model and that of the experimental result is also more favorable than the comparison between the result using default parameters and the experiment, as illustrated in Figure 5.2. This is due to the ability of the model to characterize more accurately the pinching action that was observed in the experiment.

The results of these analyses show that the hysteresis model can be incorporated into IDARC, and that it does result in an improvement in the predictive ability of the analysis program. It also validates the idea of modeling an infilled frame as a single shear wall element, rather than as two beams, a column, and a wall.



**Figure 5.1 Comparisons of Experimental and Analytical Hysteresis Behavior for Aoyama's One-Story, One-Bay Frame C2005-I**

- (a) Experimental
- (b) IDARC's Prediction Using Default Hysteresis Parameters
- (c) IDARC's Prediction Using Hysteresis Parameters from Models Developed in This Study

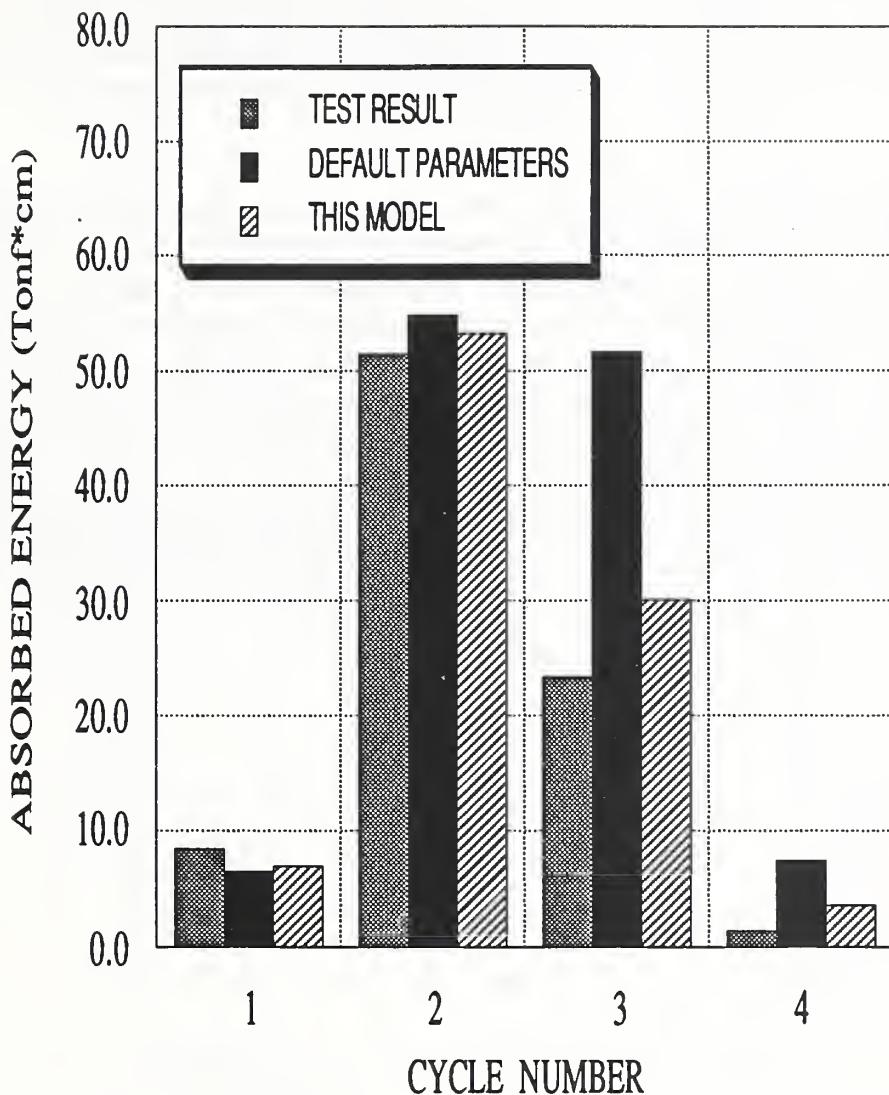


Figure 5.2 Comparisons of Experimental and Analytical Absorbed Energy on the Per Cycle Basis for Aoyama's Frame C2005-I

## 5.2 Analysis of a Three-Story One-Bay Frame

A three-story one-bay frame tested by Higashi et al.<sup>48</sup> (specimen 79-3PW) was analyzed using IDARC. The one-eighth scale model was strengthened by filling all three openings with CIP concrete. The specimen was subjected to 6 cycles of displacement-controlled reversed cyclic loadings under constant axial load. Load-displacement curves were recorded at the top of the first story. The specimen achieved an ultimate load of 8.2 tonf before failing.

Two IDARC analyses were performed, one using default values and the other using hysteresis parameters obtained from the hysteresis models developed in this study. Similar to the case of the one-story one-bay frame described in 5.1, the load-deformation characteristics of the frame were more closely matched by using the hysteresis model developed in this study than by using the default hysteresis parameters, as can be seen in Figure 5.3 a, b, and c. Ultimate strengths at the first story of 8.4 tonf and 9.5 tonf, respectively, were predicted for the two analytical cases where the hysteresis parameters obtained from this model and the default hysteresis parameters were used. Comparisons of absorbed energy per cycle, as shown in Figure 5.4, also show an improvement in predictive ability of the model developed in this study over the default hysteresis parameters.

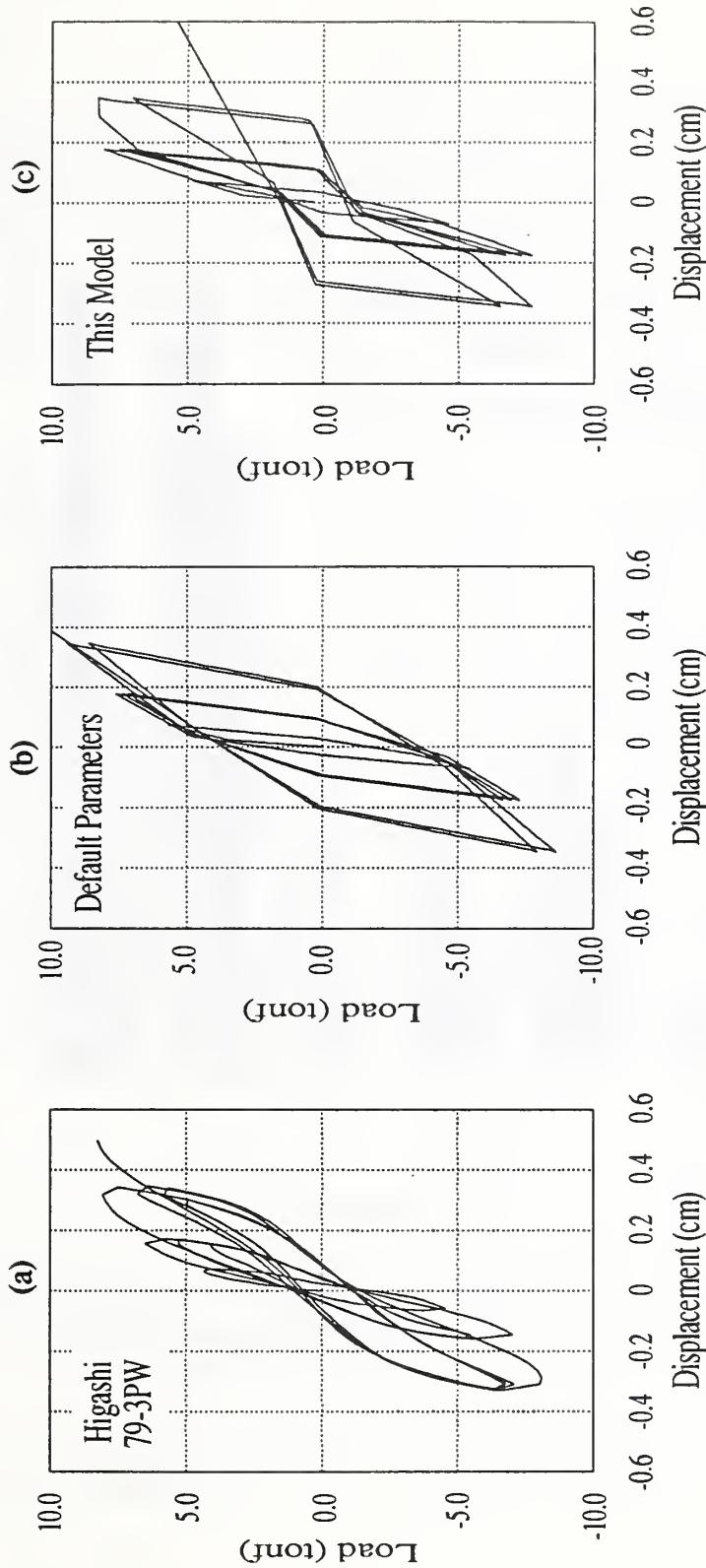


Figure 5.3 Comparisons of Experimental and Analytical Hysteresis Behavior for Higashi's Three-Story, One-Bay Frame 79-3PW

(a) Experimental  
 (b) IDARC's Prediction Using Default Hysteresis Parameters  
 (c) IDARC's Prediction Using Hysteresis Parameters from Models Developed in This Study

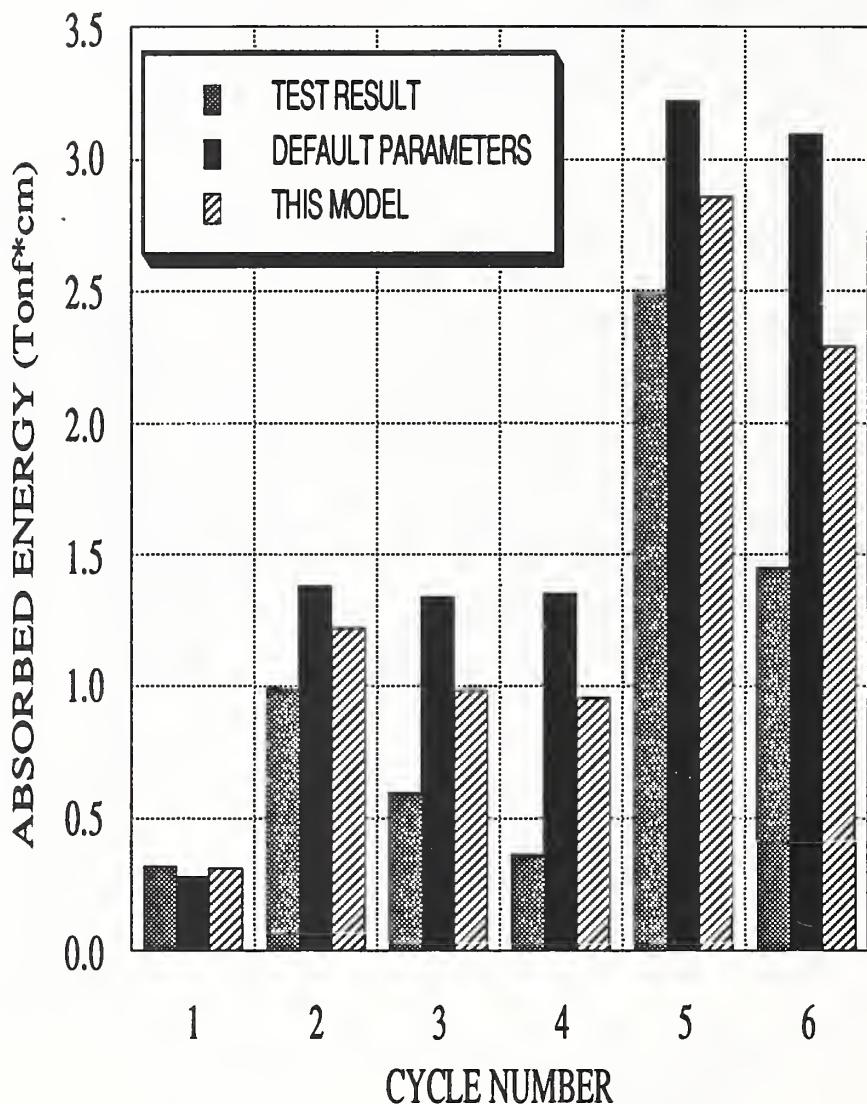


Figure 5.4 Comparisons of Experimental and Analytical Absorbed Energy on the Per Cycle Basis for Higashi's Frame 79-3PW

## 6. SUMMARY, CONCLUSIONS, AND RECOMMENDATION

### 6.1 Summary

Experimental results of fifty five lightly reinforced concrete, one-story one-bay frame specimens, including bare frames, monolithic wall-frame constructions, frames infilled with CIP reinforced concrete walls, and frames infilled with precast reinforced concrete panels were systematically examined. The purpose is to develop empirical expressions, also called hysteresis models in this study, for predicting the three parameters  $\alpha$ ,  $\beta$ ,  $\gamma$  which characterize the hysteresis behavior of reinforced concrete frames. The procedure used in developing the hysteresis models involved the following major tasks:

- Create a digital database for storage of load-deformation characteristics of lightly reinforced concrete one-story one-bay frames subjected to quasi-static reversed cyclic loading. This database, as of now, consists of fifty five tests.
- Perform system identification of the digitized load-deformation records, using NIST System Identification program NIDENT 3.0, to obtain the estimated hysteresis parameters  $\alpha$ ,  $\beta$ ,  $\gamma$ , for each of the fifty five tests. The digitized load-deformation record of each of the fifty five specimens selected in this study are shown in Appendix C, superposed by the corresponding hysteresis behavior obtained from the system identification process.
- Correlate the estimated hysteresis parameters  $\alpha$ ,  $\beta$ ,  $\gamma$ , with the geometric and material properties, and reinforcement information using the commercially available Statistical Analysis package. The results are empirical expressions, or hysteresis models, for  $\alpha$ ,  $\beta$ ,  $\gamma$  in terms of the physical properties of reinforced concrete frames.

The hysteresis models were then used to compute the hysteresis parameters of two strengthened frames. The first frame was a one-bay one-story infilled frame tested by Aoyama et al. (specimen C2005-I). The second frame was a three-story one-bay infilled frame tested by Higashi et al. (specimen 79-3PW). The computed hysteresis parameters were used in IDARC analyses of the frames and the results were compared with both the test results and the analytical results where the default values of  $\alpha$ ,  $\beta$ ,  $\gamma$ , recommended by IDARC, were used. Comparisons were made in terms of experimental and analytical load-deformation characteristics, absorbed energy per cycle, and ultimate load capacities. The comparisons show an improvement in predictive ability of the program IDARC when the hysteresis models developed in this study were used in providing hysteresis rules.

## 6.2 Conclusions

The empirical hysteresis models developed in this study, as well as the program IDARC, are still research tools and admittedly cumbersome to use. These tools, however, are capable of providing reasonable estimates of the hysteresis performance of reinforced concrete frames. From the results of this phase of the study, the following conclusions are drawn:

- The hysteresis performance (load-deformation histories) of one-bay one-story reinforced concrete bare frames, monolithic wall-frame constructions, frames infilled by CIP concrete walls, and frames infilled by precast concrete panels may be reasonably predicted using the hysteresis models developed in this study (see results in Appendix C).
- The hysteresis parameters obtained from the empirical hysteresis models developed in this study can be successfully incorporated into the program IDARC for use in the analysis of lightly reinforced concrete frames with more than one story in height.
- The database for load-deformation histories for one-bay, one-story frames created in this study enables a systematic examination of hysteresis performance of the unstrengthened and strengthened frames. These data currently are limited to two methods of frame strengthening, the CIP infilled wall and the multiple precast infilled wall methods. Future expansion of the existing database to include data concerning other frame strengthening techniques such as infilling with masonry walls, steel bracing, etc., will result in broader application and more statically significant hysteresis models.
- The hysteresis models presented in this study are developed based on the limited number of available frame tests. The complexity of the models may be reduced in the future by the increase in the number of available test data and by limiting the number of variables in the regression analysis to a few major variables.
- The same model development approach presented in this study can be used in developing hysteresis models for beam-column joints and column strengthening techniques to provide more analytical options for the selection of strengthening schemes for existing RC frames.

### 6.3 Recommendation

Even though the hysteresis models developed in this study are cumbersome to use and might be judged impractical by practitioners, such models are needed to make use of computer programs (i.e. IDARC) to predict inelastic behavior of strengthened concrete frame structures. At the present time, these models are limited to CIP infilled walls and multiple precast infilled wall panels. Specifically, through the use of appropriate values of  $\alpha$ ,  $\beta$ ,  $\gamma$  given by the empirical relationships developed in this report, one should be able to evaluate the structural responses of RC frames strengthened by CIP or precast infilled walls with different wall thicknesses, reinforcement ratios, or amounts of connecting anchors. Such evaluation process will provide an economical means for the selection of an optimal strengthening scheme.

In terms of model applicability, the hysteresis models developed in this study (which were based on one-bay, one-story frame test data) have been validated, as described in chapter 5, for two cases, i.e. one-bay, one-story frames; and one-bay, three-story frames. Thus, the application of the hysteresis models for the design and analysis of one-bay one-story, and one-bay multi-story frames is recommended. For the case of multi-bay one-story frames or multi-bay multi-story frames, the hysteresis models can be used for IDARC analysis in the same manner. At the present time, however, there is no experimental data currently exist for use in validating the analytical results for frames with more than one bay. It is suggested that the analytical results for the cases involving structures with more than one bay should be used with caution.

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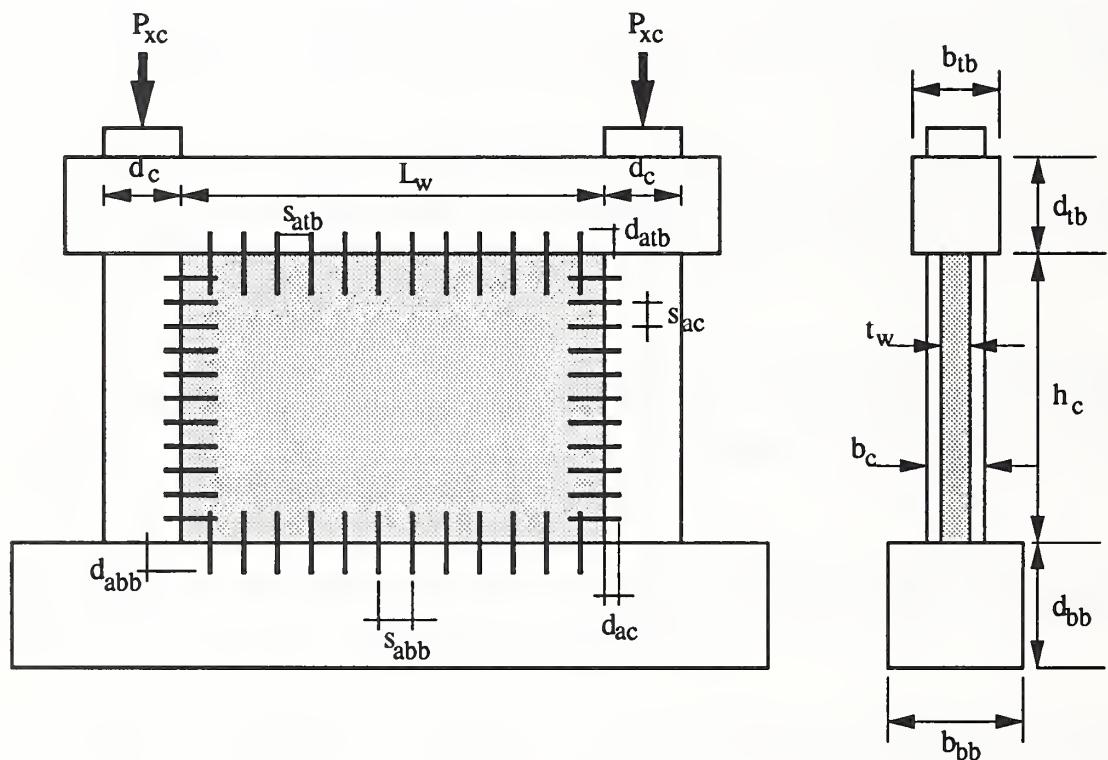
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## APPENDIX A. Definitions of Variables Used in Regression Analysis



## APPENDIX A. (Continued)

Variable	Symbols	Descriptions
<b>VARIABLES RELATING TO EXISTING FRAME</b>		
X1	$d_{tb}$	Top Beam Effective Depth
X2	$b_{tb}$	Top Beam Width
X3	$A_{st}/d_{tb}b_{tb}$	Total flexural Rein. Ratio of Top Beam
X4	$\rho_{tb,sh}$	Shear Rein. Ratio of Top Beam
X5	$b_{bb}$	Bottom Beam Effective Depth
X6	$b_{bb}$	Bottom Beam Width
X7	$A_{sb}/d_{bb}b_{bb}$	Total Flexural Rein. Ratio of Bottom Beam
X8	$\rho_{bb,sh}$	Shear Rein. Ratio of Bottom Beam
X9	$d_c$	Column Effective Depth
X10	$b_c$	Column Width
X11	$A_c$	Column Effective Area ( $d_c \cdot b_c$ )
X12	$A_{cg}$	Column Gross Cross Section Area
X13	$P_{xc}$	Axial Force in Each Column
X14	$P_{xc}/A_{cg} \cdot f_{c,f}$	Normalized Column Axial Stress
X15	$b_c$	Column Height
X16	$h_c/L_{tb}$	Ratio of Column Height to Top Beam Clear Span
X17	$\rho_{f,cl}$	Total Flex. Rein. Ratio of Left Column
X18	$\rho_{sh,cl}$	Shear Rein. Ratio of Left Column
X19	$\rho_{f,cr}$	Total Flex. Rein. Ratio of Right Column
X20	$\rho_{sh,cr}$	Shear Rein. Ratio of Right Column
X21	$f_{c,f}$	Concrete Compressive Strength of Frame
X22	$f_y$	Reinforcement Yield Strength

## APPENDIX A. (Continued)

Variable	Symbols	Descriptions
X23	$E_{c,f} (= 15,100\sqrt{f_{c,f}})$	Young's Modulus of Concrete
X24	$E_s$	Young's Modulus of Steel Reinforcement
X25	$I_c$	Moment of Inertia of Frame's Horizontal Cross-Section (Two Columns Cross-Sections)
X26	$12.E_{c,f}.I_c/h_c^3$	Lateral Stiffness of Frame

### VARIABLES RELATING TO CAST-IN-PLACE INFILL WALLS

X27	$t_w$	Thickness of Infill Wall
X28	$I_w$	Moment of Inertia of Horizontal Cross Section of Infill Wall-Column System w/o Opening
X29	$I_o$	Moment of Inertia of Horizontal Cross Section of Opening
X30	$h_1$	Height From Column Base to Bottom of Opening
X31	$h_2$	Height From Bottom to Top of Opening
X32	$h_3$	Height From Top of Opening to Bottom of Top Beam
X33	$A_w$	Horizontal Cross Sectional Area of the Infill Wall-Column System
X33	$A_o$	Horizontal Cross Sectional Area of the Opening
X35	$[h_3^3/3.E_c.I_w] + [h_3/A_w.G_w]$	Lateral Stiffness of Portion of Wall Above Opening ( $G_w = E_c/2(1+\nu)$ )
X36	$[h_2^3/12.E_c.(I_w-I_o)] + [h_2/(A_w-A_o).G_w]$	Lateral Stiffness of Portion of Wall Below Opening

## APPENDIX A. (Continued)

Variable	Symbols	Descriptions
X37	$\rho_{w,h}$	Horizontal Rein. Ratio for Infill Wall
X38	$\rho_{w,v}$	Vertical Rein. Ratio for Infill Wall
X39	$\rho_{w,sh}$	Shear Rein. Ratio for Infill Wall
X40	$f_{c,w}$	Concrete Compressive Strength for Infill Wall
X41	$f_{y,w}$	Yield Strength of Infill Wall's Reinforcements
X42	$A_{ov}$	Vertical Area of Wall Opening
X43	$A_{ov1}/(L_w \cdot h_c)_1$	Ratio of Area of Opening in the First Quadrant (Top Left) and Area of the First Quadrant of Infill Wall
X44	$A_{ov2}/(L_w \cdot h_c)_2$	Ratio..... Second Quadrant (Bottom Left) .....
X45	$A_{ov3}/(L_w \cdot h_c)_3$	Ratio..... Third Quadrant (Top Right).....
X46	$A_{ov4}/(L_w \cdot h_c)_4$	Ratio..... Fourth Quadrant (Bottom Right).....

### VARIABLES RELATING TO PRECAST PANEL INFILL WALLS

X47	$t_p$	Thickness of Precast Panel
X48	$L_{pe}$	Length of Each Precast Panel
X49	$L_{tb}/n \cdot L_{pe}$	Ratio of Top Beam Length and Length of Precast Panel, n is the Number of Panels Used.
X50	$\rho_{h,pe}$	Horizontal Rein. Ratio of Each Precast Panel
X51	$\rho_{v,pe}$	Vertical Rein. Ratio of Each Precast Panel
X52	$\rho_{sh,pe}$	Shear Rein. Ratio of Each Precast Panel

## APPENDIX A. (Continued)

Variable	Symbols	Descriptions
X53	$A_{ov1}/(L_{tb} \cdot h_c)_1$	Ratio of Area of Opening in the First Quadrant (Top Left) and Area of the First Quadrant of Infill Wall
X54	$A_{ov2}/(L_{tb} \cdot h_c)_2$	Ratio..... second Quadrant (Bottom Left) .....
X55	$A_{ov3}/(L_{tb} \cdot h_c)_3$	Ratio..... third Quadrant (Top Right).....
X56	$A_{ov4}/(L_{tb} \cdot h_c)_4$	Ratio..... Fourth Quadrant (Bottom Right).....

### VARIABLES RELATING TO CONNECTING ANCHORS (For Cast-in-Place Infill Walls)

X57	$A_{a,tb}$	Total Area of Anchors Crossing the Interface Between the Infill Wall & Top Beam
X58	$s_{a,tb}$	Anchor Spacing at Top Beam
X59	$d_{a,tb}$	Anchor Embedment Depth at Top Beam
X60	$f_{y,a,tb}$	Material Yield Stress of Anchors on Top Beam
X61	$A_{a,tb} \cdot f_{y,a,tb}$	Tensile Strength of Anchors on Top Beam
X62	$A_{a,bb}$	Total Area of Anchors and Rebars Crossing the Interface Between the Infill Wall & Bottom Beam
X63	$s_{a,bb}$	Anchor Spacing at Bottom Beam
X64	$d_{a,bb}$	Anchor Embedment Depth at Bottom Beam
X65	$f_{y,a,bb}$	Material Yield Stress of Anchors on Bottom Beam

## APPENDIX A. (Continued)

Variable	Symbols	Descriptions
X66	$A_{a,bb} \cdot f_{y,a,bb}$	Tensile Strength of Anchors on Bottom Beam
X67	$A_{a,cl}$	Total Area of Anchors and Rebars Crossing the Interface Between the Infill Wall & Left Column
X68	$s_{a,cl}$	Anchor Spacing in Left Column
X69	$d_{a,cl}$	Anchor Embedment Depth in Left Column
X70	$f_{y,a,cl}$	Material Yield Stress of Anchors on Left Column
X71	$A_{a,cl} \cdot f_{y,a,cl}$	Tensile Strength of Anchors on Left Column
X72	$A_{a,cr}$	Total Area of Anchors and Rebars Crossing the Interface Between the Infill Wall & Right Column
X73	$s_{a,cr}$	Anchor Spacing in Right Column
X74	$d_{a,cr}$	Anchor Embedment Depth in Right Column
X75	$f_{y,a,cr}$	Material Yield Stress of Anchors on Right Column
X76	$A_{a,cr} \cdot f_{y,a,cr}$	Tensile Strength of Anchors on Right Column

### **VARIABLES RELATING TO CONNECTING ANCHORS (For Monolithically-cast Wall-Frame Systems)**

X77	$t_w \cdot L_{tb} \cdot f_{c,w}$	(For Monolithically-Cast Wall-Frame System only, = 0 for all other cases)
X78	$A_{s,tb}$	Total Area of Rebars Crossing the Interface Between Wall & Top Beam of Frame
X79	$s_{s,tb}$	Rebar Spacing at Top Beam

## APPENDIX A. (Continued)

Variable	Symbols	Descriptions
X80	$f_{y,s,tb}$	Material Yield Stress of Rebar on Top Beam
X81	$A_{s,tb} \cdot f_{y,s,tb}$	Tensile Strength of Rebars on Top Beam
X82	$A_{s,bb}$	Total Area of Rebars Crossing the Interface Between Wall & Bottom Beam of Frame
X83	$s_{s,bb}$	Rebar Spacing at Bottom Beam
X84	$f_{y,s,bb}$	Material Yield Stress of Anchors on Bottom Beam
X85	$A_{s,bb} \cdot f_{y,s,bb}$	Tensile Strength of Anchors on Bottom Beam
X86	$A_{s,cl}$	Total Area of Rebars Crossing the Interface Between Wall & Left Column of Frame
X87	$s_{s,cl}$	Rebar Spacing at Left Column
X88	$f_{y,s,cl}$	Material Yield Stress of Rebars on Left Column
X89	$A_{s,cl} \cdot f_{y,s,cl}$	Tensile Strength of Rebars in Left Column
X90	$A_{s,cr}$	Total Area of Rebars Crossing the Interface Between Wall & Right Column of Frame
X91	$s_{s,cr}$	Rebar Spacing in Right Column
X92	$f_{y,s,cr}$	Material Yield Stress of Rebars on Right Column
X93	$A_{s,cr} \cdot f_{y,s,cr}$	Tensile Strength of Rebars in Right Column

## APPENDIX B. Test Specimen's Parameters

TEST NAME	X1 (CM)	X2 (CM)	X3 (%)	X4 (%)	X5 (CM)	X6 (CM)
AOYAMA C2005-I	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA C2005-II	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA C2005-III	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA C2015-A	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA C2015-B	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA C2015-C	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA P2005-A	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA P2015-A	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA C4015	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA P4015	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA M2005	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA CH2015	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA CH2018	35.00	30.00	4.86	0.48	45.00	65.00
AOYAMA OLU2015	35.00	30.00	4.86	0.48	45.00	65.00
KAHN SP1	15.88	60.96	1.10	0.14	34.93	15.24
KAHN SP2	15.88	60.96	1.10	0.14	34.93	15.24
KAHN SP3	15.88	60.96	1.10	0.14	34.93	15.24
KAHN SP5	15.88	60.96	1.10	0.14	34.93	15.24
HAYASHI-W1	17.00	20.00	2.98	0.11	47.00	30.00
HAYASHI-W2	17.00	20.00	2.98	0.11	47.00	30.00
HAYASHI-W4	17.00	20.00	2.98	0.11	47.00	30.00
HAYASHI-W5	17.00	20.00	2.98	0.11	47.00	30.00
HAYASHI-W6	17.00	20.00	2.98	0.11	47.00	30.00
SUGANO-WHA	22.00	15.00	1.54	0.17	47.00	55.00
SUGANO-W40S	22.00	15.00	1.54	0.17	47.00	55.00
SUGANO-W40W	22.00	15.00	1.54	0.17	47.00	55.00
SUGANO-W80S	22.00	15.00	1.54	0.17	47.00	55.00
SUGANO-F	22.00	15.00	1.54	0.17	47.00	55.00
SUGANO-WBL	22.00	15.00	1.54	0.17	47.00	55.00
SUGANO-WCO	22.00	15.00	1.54	0.17	47.00	55.00
HIGASHI 1-F1	17.00	20.00	2.98	0.11	37.00	50.00
HIGASHI 2-PW	17.00	20.00	2.98	0.11	37.00	50.00
HIGASHI 5-F2	17.00	20.00	2.98	0.11	34.00	50.00
HIGASHI13-FW	17.00	20.00	2.98	0.11	34.00	50.00
HIGASHI 4-C3C	17.00	20.00	2.98	0.11	37.00	50.00
HIGASHI 6-C2A	17.00	20.00	2.98	0.11	34.00	50.00
HIGASHI 7-C2B	17.00	20.00	2.98	0.11	34.00	50.00
HIGASHI 9-C40	17.00	20.00	2.98	0.11	34.00	50.00
HIGASHI 3-C3	17.00	20.00	2.98	0.11	37.00	50.00
HIGASHI 8-C4	17.00	20.00	2.98	0.11	34.00	50.00
CORLEY B5	15.24	121.92	1.00	0.10	54.61	121.92
CORLEY B6	15.24	121.92	1.00	0.10	54.61	121.92
CORLEY B7	15.24	121.92	1.00	0.10	54.61	121.92
CORLEY B8	15.24	121.92	1.00	0.10	54.61	121.92
CORLEY B9	15.24	121.92	1.00	0.10	54.61	121.92
CORLEY B11	15.24	121.92	1.00	0.10	54.61	121.92
OGATA K1	27.00	50.00	1.68	0.57	27.00	50.00
OGATA K2	27.00	50.00	1.68	0.57	27.00	50.00
OGATA K3	27.00	50.00	1.68	0.57	27.00	50.00
OGATA K4	27.00	50.00	1.68	0.57	27.00	50.00
OGATA K5	27.00	50.00	1.68	0.57	27.00	50.00
OGATA K6	27.00	50.00	1.68	0.57	27.00	50.00
GAYNOR F	83.82	30.48	0.91	0.56	53.34	45.72
GAYNOR W	83.82	30.48	0.91	0.56	53.34	45.72
GAYNOR D	83.82	30.48	0.91	0.56	53.34	45.72

## APPENDIX B. (Continued)

TEST NAME	X7 (%)	X8 (%)	X9 (CM)	X10 (CM)	X11 (CM2)	X12 (CM2)
AOYAMA C2005-I	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA C2005-II	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA C2005-III	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA C2015-A	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA C2015-B	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA C2015-C	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA P2005-A	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA P2015-A	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA C4015	1.82	0.22	37.00	20.00	740.00	800.00
AOYAMA P4015	1.82	0.22	37.00	20.00	740.00	800.00
AOYAMA M2005	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA CH2015	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA CH2018	1.82	0.22	17.00	20.00	340.00	400.00
AOYAMA OLU2015	1.82	0.22	17.00	20.00	340.00	400.00
KAHN SP1	0.38	0.14	13.34	15.24	203.30	232.26
KAHN SP2	0.38	0.14	13.34	15.24	203.30	232.26
KAHN SP3	0.38	0.14	13.34	15.24	203.30	232.26
KAHN SP5	0.38	0.14	13.34	15.24	203.30	232.26
HAYASHI-W1	2.16	0.11	17.00	20.00	340.00	400.00
HAYASHI-W2	2.16	0.11	17.00	20.00	340.00	400.00
HAYASHI-W4	2.16	0.11	17.00	20.00	340.00	400.00
HAYASHI-W5	2.16	0.11	17.00	20.00	340.00	400.00
HAYASHI-W6	2.16	0.11	17.00	20.00	340.00	400.00
SUGANO-WHA	2.00	0.17	17.00	20.00	340.00	400.00
SUGANO-W40S	2.00	0.17	17.00	20.00	340.00	400.00
SUGANO-W40W	2.00	0.17	17.00	20.00	340.00	400.00
SUGANO-W80S	2.00	0.17	17.00	20.00	340.00	400.00
SUGANO-F	2.00	0.17	17.00	20.00	340.00	400.00
SUGANO-WBL	2.00	0.17	17.00	20.00	340.00	400.00
SUGANO-WCO	2.00	0.17	17.00	20.00	340.00	400.00
HIGASHI 1-F1	0.54	0.04	17.00	20.00	340.00	400.00
HIGASHI 2-PW	0.54	0.04	17.00	20.00	340.00	400.00
HIGASHI 5-F2	0.59	0.04	17.00	20.00	340.00	400.00
HIGASHI13-FW	0.59	0.04	17.00	20.00	340.00	400.00
HIGASHI 4-C3C	0.54	0.04	17.00	20.00	340.00	400.00
HIGASHI 6-C2A	0.59	0.04	17.00	20.00	340.00	400.00
HIGASHI 7-C2B	0.59	0.04	17.00	20.00	340.00	400.00
HIGASHI 9-C40	0.59	0.04	17.00	20.00	340.00	400.00
HIGASHI 3-C3	0.54	0.04	17.00	20.00	340.00	400.00
HIGASHI 8-C4	0.59	0.04	17.00	20.00	340.00	400.00
CORLEY B5	1.00	0.10	27.94	30.48	851.61	929.03
CORLEY B6	1.00	0.10	27.94	30.48	851.61	929.03
CORLEY B7	1.00	0.10	27.94	30.48	851.61	929.03
CORLEY B8	1.00	0.10	27.94	30.48	851.61	929.03
CORLEY B9	1.00	0.10	27.94	30.48	851.61	929.03
CORLEY B11	1.00	0.10	27.94	30.48	851.61	929.03
OGATA K1	2.10	0.57	17.00	20.00	340.00	400.00
OGATA K2	2.10	0.57	17.00	20.00	340.00	400.00
OGATA K3	2.10	0.57	17.00	20.00	340.00	400.00
OGATA K4	2.10	0.57	17.00	20.00	340.00	400.00
OGATA K5	2.10	0.57	17.00	20.00	340.00	400.00
OGATA K6	2.10	0.57	17.00	20.00	340.00	400.00
GAYNOR F	1.59	0.25	22.86	30.48	696.77	929.03
GAYNOR W	1.59	0.25	22.86	30.48	696.77	929.03
GAYNOR D	1.59	0.25	22.86	30.48	696.77	929.03

## APPENDIX B. (Continued)

TEST NAME	X13 (TONF)	X14	X15 (CM)	X16	X17 (%)	X18 (%)
AOYAMA C2005-I	12.00	0.12712	97.00	0.539	1.49	0.21
AOYAMA C2005-II	12.00	0.12712	97.00	0.539	1.49	0.21
AOYAMA C2005-III	12.00	0.13274	97.00	0.539	1.49	0.21
AOYAMA C2015-A	12.00	0.13453	97.00	0.539	4.47	0.21
AOYAMA C2015-B	12.00	0.15152	97.00	0.539	4.47	0.21
AOYAMA C2015-C	12.00	0.074442	97.00	0.539	4.47	0.21
AOYAMA P2005-A	12.00	0.13636	97.00	0.539	1.49	0.21
AOYAMA P2015-A	12.00	0.076142	97.00	0.539	4.47	0.21
AOYAMA C4015	12.00	0.064103	97.00	0.606	2.06	0.21
AOYAMA P4015	12.00	0.050505	97.00	0.606	2.06	0.21
AOYAMA M2005	12.00	0.099668	97.00	0.539	1.49	0.21
AOYAMA CH2015	12.00	0.10381	97.00	0.539	4.47	0.21
AOYAMA CH2018	12.00	0.11494	97.00	0.539	5.35	0.21
AOYAMA OLU2015	12.00	0.13453	97.00	0.539	4.47	0.21
KAHN SP1	0.00	0	149.86	0.615	3.94	0.07
KAHN SP2	0.00	0	149.86	0.615	3.94	0.07
KAHN SP3	0.00	0	149.86	0.615	3.94	0.07
KAHN SP5	0.00	0	149.86	0.615	3.94	0.07
HAYASHI-W1	12.00	0.16393	90.00	0.5625	1.49	0.11
HAYASHI-W2	12.00	0.16393	90.00	0.5625	1.49	0.11
HAYASHI-W4	12.00	0.16393	90.00	0.5625	1.49	0.11
HAYASHI-W5	12.00	0.16216	90.00	0.5625	1.49	0.11
HAYASHI-W6	12.00	0.16216	90.00	0.5625	1.49	0.11
SUGANO-WHA	12.48	0.13	80.00	0.53333	1.49	0.13
SUGANO-W40S	12.48	0.13	80.00	0.53333	1.49	0.13
SUGANO-W40W	12.48	0.13	80.00	0.53333	1.49	0.13
SUGANO-W80S	12.48	0.13	80.00	0.53333	1.49	0.13
SUGANO-F	12.48	0.13	80.00	0.53333	1.49	0.13
SUGANO-WBL	12.48	0.13	80.00	0.53333	1.49	0.13
SUGANO-WCO	12.48	0.13	80.00	0.53333	1.49	0.13
HIGASHI 1-F1	12.00	0.17045	90.00	0.5625	1.49	0.11
HIGASHI 2-PW	12.00	0.17045	90.00	0.5625	1.49	0.11
HIGASHI 5-F2	12.00	0.14286	90.00	0.5625	1.49	0.11
HIGASHI13-FW	12.00	0.14286	90.00	0.5625	1.49	0.11
HIGASHI 4-C3C	12.00	0.17045	90.00	0.5625	1.49	0.11
HIGASHI 6-C2A	12.00	0.14286	90.00	0.5625	1.49	0.11
HIGASHI 7-C2B	12.00	0.14286	90.00	0.5625	1.49	0.11
HIGASHI 9-C40	12.00	0.14286	90.00	0.5625	1.49	0.11
HIGASHI 3-C3	12.00	0.17045	90.00	0.5625	1.49	0.11
HIGASHI 8-C4	12.00	0.14286	90.00	0.5625	1.49	0.11
CORLEY B5	0.00	0	447.04	2.3467	3.67	1.35
CORLEY B6	27.75	0.13432	447.04	2.3467	3.67	0.81
CORLEY B7	35.59	0.076172	447.04	2.3467	3.67	1.35
CORLEY B8	35.59	0.089565	447.04	2.3467	3.67	1.35
CORLEY B9	35.59	0.08521	447.04	2.3467	3.67	1.35
CORLEY B11	0.00	0	447.04	2.3467	3.67	1.35
OGATA K1	7.68	0.097959	150.00	0.9375	0.71	0.96
OGATA K2	7.68	0.097959	150.00	0.9375	1.43	1.44
OGATA K3	7.68	0.097959	150.00	0.9375	2.14	1.92
OGATA K4	7.68	0.090566	150.00	0.9375	1.43	1.44
OGATA K5	7.68	0.090566	150.00	0.9375	1.43	1.44
OGATA K6	7.68	0.090566	150.00	0.9375	2.14	1.92
GAYNOR F	0.00	0	213.36	0.5676	2.22	0.15
GAYNOR W	0.00	0	213.36	0.5676	2.22	0.15
GAYNOR D	0.00	0	213.36	0.5676	2.22	0.15

## APPENDIX B. (Continued)

TEST NAME	X19 (%)	X20 (%)	X21 (TONF/CM2)	X22 (TONF/CM2)	X23 (TONF/CM2)
AOYAMA C2005-I	1.49	0.21	0.236	3.72	231.97
AOYAMA C2005-II	1.49	0.21	0.236	3.08	231.97
AOYAMA C2005-III	1.49	0.21	0.226	3.08	227.00
AOYAMA C2015-A	4.47	0.21	0.223	3.71	225.49
AOYAMA C2015-B	4.47	0.21	0.198	3.71	212.48
AOYAMA C2015-C	4.47	0.21	0.403	3.71	303.13
AOYAMA P2005-A	1.49	0.21	0.22	3.08	223.97
AOYAMA P2015-A	4.47	0.21	0.394	3.71	299.73
AOYAMA C4015	2.06	0.21	0.234	3.62	230.99
AOYAMA P4015	2.06	0.21	0.297	3.62	260.23
AOYAMA M2005	1.49	0.21	0.301	3.68	261.98
AOYAMA CH2015	4.47	0.21	0.289	3.84	256.70
AOYAMA CH2018	5.35	0.21	0.261	3.84	243.95
AOYAMA OLU2015	4.47	0.21	0.223	3.84	225.49
KAHN SP1	3.94	0.07	0.35085	3.5844	282.84
KAHN SP2	3.94	0.07	0.31698	3.5844	268.84
KAHN SP3	3.94	0.07	0.25161	3.5844	239.52
KAHN SP5	3.94	0.07	0.2474	3.5844	237.51
HAYASHI-W1	1.49	0.11	0.183	3.55	204.27
HAYASHI-W2	1.49	0.11	0.183	3.55	204.27
HAYASHI-W4	1.49	0.11	0.183	3.55	204.27
HAYASHI-W5	1.49	0.11	0.185	3.55	205.38
HAYASHI-W6	1.49	0.11	0.185	3.55	205.38
SUGANO-WHA	1.49	0.13	0.24	3.76	233.93
SUGANO-W40S	1.49	0.13	0.24	3.76	233.93
SUGANO-W40W	1.49	0.13	0.24	3.76	233.93
SUGANO-W80S	1.49	0.13	0.24	3.76	233.93
SUGANO-F	1.49	0.13	0.24	3.76	233.93
SUGANO-WBL	1.49	0.13	0.24	3.76	233.93
SUGANO-WCO	1.49	0.13	0.24	3.76	233.93
HIGASHI 1-F1	1.49	0.11	0.176	3.98	200.32
HIGASHI 2-PW	1.49	0.11	0.176	3.98	200.32
HIGASHI 5-F2	1.49	0.11	0.21	3.96	218.82
HIGASHI13-FW	1.49	0.11	0.21	3.96	218.82
HIGASHI 4-C3C	1.49	0.11	0.176	3.98	200.32
HIGASHI 6-C2A	1.49	0.11	0.21	3.96	218.82
HIGASHI 7-C2B	1.49	0.11	0.21	3.96	218.82
HIGASHI 9-C40	1.49	0.11	0.21	3.96	218.82
HIGASHI 3-C3	1.49	0.11	0.176	3.98	200.32
HIGASHI 8-C4	1.49	0.11	0.21	3.96	218.82
CORLEY B5	3.67	1.35	0.46176	4.5262	324.48
CORLEY B6	3.67	0.81	0.22238	4.4911	225.18
CORLEY B7	3.67	1.35	0.50287	4.6668	338.61
CORLEY B8	3.67	1.35	0.42767	4.5614	312.27
CORLEY B9	3.67	1.35	0.44953	4.3786	320.15
CORLEY B11	3.67	1.35	0.54821	4.4419	353.55
OGATA K1	0.71	0.96	0.196	3.995	211.40
OGATA K2	1.43	1.44	0.196	3.995	211.40
OGATA K3	2.14	1.92	0.196	3.995	211.40
OGATA K4	1.43	1.44	0.212	3.995	219.86
OGATA K5	1.43	1.44	0.212	3.995	219.86
OGATA K6	2.14	1.92	0.212	3.995	219.86
GAYNOR F	2.22	0.15	0.292	4.217	258.03
GAYNOR W	2.22	0.15	0.392	4.217	298.96
GAYNOR D	2.22	0.15	0.337	4.217	277.20

## APPENDIX B. (Continued)

TEST NAME	X24 (TONF/CM2)	X25 (CM4)	X26 (TONF/CM)	X27 (CM)	X28 (CM4)	X29 (CM4)
AOYAMA C2005-I	1800.00	8.02E+06	24472.00	10.00	1.29E+07	0
AOYAMA C2005-II	1800.00	8.02E+06	24472.00	10.00	1.29E+07	0
AOYAMA C2005-III	1800.00	8.02E+06	23948.00	10.00	1.29E+07	0
AOYAMA C2015-A	1800.00	8.02E+06	23789.00	10.00	1.29E+07	0
AOYAMA C2015-B	1800.00	8.02E+06	22416.00	10.00	1.29E+07	0
AOYAMA C2015-C	1800.00	8.02E+06	31979.00	10.00	1.29E+07	0
AOYAMA P2005-A	1800.00	8.02E+06	23628.00	10.00	1.29E+07	0
AOYAMA P2015-A	1800.00	8.02E+06	31620.00	10.00	1.29E+07	0
AOYAMA C4015	1800.00	1.62E+07	49273.00	10.00	1.96E+07	0
AOYAMA P4015	1800.00	1.62E+07	55511.00	10.00	1.96E+07	0
AOYAMA M2005	1800.00	8.02E+06	27638.00	10.00	1.29E+07	0
AOYAMA CH2015	1800.00	8.02E+06	27081.00	10.00	1.29E+07	0
AOYAMA CH2018	1800.00	8.02E+06	25736.00	10.00	1.29E+07	0
AOYAMA OLU2015	1800.00	8.02E+06	23789.00	10.00	1.29E+07	2.51E+05
KAHN SP1	1800.00	7.79E+06	7860.00	7.62	1.70E+07	0
KAHN SP2	1800.00	7.79E+06	7471.00	0.00	7.79E+06	0
KAHN SP3	1800.00	7.79E+06	6656.20	7.62	1.70E+07	0
KAHN SP5	1800.00	7.79E+06	6600.30	7.62	1.70E+07	0
HAYASHI-W1	1970.00	6.51E+06	21878.00	0.00	6.51E+06	0
HAYASHI-W2	1970.00	6.51E+06	21878.00	7.50	9.07E+06	0
HAYASHI-W4	1970.00	6.51E+06	21878.00	7.50	9.07E+06	0
HAYASHI-W5	1970.00	6.51E+06	21998.00	7.50	9.07E+06	0
HAYASHI-W6	1970.00	6.51E+06	21998.00	7.50	9.07E+06	0
SUGANO-WHA	1900.00	5.81E+06	31837.00	8.00	8.06E+06	0
SUGANO-W40S	1900.00	5.81E+06	31837.00	4.00	6.93E+06	0
SUGANO-W40W	1900.00	5.81E+06	31837.00	4.00	6.93E+06	0
SUGANO-W80S	1900.00	5.81E+06	31837.00	8.00	8.06E+06	0
SUGANO-F	1900.00	5.81E+06	31837.00	0.00	5.81E+06	0
SUGANO-WBL	1900.00	5.81E+06	31837.00	10.00	8.62E+06	0
SUGANO-WCO	1900.00	5.81E+06	31837.00	8.00	8.06E+06	0
HIGASHI 1-F1	1800.00	6.51E+06	21456.00	0.00	6.51E+06	0
HIGASHI 2-PW	1800.00	6.51E+06	21456.00	7.50	9.07E+06	0
HIGASHI 5-F2	1800.00	6.51E+06	23437.00	0.00	6.51E+06	0
HIGASHI13-FW	1800.00	6.51E+06	23437.00	7.50	9.07E+06	0
HIGASHI 4-C3C	1800.00	6.51E+06	21456.00	7.50	9.07E+06	0
HIGASHI 6-C2A	1800.00	6.51E+06	23437.00	7.50	9.07E+06	2.74E+05
HIGASHI 7-C2B	1800.00	6.51E+06	23437.00	7.50	9.07E+06	1.92E+06
HIGASHI 9-C40	1800.00	6.51E+06	23437.00	7.50	9.07E+06	0
HIGASHI 3-C3	1800.00	6.51E+06	21456.00	7.50	9.07E+06	0
HIGASHI 8-C4	1800.00	6.51E+06	23437.00	7.50	9.07E+06	0
CORLEY B5	1900.00	2.28E+07	994.87	10.20	2.87E+07	0
CORLEY B6	1900.00	2.28E+07	690.41	10.20	2.87E+07	0
CORLEY B7	1900.00	2.28E+07	1038.20	10.20	2.87E+07	0
CORLEY B8	1900.00	2.28E+07	957.45	10.20	2.87E+07	0
CORLEY B9	1900.00	2.28E+07	981.61	10.20	2.87E+07	0
CORLEY B11	1900.00	2.28E+07	1084.00	10.20	2.87E+07	0
OGATA K1	1900.00	6.51E+06	4890.70	8.00	9.24E+06	0
OGATA K2	1900.00	6.51E+06	4890.70	8.00	9.24E+06	0
OGATA K3	1900.00	6.51E+06	4890.70	8.00	9.24E+06	0
OGATA K4	1900.00	6.51E+06	5086.40	8.00	9.24E+06	0
OGATA K5	1900.00	6.51E+06	5086.40	8.00	9.24E+06	0
OGATA K6	1900.00	6.51E+06	5086.40	8.00	9.24E+06	0
GAYNOR F	1800.00	7.69E+07	24501.00	13.34	1.36E+08	0
GAYNOR W	1800.00	7.69E+07	28388.00	13.34	1.36E+08	3.20E+06
GAYNOR D	1800.00	7.69E+07	26321.00	13.34	1.36E+08	1.17E+06

## APPENDIX B. (Continued)

TEST NAME	X30 (CM)	X31 (CM)	X32 (CM)	X33 (CM2)	X34 (CM2)	X35
AOYAMA C2005-I	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA C2005-II	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA C2005-III	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA C2015-A	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA C2015-B	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA C2015-C	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA P2005-A	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA P2015-A	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA C4015	0.00	0.00	0.00	3200.70	0.00	0
AOYAMA P4015	0.00	0.00	0.00	3200.70	0.00	0
AOYAMA M2005	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA CH2015	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA CH2018	0.00	0.00	0.00	2599.60	0.00	0
AOYAMA OLU2015	43.00	40.00	14.00	2599.60	670.00	6.93E-08
KAHN SP1	0.00	0.00	0.00	2321.30	0.00	0
KAHN SP2	0.00	0.00	0.00	464.52	0.00	0
KAHN SP3	0.00	0.00	0.00	2321.30	0.00	0
KAHN SP5	0.00	0.00	0.00	2321.30	0.00	0
HAYASHI-W1	0.00	0.00	0.00	800.00	0.00	0
HAYASHI-W2	0.00	0.00	0.00	2000.00	0.00	0
HAYASHI-W4	0.00	0.00	0.00	2000.00	0.00	0
HAYASHI-W5	0.00	0.00	0.00	2000.00	0.00	0
HAYASHI-W6	0.00	0.00	0.00	2000.00	0.00	0
SUGANO-WHA	0.00	0.00	0.00	2000.00	0.00	0
SUGANO-W40S	0.00	0.00	0.00	1400.00	0.00	0
SUGANO-W40W	0.00	0.00	0.00	1400.00	0.00	0
SUGANO-W80S	0.00	0.00	0.00	2000.00	0.00	0
SUGANO-F	0.00	0.00	0.00	800.00	0.00	0
SUGANO-WBL	0.00	0.00	0.00	2300.00	0.00	0
SUGANO-WCO	0.00	0.00	0.00	2000.00	0.00	0
HIGASHI 1-F1	0.00	0.00	0.00	800.00	0.00	0
HIGASHI 2-PW	0.00	0.00	0.00	2000.00	0.00	0
HIGASHI 5-F2	0.00	0.00	0.00	800.00	0.00	0
HIGASHI13-FW	0.00	0.00	0.00	2000.00	0.00	0
HIGASHI 4-C3C	0.00	0.00	0.00	2000.00	0.00	0
HIGASHI 6-C2A	0.00	90.00	0.00	2000.00	570.00	0
HIGASHI 7-C2B	0.00	90.00	0.00	2000.00	570.00	0
HIGASHI 9-C40	0.00	0.00	0.00	2000.00	0.00	0
HIGASHI 3-C3	0.00	0.00	0.00	2000.00	0.00	0
HIGASHI 8-C4	0.00	0.00	0.00	2000.00	0.00	0
CORLEY B5	0.00	0.00	0.00	3801.10	0.00	0
CORLEY B6	0.00	0.00	0.00	3801.10	0.00	0
CORLEY B7	0.00	0.00	0.00	3801.10	0.00	0
CORLEY B8	0.00	0.00	0.00	3801.10	0.00	0
CORLEY B9	0.00	0.00	0.00	3801.10	0.00	0
CORLEY B11	0.00	0.00	0.00	3801.10	0.00	0
OGATA K1	0.00	0.00	0.00	0.00	0.00	0
OGATA K2	0.00	0.00	0.00	0.00	0.00	0
OGATA K3	0.00	0.00	0.00	0.00	0.00	0
OGATA K4	0.00	0.00	0.00	0.00	0.00	0
OGATA K5	0.00	0.00	0.00	0.00	0.00	0
OGATA K6	0.00	0.00	0.00	0.00	0.00	0
GAYNOR F	0.00	0.00	0.00	6872.80	0.00	0
GAYNOR W	66.04	81.28	66.04	6872.80	1897.50	1.15E-07
GAYNOR D	0.00	142.24	71.12	6872.80	1355.30	1.21E-07

## APPENDIX B. (Continued)

TEST NAME	X36	X37 (%)	X38 (%)	X39 (%)	X40 (TONF/CM2)	X41 (TONF/CM2)
AOYAMA C2005-I	0	0.85	0.85	0	0.21	3.99
AOYAMA C2005-II	0	0.85	0.85	0	0.21	3.99
AOYAMA C2005-III	0	0.85	0.85	0	0.22	3.99
AOYAMA C2015-A	0	0.85	0.85	0	0.15	3.62
AOYAMA C2015-B	0	0.85	0.85	0	0.15	3.62
AOYAMA C2015-C	0	0.85	0.85	0	0.39	3.62
AOYAMA P2005-A	0	0.85	0.85	0	0.22	3.99
AOYAMA P2015-A	0	0.85	0.85	0	0.39	3.62
AOYAMA C4015	0	0.85	0.85	0	0.30	3.62
AOYAMA P4015	0	0.85	0.85	0	0.30	3.62
AOYAMA M2005	0	0.85	0.85	0	0.29	3.99
AOYAMA CH2015	0	0.85	0.85	0	0.22	3.96
AOYAMA CH2018	0	0.85	0.85	0	0.22	3.96
AOYAMA OLU2015	2.67E-07	0.85	0.85	0	0.18	3.96
KAHN SP1	0	0.44	0.46	0	0.35	4.49
KAHN SP2	0	0.00	0.00	0	0.00	0.00
KAHN SP3	0	0.44	0.46	0	0.20	4.49
KAHN SP5	0	0.00	0.00	0	0.20	4.49
HAYASHI-W1	0	0.00	0.00	0	0.00	0.00
HAYASHI-W2	0	0.75	0.75	0	0.18	3.55
HAYASHI-W4	0	0.75	0.75	0	0.27	3.55
HAYASHI-W5	0	0.75	0.75	0	0.31	3.55
HAYASHI-W6	0	0.75	0.75	0	0.31	3.55
SUGANO-WHA	0	0.70	0.70	0	0.38	3.38
SUGANO-W40S	0	0.70	0.70	0	0.38	3.38
SUGANO-W40W	0	0.70	0.70	0	0.38	3.38
SUGANO-W80S	0	0.70	0.70	0	0.38	3.38
SUGANO-F	0	0.00	0.00	0	0.00	0.00
SUGANO-WBL	0	0.70	0.70	0	0.30	3.38
SUGANO-WCO	0	0.70	0.70	0	0.38	3.38
HIGASHI 1-F1	0	0.00	0.00	0	0.00	0.00
HIGASHI 2-PW	0	0.85	0.85	0	0.22	3.43
HIGASHI 5-F2	0	0.00	0.00	0	0.00	0.00
HIGASHI13-FW	0	0.28	0.28	0	0.21	3.76
HIGASHI 4-C3C	0	0.85	0.85	0	0.24	3.43
HIGASHI 6-C2A	7.48E-07	0.85	0.85	0	0.23	3.76
HIGASHI 7-C2B	7.55E-07	0.85	0.85	0	0.23	3.76
HIGASHI 9-C40	0	0.85	0.85	0	0.23	3.76
HIGASHI 3-C3	0	0.85	0.85	0	0.24	3.43
HIGASHI 8-C4	0	0.85	0.85	0	0.23	3.76
CORLEY B5	0	0.63	0.29	0	0.46	4.53
CORLEY B6	0	0.63	0.29	0	0.22	4.49
CORLEY B7	0	0.63	0.29	0	0.50	4.67
CORLEY B8	0	1.38	0.29	0	0.43	4.56
CORLEY B9	0	0.63	0.29	0	0.45	4.38
CORLEY B11	0	0.63	0.29	0	0.55	4.44
OGATA K1	0	0.27	0.27	0	0.20	4.03
OGATA K2	0	0.53	0.53	0	0.20	4.03
OGATA K3	0	0.80	0.80	0	0.20	4.03
OGATA K4	0	0.80	0.80	0	0.21	4.03
OGATA K5	0	0.53	0.53	0	0.21	4.03
OGATA K6	0	0.83	0.83	0	0.21	4.03
GAYNOR F	0	0.32	0.32	0	0.24	4.22
GAYNOR W	1.92E-07	0.32	0.32	0	0.22	4.22
GAYNOR D	3.00E-07	0.32	0.32	0	0.23	4.22

## APPENDIX B. (Continued)

TEST NAME	X42 (CM2)	X43	X44	X45	X46	X47 (CM)
AOYAMA C2005-I	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2005-II	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2005-III	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-B	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-C	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P2005-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P2015-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C4015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P4015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA M2005	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA CH2015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA CH2018	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA OLU2015	2680.00	0.26	0.04	—	0.04	0.00
KAHN SP1	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP2	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP3	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP5	0.00	0.00	0.00	0.00	0.00	7.62
HAYASHI-W1	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W2	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W4	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W5	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W6	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WHA	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W40S	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W40W	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W80S	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-F	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WBL	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WCO	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 1-F1	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 2-PW	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 5-F2	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI13-FW	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 4-C3C	0.00	0.00	0.00	0.00	0.00	7.50
HIGASHI 6-C2A	6612.00	0.00	0.00	0.00	0.00	7.50
HIGASHI 7-C2B	6612.00	0.00	0.00	0.00	0.00	7.50
HIGASHI 9-C40	0.00	0.00	0.00	0.00	0.00	7.50
HIGASHI 3-C3	0.00	0.00	0.00	0.00	0.00	7.50
HIGASHI 8-C4	0.00	0.00	0.00	0.00	0.00	7.50
CORLEY B5	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B6	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B7	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B8	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B9	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B11	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K1	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K2	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K3	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K4	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K5	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K6	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR F	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR W	11561.00	0.14	0.14	0.14	0.14	0.00
GAYNOR D	14452.00	0.09	0.27	0.09	0.27	0.00

## APPENDIX B. (Continued)

TEST NAME	X48 (CM)	X49	X50 (%)	X51 (%)	X52 (%)	X53
AOYAMA C2005-I	0.00	0.00	0	0	0	0
AOYAMA C2005-II	0.00	0.00	0	0	0	0
AOYAMA C2005-III	0.00	0.00	0	0	0	0
AOYAMA C2015-A	0.00	0.00	0	0	0	0
AOYAMA C2015-B	0.00	0.00	0	0	0	0
AOYAMA C2015-C	0.00	0.00	0	0	0	0
AOYAMA P2005-A	0.00	0.00	0	0	0	0
AOYAMA P2015-A	0.00	0.00	0	0	0	0
AOYAMA C4015	0.00	0.00	0	0	0	0
AOYAMA P4015	0.00	0.00	0	0	0	0
AOYAMA M2005	0.00	0.00	0	0	0	0
AOYAMA CH2015	0.00	0.00	0	0	0	0
AOYAMA CH2018	0.00	0.00	0	0	0	0
AOYAMA OLU2015	0.00	0.00	0	0	0	0
KAHN SP1	0.00	0.00	0	0	0	0
KAHN SP2	0.00	0.00	0	0	0	0
KAHN SP3	0.00	0.00	0	0	0	0
KAHN SP5	40.32	1.00	0.678	0.458	0	0
HAYASHI-W1	0.00	0.00	0	0	0	0
HAYASHI-W2	0.00	0.00	0	0	0	0
HAYASHI-W4	0.00	0.00	0	0	0	0
HAYASHI-W5	0.00	0.00	0	0	0	0
HAYASHI-W6	0.00	0.00	0	0	0	0
SUGANO-WHA	0.00	0.00	0	0	0	0
SUGANO-W40S	0.00	0.00	0	0	0	0
SUGANO-W40W	0.00	0.00	0	0	0	0
SUGANO-W80S	0.00	0.00	0	0	0	0
SUGANO-F	0.00	0.00	0	0	0	0
SUGANO-WBL	0.00	0.00	0	0	0	0
SUGANO-WCO	0.00	0.00	0	0	0	0
HIGASHI 1-F1	0.00	0.00	0	0	0	0
HIGASHI 2-PW	0.00	0.00	0	0	0	0
HIGASHI 5-F2	0.00	0.00	0	0	0	0
HIGASHI13-FW	0.00	0.00	0	0	0	0
HIGASHI 4-C3C	51.00	1.00	0.8453	0.8453	0	0
HIGASHI 6-C2A	38.00	2.00	0.8453	0.8453	0	0.475
HIGASHI 7-C2B	38.00	2.00	0.8453	0.8453	0	0.475
HIGASHI 9-C40	38.00	1.00	0.8453	0.8453	0	0
HIGASHI 3-C3	51.00	1.00	0.8453	0.8453	0	0
HIGASHI 8-C4	38.00	1.00	0.8453	0.8453	0	0
CORLEY B5	0.00	0.00	0	0	0	0
CORLEY B6	0.00	0.00	0	0	0	0
CORLEY B7	0.00	0.00	0	0	0	0
CORLEY B8	0.00	0.00	0	0	0	0
CORLEY B9	0.00	0.00	0	0	0	0
CORLEY B11	0.00	0.00	0	0	0	0
OGATA K1	0.00	0.00	0	0	0	0
OGATA K2	0.00	0.00	0	0	0	0
OGATA K3	0.00	0.00	0	0	0	0
OGATA K4	0.00	0.00	0	0	0	0
OGATA K5	0.00	0.00	0	0	0	0
OGATA K6	0.00	0.00	0	0	0	0
GAYNOR F	0.00	0.00	0	0	0	0
GAYNOR W	0.00	0.00	0	0	0	0
GAYNOR D	0.00	0.00	0	0	0	0

## APPENDIX B. (Continued)

TEST NAME	X54	X55	X56	X57 (CM2)	X58 (CM)	X59 (CM)
AOYAMA C2005-I	0	0	0	15.69	7.50	10.00
AOYAMA C2005-II	0	0	0	15.69	7.50	10.00
AOYAMA C2005-III	0	0	0	15.69	7.50	10.00
AOYAMA C2015-A	0	0	0	15.69	7.50	10.00
AOYAMA C2015-B	0	0	0	15.69	7.50	10.00
AOYAMA C2015-C	0	0	0	15.69	7.50	10.00
AOYAMA P2005-A	0	0	0	0.00	0.00	0.00
AOYAMA P2015-A	0	0	0	0.00	0.00	0.00
AOYAMA C4015	0	0	0	14.26	7.50	10.00
AOYAMA P4015	0	0	0	0.00	0.00	0.00
AOYAMA M2005	0	0	0	15.69	7.50	10.00
AOYAMA CH2015	0	0	0	15.69	7.50	10.00
AOYAMA CH2018	0	0	0	15.69	7.50	10.00
AOYAMA OLU2015	0	0	0	15.69	7.50	10.00
KAHN SP1	0	0	0	0.00	0.00	0.00
KAHN SP2	0	0	0	0.00	0.00	0.00
KAHN SP3	0	0	0	8.52	21.27	9.53
KAHN SP5	0	0	0	47.50	9.84	9.53
HAYASHI-W1	0	0	0	0.00	0.00	0.00
HAYASHI-W2	0	0	0	0.00	0.00	0.00
HAYASHI-W4	0	0	0	9.54	10.00	4.00
HAYASHI-W5	0	0	0	9.54	10.00	4.00
HAYASHI-W6	0	0	0	9.54	10.00	4.00
SUGANO-WHA	0	0	0	12.57	10.00	10.00
SUGANO-W40S	0	0	0	0.00	0.00	0.00
SUGANO-W40W	0	0	0	0.00	0.00	0.00
SUGANO-W80S	0	0	0	0.00	0.00	0.00
SUGANO-F	0	0	0	0.00	0.00	0.00
SUGANO-WBL	0	0	0	6.28	20.00	10.00
SUGANO-WCO	0	0	0	8.64	15.00	10.00
HIGASHI 1-F1	0	0	0	0.00	0.00	0.00
HIGASHI 2-PW	0	0	0	9.12	12.00	4.00
HIGASHI 5-F2	0	0	0	0.00	0.00	0.00
HIGASHI13-FW	0	0	0	0.00	0.00	0.00
HIGASHI 4-C3C	0	0	0	12.06	14.00	4.00
HIGASHI 6-C2A	0.475	0.475	0.475	8.04	14.00	4.00
HIGASHI 7-C2B	0.475	0.475	0.475	8.04	14.00	4.00
HIGASHI 9-C40	0	0	0	21.63	10.00	4.00
HIGASHI 3-C3	0	0	0	21.63	10.00	4.00
HIGASHI 8-C4	0	0	0	20.36	10.00	4.00
CORLEY B5	0	0	0	0.00	0.00	0.00
CORLEY B6	0	0	0	0.00	0.00	0.00
CORLEY B7	0	0	0	0.00	0.00	0.00
CORLEY B8	0	0	0	0.00	0.00	0.00
CORLEY B9	0	0	0	0.00	0.00	0.00
CORLEY B11	0	0	0	0.00	0.00	0.00
OGATA K1	0	0	0	0.00	0.00	0.00
OGATA K2	0	0	0	0.00	0.00	0.00
OGATA K3	0	0	0	0.00	0.00	0.00
OGATA K4	0	0	0	0.00	0.00	0.00
OGATA K5	0	0	0	0.00	0.00	0.00
OGATA K6	0	0	0	0.00	0.00	0.00
GAYNOR F	0	0	0	34.06	30.48	22.86
GAYNOR W	0	0	0	34.06	30.48	22.86
GAYNOR D	0	0	0	34.06	30.48	22.86

## APPENDIX B. (Continued)

TEST NAME	X60 (TONF/CM2)	X61 (TONF)	X62 (CM2)	X63 (CM)	X64 (CM)	X65 (TONF/CM2)
AOYAMA C2005-I	3.53	55.37	15.69	7.50	10.00	3.53
AOYAMA C2005-II	3.53	55.37	15.69	7.50	10.00	3.53
AOYAMA C2005-III	3.53	55.37	15.69	7.50	9.00	3.53
AOYAMA C2015-A	3.53	55.37	15.69	7.50	10.00	3.53
AOYAMA C2015-B	3.53	55.37	15.69	7.50	10.00	3.53
AOYAMA C2015-C	3.53	55.37	15.69	7.50	10.00	3.53
AOYAMA P2005-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P2015-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C4015	3.53	50.34	14.26	7.50	10.00	3.53
AOYAMA P4015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA M2005	3.53	55.37	15.69	7.50	10.00	3.53
AOYAMA CH2015	3.88	60.86	15.69	7.50	10.00	3.88
AOYAMA CH2018	3.88	60.86	15.69	7.50	10.00	3.88
AOYAMA OLU2015	3.88	60.86	15.69	7.50	10.00	3.88
KAHN SP1	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP2	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP3	4.49	38.25	8.52	21.27	9.53	4.49
KAHN SP5	4.49	213.35	47.50	9.84	9.53	4.49
HAYASHI-W1	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W2	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W4	2.79	26.62	9.54	10.00	4.00	2.79
HAYASHI-W5	2.79	26.62	9.54	10.00	4.00	2.79
HAYASHI-W6	2.79	26.62	9.54	10.00	4.00	2.79
SUGANO-WHA	7.18	90.22	12.57	10.00	10.00	7.18
SUGANO-W40S	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W40W	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W80S	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-F	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WBL	7.18	45.11	6.28	20.00	10.00	7.18
SUGANO-WCO	7.18	62.03	8.64	15.00	10.00	7.18
HIGASHI 1-F1	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 2-PW	2.79	25.44	9.12	12.00	4.00	2.79
HIGASHI 5-F2	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI13-FW	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 4-C3C	2.79	33.66	12.06	14.00	4.00	2.79
HIGASHI 6-C2A	2.79	22.44	8.04	14.00	4.00	2.79
HIGASHI 7-C2B	2.79	22.44	8.04	14.00	4.00	2.79
HIGASHI 9-C40	2.79	60.35	21.63	10.00	4.00	2.79
HIGASHI 3-C3	2.79	60.35	21.63	10.00	4.00	2.79
HIGASHI 8-C4	2.79	56.80	20.36	10.00	4.00	2.79
CORLEY B5	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B6	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B7	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B8	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B9	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B11	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K1	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K2	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K3	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K4	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K5	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K6	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR F	4.22	143.65	34.06	30.48	22.86	4.22
GAYNOR W	4.22	143.65	34.06	30.48	22.86	4.22
GAYNOR D	4.22	143.65	34.06	30.48	22.86	4.22

## APPENDIX B. (Continued)

TEST NAME	X66 (TONF)	X67 (CM2)	X68 (CM)	X69 (CM)	X70 (TONF/CM2)	X71 (TONF)
AOYAMA C2005-I	55.37	7.84	7.50	10.00	3.53	27.69
AOYAMA C2005-II	55.37	7.84	7.50	10.00	3.53	27.69
AOYAMA C2005-III	55.37	7.84	7.50	9.00	3.53	27.69
AOYAMA C2015-A	55.37	7.84	7.50	10.00	3.53	27.69
AOYAMA C2015-B	55.37	7.84	7.50	10.00	3.53	27.69
AOYAMA C2015-C	55.37	7.84	7.50	10.00	3.53	27.69
AOYAMA P2005-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P2015-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C4015	50.34	7.84	7.50	10.00	3.53	27.69
AOYAMA P4015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA M2005	55.37	7.84	7.50	10.00	3.53	27.69
AOYAMA CH2015	60.86	7.84	7.50	10.00	3.88	30.43
AOYAMA CH2018	60.86	7.84	7.50	10.00	3.88	30.43
AOYAMA OLU2015	60.86	7.84	7.50	10.00	3.88	30.43
KAHN SP1	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP2	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP3	38.25	4.97	22.86	9.53	4.49	22.31
KAHN SP5	213.35	0.00	0.00	0.00	0.00	0.00
HAYASHI-W1	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W2	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W4	26.62	5.09	10.00	4.00	2.79	14.20
HAYASHI-W5	26.62	5.09	10.00	4.00	2.79	14.20
HAYASHI-W6	26.62	5.09	10.00	4.00	2.79	14.20
SUGANO-WHA	90.22	7.07	10.00	10.00	7.18	50.75
SUGANO-W40S	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W40W	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W80S	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-F	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WBL	45.11	0.00	0.00	0.00	0.00	0.00
SUGANO-WCO	62.03	4.71	15.00	10.00	7.18	33.84
HIGASHI 1-F1	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 2-PW	25.44	0.00	0.00	0.00	0.00	0.00
HIGASHI 5-F2	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI13-FW	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 4-C3C	33.66	0.00	0.00	0.00	0.00	0.00
HIGASHI 6-C2A	22.44	0.00	0.00	0.00	0.00	0.00
HIGASHI 7-C2B	22.44	0.00	0.00	0.00	0.00	0.00
HIGASHI 9-C40	60.35	0.00	0.00	0.00	0.00	0.00
HIGASHI 3-C3	60.35	0.00	0.00	0.00	0.00	0.00
HIGASHI 8-C4	56.80	0.00	0.00	0.00	0.00	0.00
CORLEY B5	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B6	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B7	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B8	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B9	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B11	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K1	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K2	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K3	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K4	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K5	0.00	0.00	0.00	0.00	0.00	0.00
OGATA K6	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR F	143.65	19.87	30.48	22.86	4.22	83.80
GAYNOR W	143.65	19.87	30.48	22.86	4.22	83.80
GAYNOR D	143.65	19.87	30.48	22.86	4.22	83.80

## APPENDIX B. (Continued)

TEST NAME	X72 (CM2)	X73 (CM)	X74 (CM)	X75 (TONF/CM2)	X76 (TONF)	X77	
AOYAMA C2005-I	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA C2005-II	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA C2005-III	7.84	7.50	9.00	3.53	27.69	0.00	
AOYAMA C2015-A	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA C2015-B	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA C2015-C	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA P2005-A	0.00	0.00	0.00	0.00	0.00	26693.00	
AOYAMA P2015-A	0.00	0.00	0.00	0.00	0.00	35722.00	
AOYAMA C4015	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA P4015	0.00	0.00	0.00	0.00	0.00	27585.00	
AOYAMA M2005	7.84	7.50	10.00	3.53	27.69	0.00	
AOYAMA CH2015	7.84	7.50	10.00	3.88	30.43	0.00	
AOYAMA CH2018	7.84	7.50	10.00	3.88	30.43	0.00	
AOYAMA OLU2015	7.84	7.50	10.00	—	3.88	30.43	0.00
KAHN SP1	0.00	0.00	0.00	0.00	0.00	34780.00	
KAHN SP2	0.00	0.00	0.00	0.00	0.00	0.00	
KAHN SP3	4.97	22.86	9.53	4.49	22.31	0.00	
KAHN SP5	0.00	0.00	0.00	0.00	0.00	0.00	
HAYASHI-W1	0.00	0.00	0.00	0.00	0.00	0.00	
HAYASHI-W2	0.00	0.00	0.00	0.00	0.00	16233.00	
HAYASHI-W4	5.09	10.00	4.00	2.79	14.20	0.00	
HAYASHI-W5	5.09	10.00	4.00	2.79	14.20	0.00	
HAYASHI-W6	5.09	10.00	4.00	2.79	14.20	0.00	
SUGANO-WHA	7.07	10.00	10.00	7.18	50.75	0.00	
SUGANO-W40S	0.00	0.00	0.00	0.00	0.00	9295.20	
SUGANO-W40W	0.00	0.00	0.00	0.00	0.00	9295.20	
SUGANO-W80S	0.00	0.00	0.00	0.00	0.00	18590.00	
SUGANO-F	0.00	0.00	0.00	0.00	0.00	0.00	
SUGANO-WBL	0.00	0.00	0.00	0.00	0.00	0.00	
SUGANO-WCO	4.71	15.00	10.00	7.18	33.84	0.00	
HIGASHI 1-F1	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 2-PW	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 5-F2	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI13-FW	0.00	0.00	0.00	0.00	0.00	17389.00	
HIGASHI 4-C3C	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 6-C2A	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 7-C2B	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 9-C40	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 3-C3	0.00	0.00	0.00	0.00	0.00	0.00	
HIGASHI 8-C4	0.00	0.00	0.00	0.00	0.00	0.00	
CORLEY B5	0.00	0.00	0.00	0.00	0.00	41754.00	
CORLEY B6	0.00	0.00	0.00	0.00	0.00	28976.00	
CORLEY B7	0.00	0.00	0.00	0.00	0.00	43573.00	
CORLEY B8	0.00	0.00	0.00	0.00	0.00	40183.00	
CORLEY B9	0.00	0.00	0.00	0.00	0.00	41197.00	
CORLEY B11	0.00	0.00	0.00	0.00	0.00	45495.00	
OGATA K1	0.00	0.00	0.00	0.00	0.00	17920.00	
OGATA K2	0.00	0.00	0.00	0.00	0.00	17920.00	
OGATA K3	0.00	0.00	0.00	0.00	0.00	17920.00	
OGATA K4	0.00	0.00	0.00	0.00	0.00	18637.00	
OGATA K5	0.00	0.00	0.00	0.00	0.00	18637.00	
OGATA K6	0.00	0.00	0.00	0.00	0.00	18637.00	
GAYNOR F	19.87	30.48	22.86	4.22	83.80	0.00	
GAYNOR W	19.87	30.48	22.86	4.22	83.80	0.00	
GAYNOR D	19.87	30.48	22.86	4.22	83.80	0.00	

## APPENDIX B. (Continued)

TEST NAME	X78 (CM2)	X79 (CM)	X80 (TONF/CM2)	X81 (TONF)	X82 (CM2)	X83 (CM)
AOYAMA C2005-I	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2005-II	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2005-III	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-B	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-C	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P2005-A	14.58	7.50	3.99	58.18	14.58	7.50
AOYAMA P2015-A	14.58	7.50	3.62	52.79	14.58	7.50
AOYAMA C4015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P4015	13.31	7.50	3.62	48.20	13.31	7.50
AOYAMA M2005	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA CH2015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA CH2018	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA OLU2015	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP1	7.81	21.27	4.49	35.06	7.81	21.27
KAHN SP2	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP3	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP5	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W1	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W2	9.00	6.00	3.55	31.95	9.00	6.00
HAYASHI-W4	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W5	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W6	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WHA	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W40S	4.20	10.00	3.38	14.20	4.20	10.00
SUGANO-W40W	4.20	10.00	3.38	14.20	4.20	10.00
SUGANO-W80S	8.40	10.00	3.38	28.39	8.40	10.00
SUGANO-F	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WBL	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WCO	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 1-F1	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 2-PW	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 5-F2	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI13-FW	3.49	15.00	3.96	13.81	3.49	15.00
HIGASHI 4-C3C	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 6-C2A	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 7-C2B	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 9-C40	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 3-C3	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 8-C4	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B5	5.60	20.00	4.53	25.35	5.60	20.00
CORLEY B6	5.60	20.00	4.49	25.15	5.60	20.00
CORLEY B7	5.60	20.00	4.67	26.13	5.60	20.00
CORLEY B8	5.60	20.00	4.56	25.54	5.60	20.00
CORLEY B9	5.60	20.00	4.38	24.52	5.60	20.00
CORLEY B11	5.60	20.00	4.44	24.88	5.60	20.00
OGATA K1	3.49	15.00	4.03	14.06	3.49	15.00
OGATA K2	6.97	15.00	4.03	28.12	6.97	15.00
OGATA K3	10.78	10.00	4.03	43.46	10.78	10.00
OGATA K4	10.78	10.00	4.03	43.46	10.78	10.00
OGATA K5	3.49	15.00	4.03	14.06	3.49	15.00
OGATA K6	5.39	15.00	4.03	21.73	5.39	15.00
GAYNOR F	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR W	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR D	0.00	0.00	0.00	0.00	0.00	0.00

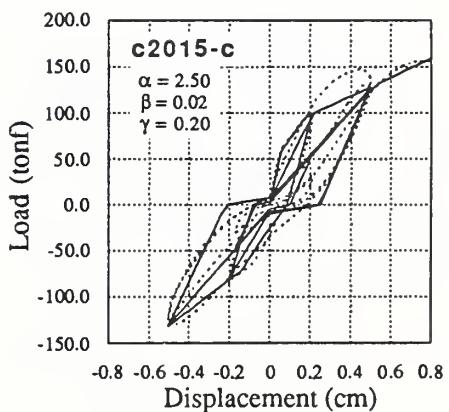
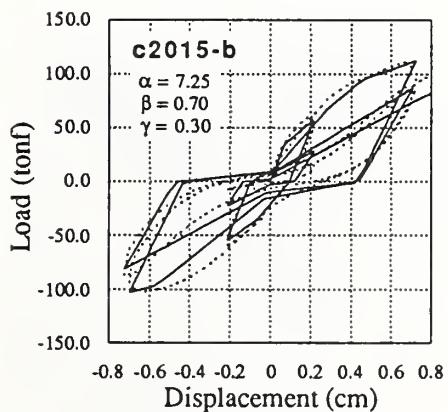
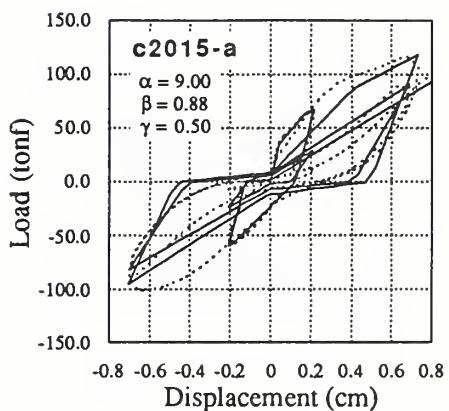
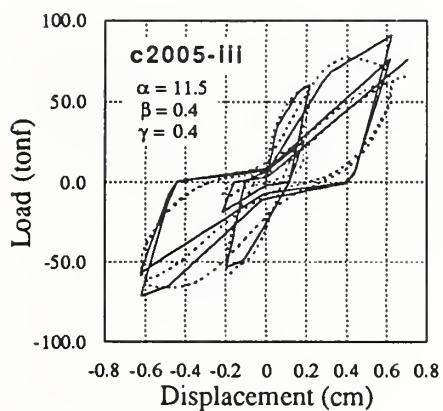
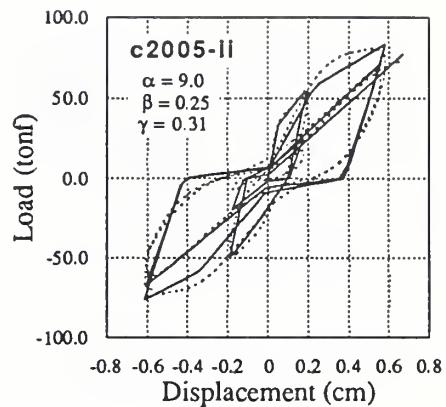
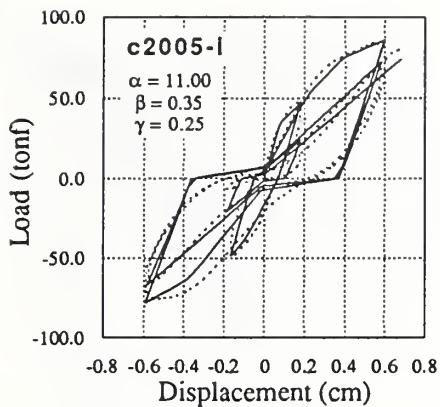
## APPENDIX B. (Continued)

TEST NAME	X84 (TONF/CM2)	X85 (TONF)	X86 (CM2)	X87 (CM)	X88 (TONF/CM2)	X89 (TONF)
AOYAMA C2005-I	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2005-II	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2005-III	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-A	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-B	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA C2015-C	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P2005-A	3.99	58.18	7.61	7.50	3.99	30.36
AOYAMA P2015-A	3.62	52.79	7.61	7.50	3.62	27.54
AOYAMA C4015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA P4015	3.62	48.20	7.61	7.50	3.62	27.54
AOYAMA M2005	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA CH2015	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA CH2018	0.00	0.00	0.00	0.00	0.00	0.00
AOYAMA OLU2015	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP1	4.49	35.06	4.26	22.86	4.49	19.12
KAHN SP2	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP3	0.00	0.00	0.00	0.00	0.00	0.00
KAHN SP5	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W1	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W2	3.55	31.95	5.06	6.00	3.55	17.97
HAYASHI-W4	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W5	0.00	0.00	0.00	0.00	0.00	0.00
HAYASHI-W6	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WHA	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-W40S	3.38	14.20	2.24	10.00	3.38	7.57
SUGANO-W40W	3.38	14.20	2.24	10.00	3.38	7.57
SUGANO-W80S	3.38	28.39	4.48	10.00	3.38	15.14
SUGANO-F	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WBL	0.00	0.00	0.00	0.00	0.00	0.00
SUGANO-WCO	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 1-F1	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 2-PW	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 5-F2	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI13-FW	3.96	13.81	2.22	15.00	3.96	8.79
HIGASHI 4-C3C	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 6-C2A	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 7-C2B	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 9-C40	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 3-C3	0.00	0.00	0.00	0.00	0.00	0.00
HIGASHI 8-C4	0.00	0.00	0.00	0.00	0.00	0.00
CORLEY B5	4.53	25.35	25.47	10.16	4.53	115.28
CORLEY B6	4.49	25.15	25.47	10.16	4.49	114.39
CORLEY B7	4.67	26.13	25.47	10.16	4.67	118.86
CORLEY B8	4.56	25.54	25.47	10.16	4.56	116.18
CORLEY B9	4.38	24.52	25.47	10.16	4.38	111.52
CORLEY B11	4.44	24.88	25.47	10.16	4.44	113.14
OGATA K1	4.03	14.06	3.49	15.00	4.03	14.06
OGATA K2	4.03	28.12	6.97	15.00	4.03	28.12
OGATA K3	4.03	43.46	10.78	10.00	4.03	43.46
OGATA K4	4.03	43.46	10.78	10.00	4.03	43.46
OGATA K5	4.03	14.06	3.49	15.00	4.03	14.06
OGATA K6	4.03	21.73	5.39	15.00	4.03	21.73
GAYNOR F	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR W	0.00	0.00	0.00	0.00	0.00	0.00
GAYNOR D	0.00	0.00	0.00	0.00	0.00	0.00

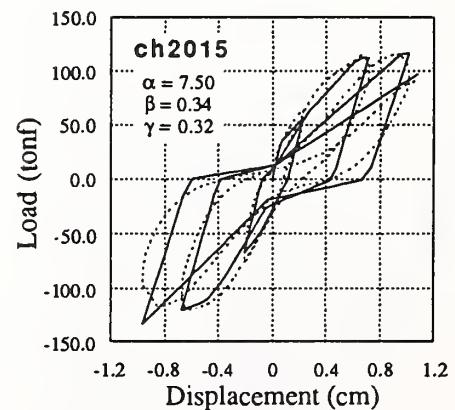
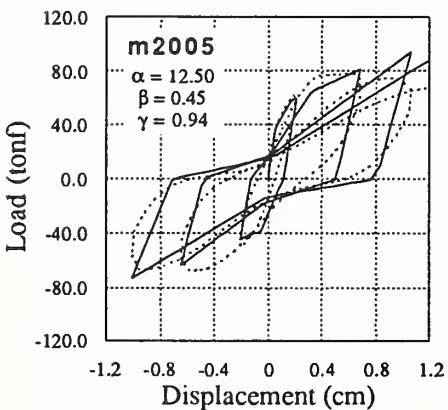
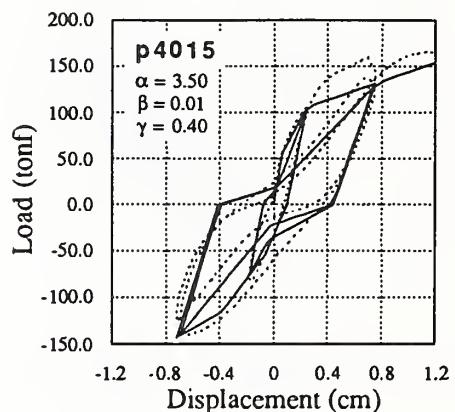
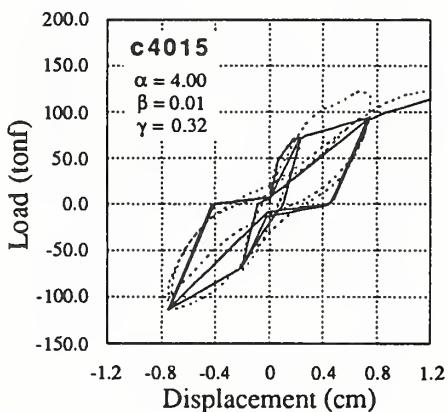
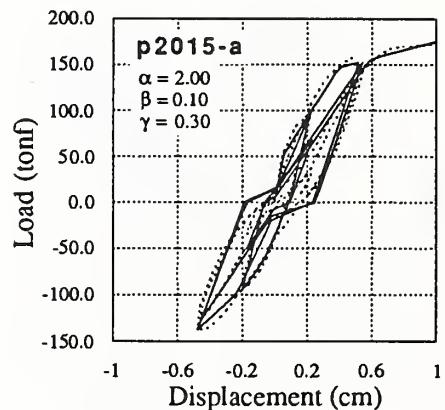
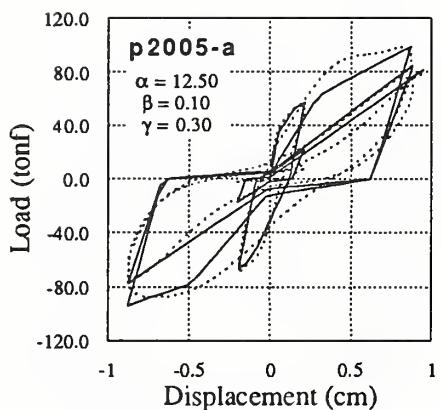
## APPENDIX B. (Continued)

TEST NAME	X90 (CM2)	X91 (CM)	X92 (TONF/CM2)	X93 (TONF)
AOYAMA C2005-I	0.00	0.00	0.00	0.00
AOYAMA C2005-II	0.00	0.00	0.00	0.00
AOYAMA C2005-III	0.00	0.00	0.00	0.00
AOYAMA C2015-A	0.00	0.00	0.00	0.00
AOYAMA C2015-B	0.00	0.00	0.00	0.00
AOYAMA C2015-C	0.00	0.00	0.00	0.00
AOYAMA P2005-A	7.61	7.50	3.99	30.36
AOYAMA P2015-A	7.61	7.50	3.62	27.54
AOYAMA C4015	0.00	0.00	0.00	0.00
AOYAMA P4015	7.61	7.50	3.62	27.54
AOYAMA M2005	0.00	0.00	0.00	0.00
AOYAMA CH2015	0.00	0.00	0.00	0.00
AOYAMA CH2018	0.00	0.00	0.00	0.00
AOYAMA OLU2015	0.00	0.00	0.00	0.00
KAHN SP1	4.26	22.86	4.49	19.12
KAHN SP2	0.00	0.00	0.00	0.00
KAHN SP3	0.00	0.00	0.00	0.00
KAHN SP5	0.00	0.00	0.00	0.00
HAYASHI-W1	0.00	0.00	0.00	0.00
HAYASHI-W2	5.06	6.00	3.55	17.97
HAYASHI-W4	0.00	0.00	0.00	0.00
HAYASHI-W5	0.00	0.00	0.00	0.00
HAYASHI-W6	0.00	0.00	0.00	0.00
SUGANO-WHA	0.00	0.00	0.00	0.00
SUGANO-W40S	2.24	10.00	3.38	7.57
SUGANO-W40W	2.24	10.00	3.38	7.57
SUGANO-W80S	4.48	10.00	3.38	15.14
SUGANO-F	0.00	0.00	0.00	0.00
SUGANO-WBL	0.00	0.00	0.00	0.00
SUGANO-WCO	0.00	0.00	0.00	0.00
HIGASHI 1-F1	0.00	0.00	0.00	0.00
HIGASHI 2-PW	0.00	0.00	0.00	0.00
HIGASHI 5-F2	0.00	0.00	0.00	0.00
HIGASHI13-FW	2.22	15.00	3.96	8.79
HIGASHI 4-C3C	0.00	0.00	0.00	0.00
HIGASHI 6-C2A	0.00	0.00	0.00	0.00
HIGASHI 7-C2B	0.00	0.00	0.00	0.00
HIGASHI 9-C40	0.00	0.00	0.00	0.00
HIGASHI 3-C3	0.00	0.00	0.00	0.00
HIGASHI 8-C4	0.00	0.00	0.00	0.00
CORLEY B5	25.47	10.16	4.53	115.28
CORLEY B6	25.47	10.16	4.49	114.39
CORLEY B7	25.47	10.16	4.67	118.86
CORLEY B8	25.47	10.16	4.56	116.18
CORLEY B9	25.47	10.16	4.38	111.52
CORLEY B11	25.47	10.16	4.44	113.14
OGATA K1	3.49	15.00	4.03	14.06
OGATA K2	6.97	15.00	4.03	28.12
OGATA K3	10.78	10.00	4.03	43.46
OGATA K4	10.78	10.00	4.03	43.46
OGATA K5	3.49	15.00	4.03	14.06
OGATA K6	5.39	15.00	4.03	21.73
GAYNOR F	0.00	0.00	0.00	0.00
GAYNOR W	0.00	0.00	0.00	0.00
GAYNOR D	0.00	0.00	0.00	0.00

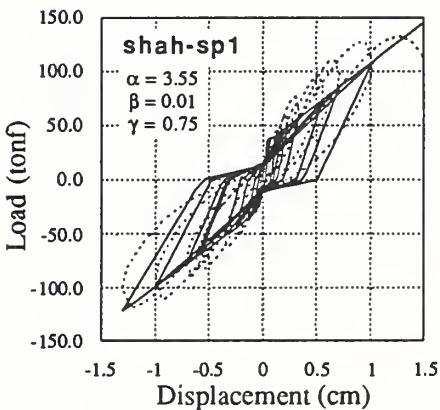
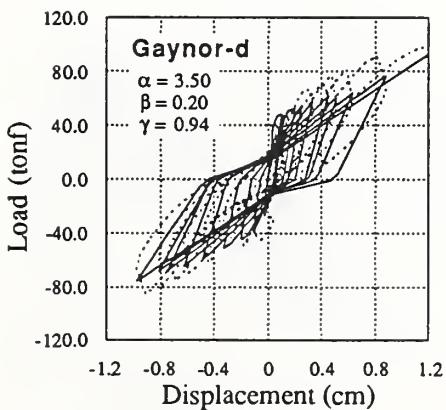
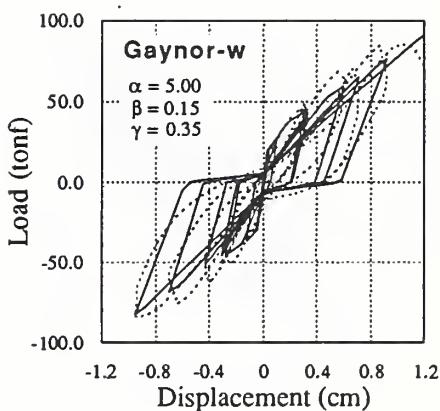
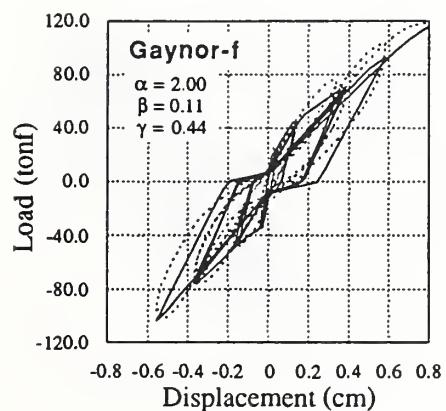
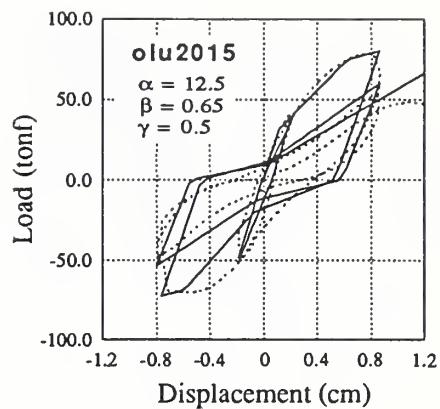
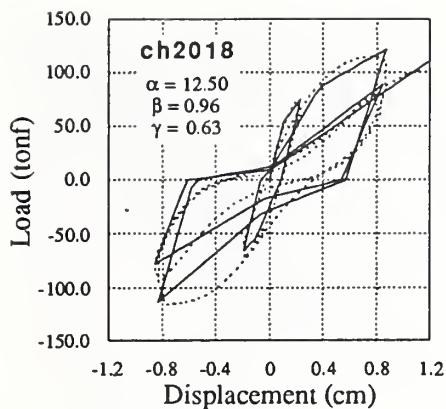
## APPENDIX C. Test Results and System Identification



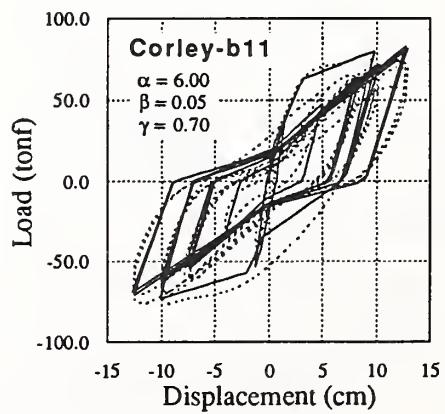
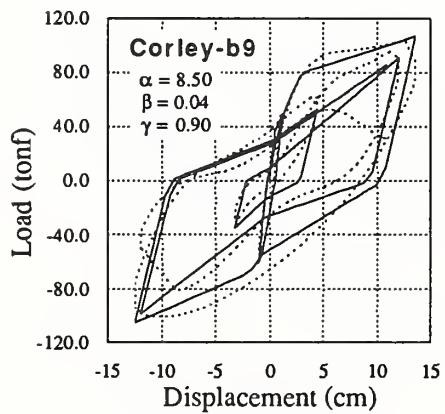
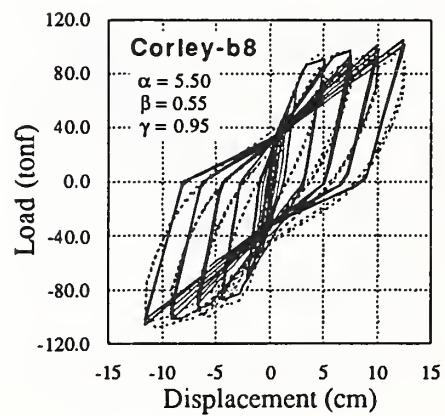
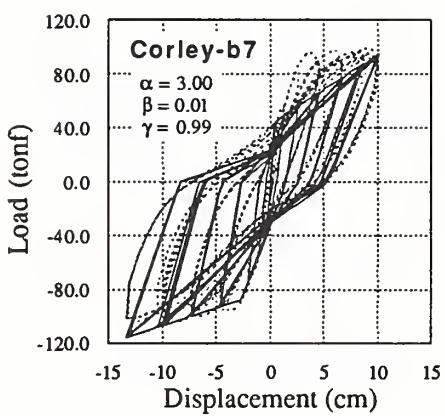
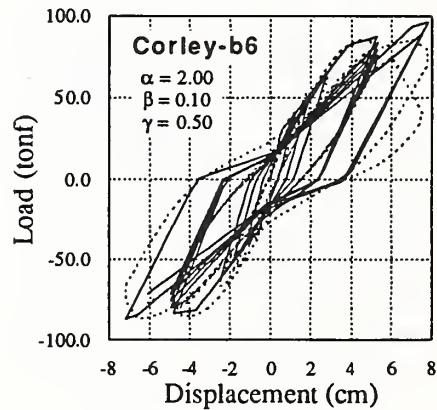
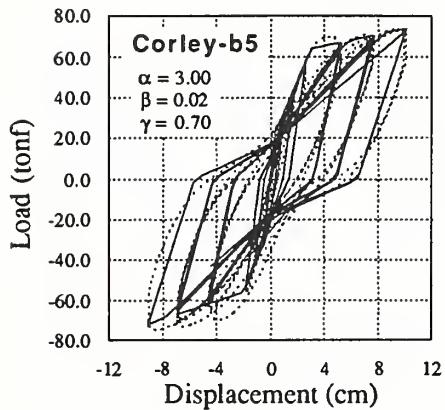
## APPENDIX C. (Continued)



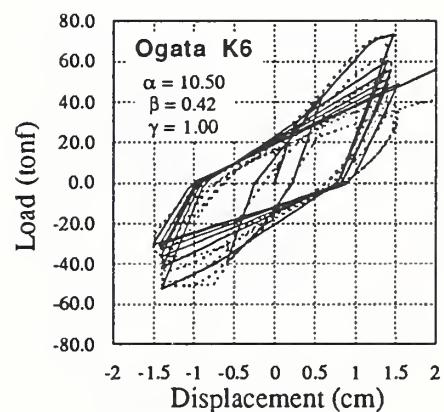
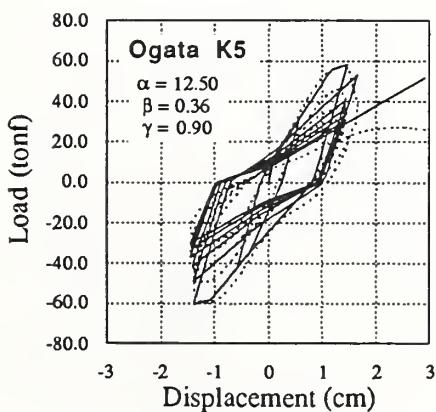
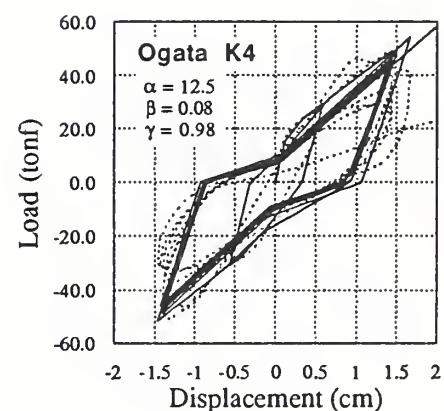
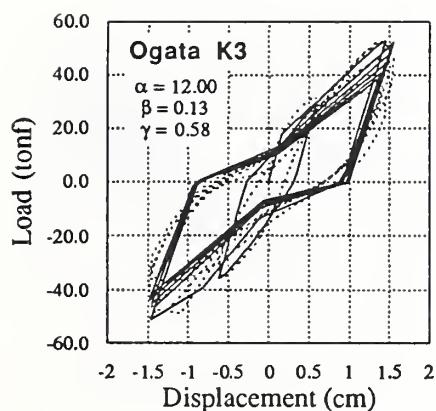
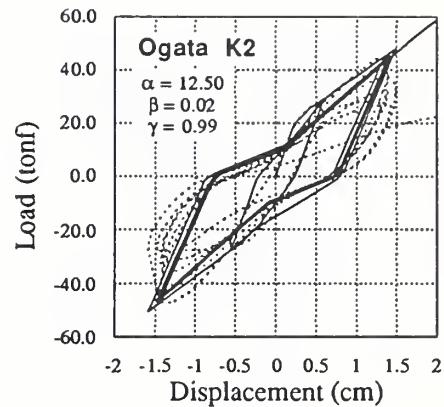
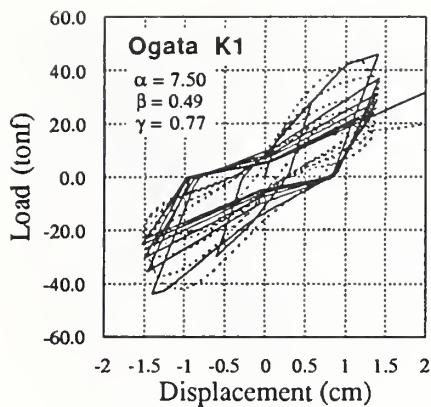
## APPENDIX C. (Continued)



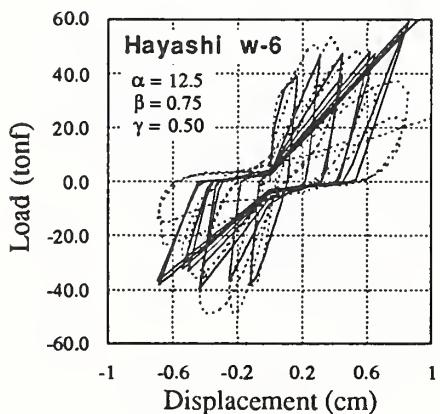
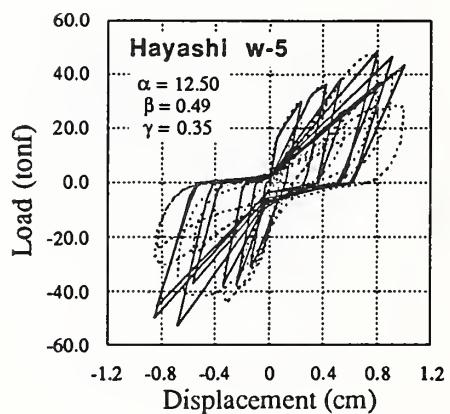
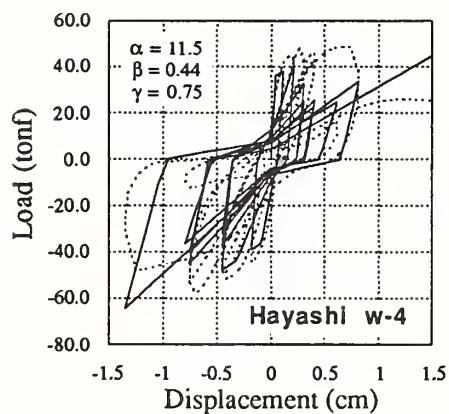
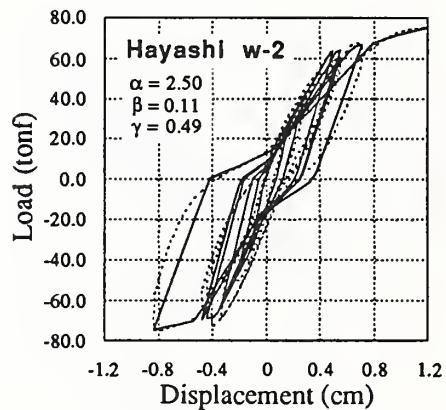
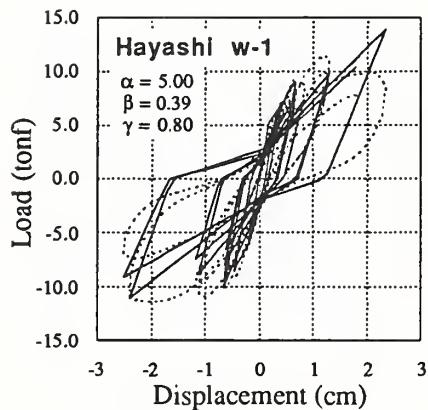
## APPENDIX C. (Continued)



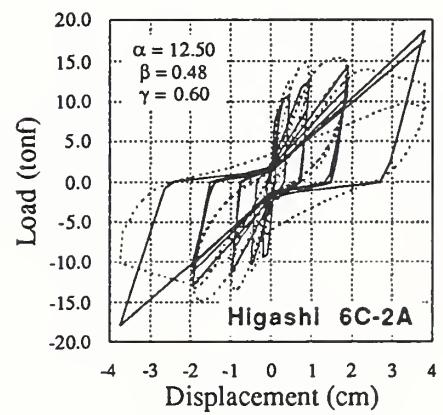
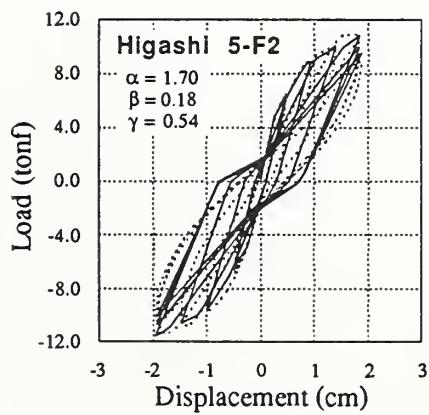
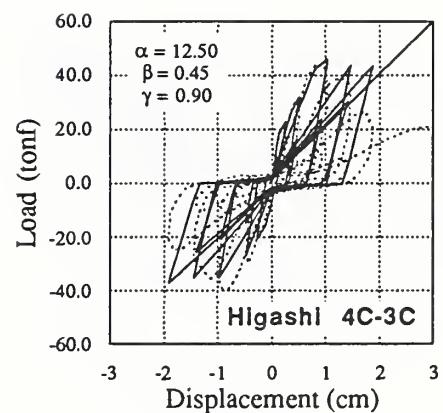
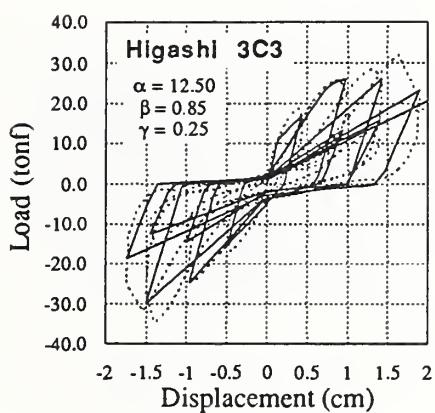
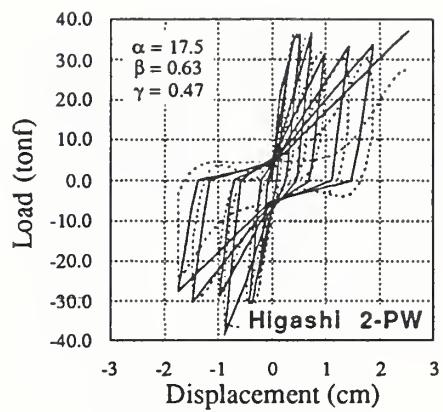
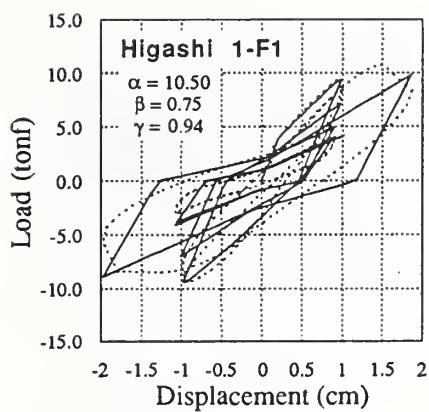
## APPENDIX C. (Continued)



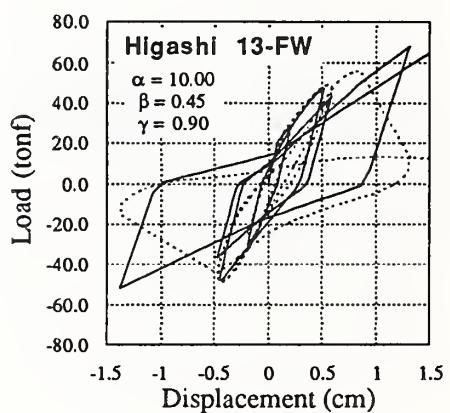
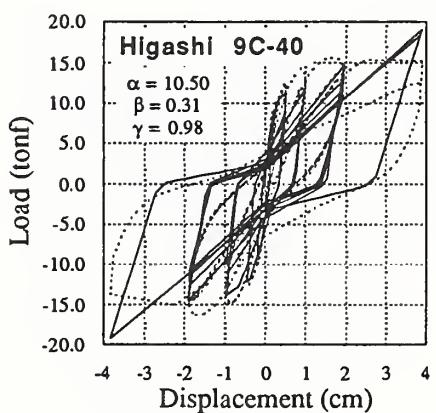
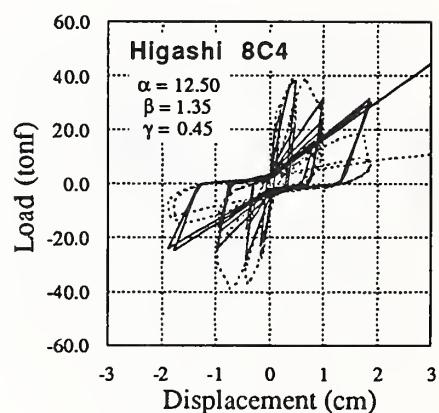
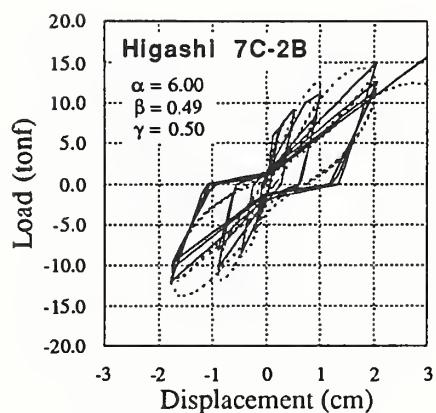
## APPENDIX C. (Continued)



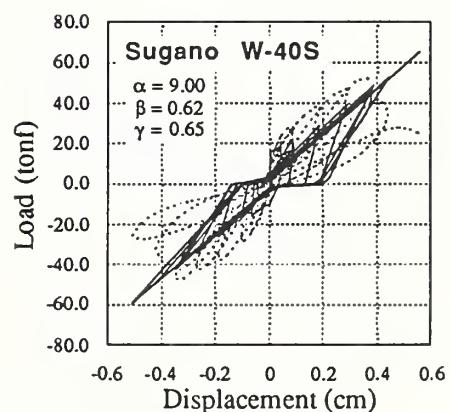
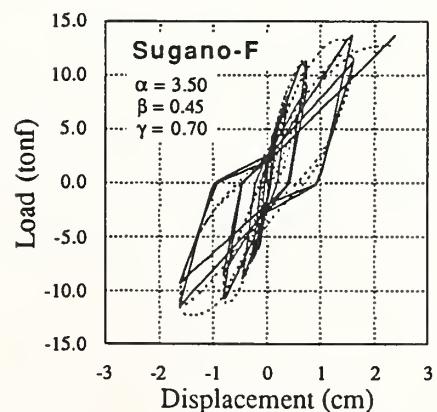
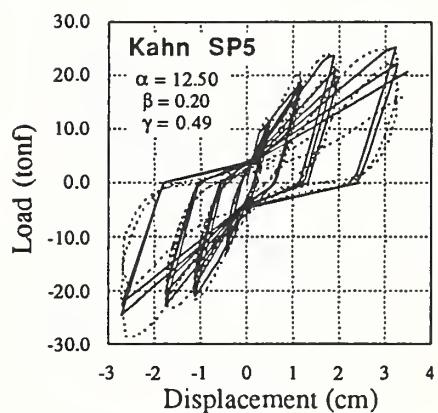
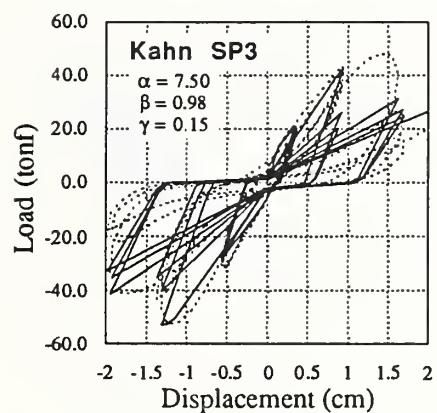
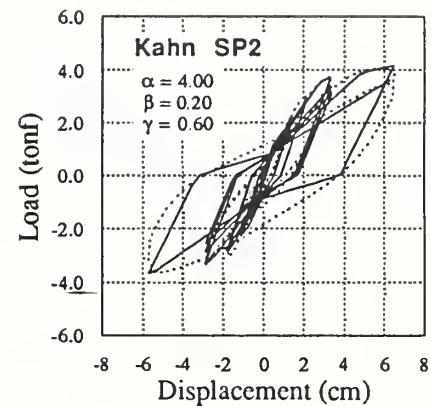
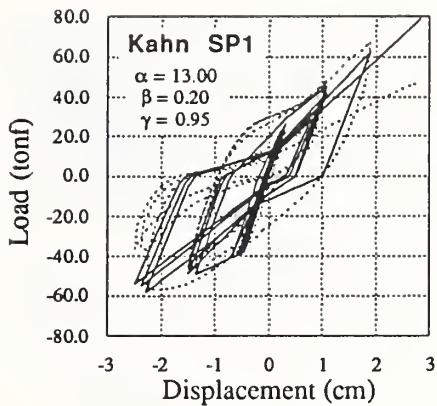
## APPENDIX C. (Continued)



## APPENDIX C. (Continued)



## APPENDIX C. (Continued)



## APPENDIX C. (Continued)

